

## PROGRAM TESTING IN LOOP-EXIT SCHEMES

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**REZUMAT.** - Testarea schemelor Loop-Exit. În această lucrare se introduce noţiunea de drum complet într-o schemă Loop-Exit şi se arată importanţa drumurilor complete într-o schemă program pentru testarea programelor. De asemenea, se construieşte un limbaj care generează mulţimea drumurilor complete.

**1. Introduction.** In this paper we consider the Loop-Exit Schemes as they were defined in [2]. Nevertheless, we impose a minor condition: there is an initial assignement  $a_0$  just at the begining (after START block in the corresponding flowchart), and a final assignment  $a_f$  at the end (in front of the STOP block).  $A$  and  $T$  are the sets of assignment and test symbols, respectively, and  $M = A \cup T$ . Also, we denote by  $SW(S)$  the skeleton word associated to  $S$ , and we denote by  $D(xay)$  the direct word from  $x$  to  $y$  (as in [4]).

To each Loop-Exit Scheme  $S$  a language  $L(S)$  may be associated. More exactly, we have the following definition:

**DEFINITION 1.** The language  $L(S)$  associated to the Loop-Exit Scheme  $S$  is generated by the following context free grammar [1,2,3]:

$$G(S) = (N, \Sigma, P, \varphi)$$

where

$$N = \{\varphi\} \cup \{I_j | j > 0\} \cup \{L_k | k > 0\},$$

$$\Sigma = M \cup \{+, -\}$$

$I_j$  is a nonterminal for  $IF_j$ , and  $L_k$  and  $B_k$  are two nonterminals

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for  $LOOP_k$  from the definition of the Loop-Exit Scheme  $S$ ,  $\nabla$  is a new symbol - the axiom of  $G(S)$ , and the set  $\mathcal{P}$  of the productions is constructed by the following rules:

a)  $\nabla \rightarrow SW(S)$

b) the following productions

b1)  $I_j \rightarrow b-$

b2)  $I_j \rightarrow b+SW(\alpha)$  only if  $\alpha$  has not the form  $\alpha'EXIT_k$

are in  $\mathcal{P}$  if

$IF_j b THEN_j \alpha ENDIF_j ;$

is in  $S$ .

c) the productions

c1)  $I_j \rightarrow b+SW(\alpha)$  if  $\alpha \neq \alpha'EXIT_k$ ;

c2)  $I_j \rightarrow b-SW(\beta)$  if  $\beta \neq \beta'EXIT_k$ ;

are in  $\mathcal{P}$  if

$IF_j b THEN_j \alpha ELSE_j \beta ENDIF_j ;$

is in  $S$ .

d) if

$LOOP_k \alpha_1 \alpha_2 \delta ENDLOOP_k ;$

is in  $S$  then the productions

d1)  $L_k \rightarrow SW(\alpha_1 \alpha_2 \delta) L_k$

d2)  $B_k \rightarrow SW(\alpha_1 \alpha_2 \delta) B_k \mid \epsilon$

d3)  $L_k \rightarrow D(LOOP_k \alpha_1 IF_j) b+SW(\beta)$

if

$\alpha_2 = IF_j b THEN_j \beta EXIT_k; ENDIF_j;$

or

$\alpha_2 = IF_j b THEN_j \beta EXIT_k; ELSE_j \gamma ENDIF_j;$

d4)  $L_k \rightarrow D(LOOP_k \alpha_1 IF_j) b-SW(\beta)$

if

$\alpha_2 = \text{IF}_j \ b \ \text{THEN}_j \ \gamma \ \text{ELSE}_j \ \beta \ \text{EXIT}_k; \ \text{ENDIF}_j;$

are in  $P$ .

Intuitively,  $L(S)$  contains the set of all sequences which can be met during the execution of the scheme.

**2. The complete paths in a Loop-Exit Scheme.** An important problem in software development is program testing. Testing may be done starting from the specification of the resolved problem, or starting from the text of the program. In the second alternative it is important to know all the paths from the START block to the STOP block of the corresponding flow chart. For this purpose we introduce the notion of complete path in a Loop-Exit Scheme.

**DEFINITION 2.** A word  $z = a_{i_1}X_{i_1}a_{i_2}X_{i_2}\dots a_{i_s}X_{i_s}$ , is a section for

$S$  if and only if there is  $w \in L(S)$  such that:

a)  $w = xzy$

b)  $i_j < i_{j+1}$  for  $j=1, 2, \dots, s-1$

c) if  $x \neq \epsilon$  then  $x = x'a_{i_0}X_{i_0}$  with  $i_0 > i_1$

d) if  $y \neq \epsilon$  then  $y = a_{i_{s+1}}X_{i_{s+1}}y'$  with  $i_s > i_{s+1}$ .

The set of all sections is denoted by  $\text{SEC}(S)$ .

The following theorem is proved in [2]:

**THEOREM 1.** For each  $S$  we have  $L(S) \subset (\text{SEC}(S))$ .

**DEFINITION 3.** A word  $z \in \text{SEC}(S)$  is a branch for  $S$  if and only if there is  $w \in L(S)$  such that  $w = zy$ . The set of all branches of  $S$  is denoted by  $\text{BRA}(S)$ .

Next, an algorithm to construct the set  $\text{BRA}(S)$  is given.

**Algorithm 1.** Which constructs the set  $\text{BRA}(S)$ , has the following steps:

**Step 1.** The grammar  $G_1$  has the productions obtained from the productions of  $G(S)$  by replacing the productions

$$B_k \rightarrow \alpha B_k \mid \epsilon,$$

with the production  $B_k \rightarrow \alpha$  and in all the other productions which have not this form the metasymbol  $B_k$  is replaced by  $\epsilon$ .

**Step 2.** Putting off the inaccessible and useless metasymbols of  $G_1$  we obtained the grammar  $G_2$  [1];

**Step 3.** The grammar  $G_3$  is obtained from the grammar  $G_2$  by replacing the productions of the form

$$L_k \rightarrow \alpha L_k$$

by the productions

$$L_k^a \rightarrow \alpha$$

where  $L_k^a$  is a new metasymbol associated to  $L_k$ ;

**Step 4.** The grammar  $G_4$  is constructed from the grammar  $G_3$  by adding to the productions of  $G_3$  some new productions. If  $L_k$  is a recursive symbol in  $G_2$  and  $A \rightarrow \alpha L_k \beta$  is in  $G_3$  then add the

production  $A \rightarrow L_k^a$  to  $G_4$ . Here  $L_k^a$  is the symbol associated

to  $L_k$ .

**Step 5.** One computes  $BRA(S) = L(G_4)$ .

To each metasymbol  $A$  of a grammar

$$G = (N, \Sigma, \mathcal{P}, \nabla)$$

one can associate the grammar

$$G_A = (N, \Sigma, \mathcal{P}, A)$$

which has the metasymbol  $A$  as the axiom.

If  $BRA(A)$  is the result of the application of the algorithm 1 to the grammar  $G_A$  then the following theorem holds [1].

**THEOREM 3.** If  $S$  is a Loop-Exit Scheme then

$$SEC(S) = BRA(S) \cup \{BRA(A) \mid A \text{ is recursive in } G_S^r\},$$

where  $G_S^r$  is the reduced grammar of the scheme  $S$ .

**DEFINITION 4.** For each  $xy^n z \in L(S)$  with  $n \geq 0$  and  $y \in SEC(S)$  the words  $w_1 = xz$  and  $w_2 = xyz$  with  $x = a_0 x_1$  and  $z = z_1 a_f$  (i.e. which contains the assignments  $a_0$  and  $a_f$ ) are called complete paths of the Loop-Exit Scheme. The set of all complete paths of  $S$  is denoted by  $CP(S)$ .

**THEOREM 4.** Let  $G_p$  be the grammar obtained from  $G$  in the following way: if  $A$  is a recursive symbol in  $G$  and

$$A \rightarrow \alpha A \mid \beta_1 \mid \beta_2 \dots \mid \beta_k$$

are all the A-productions of  $G$  then the A-productions of  $G_p$  are

$$A \rightarrow \beta_1 \mid \beta_2 \dots \mid \beta_k \mid \alpha\beta_1 \mid \alpha\beta_2 \dots \mid \alpha\beta_k$$

The language generated by the grammar  $G_p$  generates  $CP(S)$ .

The proof of this theorem follows immediately from the definition 4.

To illustrate these we consider the following Loop-Exit Scheme:

```

a1 a2
LOOP1
    IF1 a3 THEN1 EXIT1 ENDIF1
    IF2 a4 THEN2 a5
        ELSE2 a6 a7 a8 ENDIF2
    ENDLOOP1
a9

```

The grammar  $G(S)$  and the reduced grammar  $G_S^r$  are

$G(S)$

$G_S^r$

$$\nabla \rightarrow a_1 a_2 L_1 a_9$$

$$L_1 \rightarrow I_1 I_2 L_1 \mid a_3^+$$

$$B_1 \rightarrow I_1 I_2 B_1 \mid \epsilon$$

$$I_1 \rightarrow a_3^-$$

$$I_2 \rightarrow a_4 + a_5 \mid a_4 - a_6 a_7 a_8$$

$$\nabla \rightarrow a_1 a_2 L_1 a_9$$

$$L_1 \rightarrow I_1 I_2 L_1 \mid a_3^+$$

$$I_1 \rightarrow a_3^-$$

$$I_2 \rightarrow a_4 + a_5 \mid a_4 - a_6 a_7 a_8$$

For this Loop-Exit Scheme we have

$$BRA(S) = \{ a_1 a_2 a_3 + a_9, a_1 a_2 a_3 - a_4 + a_5, a_1 a_2 a_3 - a_4 - a_6 a_7 a_8 \}$$

and

$$SEC(S) = BRA(S) \sqcup \{ a_3+a_9, a_3-a_4+a_5, a_3-a_4-a_6a_7a_8 \}$$

The grammar  $G_p$  has the following productions:

$$v \rightarrow a_1 a_2 L_1 a_9$$

$$L_1 \rightarrow I_1 I_2 a_3^+ \mid a_3^+$$

$$I_1 \rightarrow a_3^-$$

$$I_2 \rightarrow a_4+a_5 \mid a_4-a_6a_7a_8$$

and the set of the complete paths is

$$CP(S) = \{ a_1a_2a_3+a_9, a_1a_2a_3-a_4+a_5a_3+a_9, a_1a_2a_3-a_4-a_6a_7a_8a_3+a_9 \}.$$

**3. Testing a Loop-Exit Program Scheme.** Similarly to [6] any Loop-Exit Scheme becomes a Program Scheme if the assignments and test symbols are defined as follows.

Let

$$V = \{v_1, v_2, \dots, v_m\} = I \sqcup W \sqcup O$$

be a set of variables, where  $I$  is the set of input variables,  $W$  is the set of working variables, and  $O$  is the set of the output variables. We may suppose, as in [9], that the set  $I$ ,  $W$  and  $O$  are mutually disjoint. Let

$$F = \{f_1, f_2, \dots, f_n\}$$

be a set of functional symbols. We suppose that each assignment  $a \in A$  is of the form

$$v := f(y_1, y_2, \dots, y_k)$$

where  $f \in F$ ,  $k \geq 0$ ,  $y_1, y_2, \dots, y_k \in I \cup W$ , and  $v \in W \cup O$ .

Further, let

$$T = \{t_1, t_2, \dots, t_r\}$$

be a set of test symbols. We suppose that each test symbol of the

Loop-Exit Scheme is of the form

$$t(y_1, y_2, \dots, y_k)$$

where  $t \in T$ ,  $k \geq 0$ , and  $y_1, y_2, \dots, y_k \in I \cup W$ .

DEFINITION 5. A Loop-Exit Scheme  $S$  is a Loop-Exit program Scheme if the symbols  $a \in M$  are defined as above, and for any  $w \in L(S)$  and any  $v \in W$  if  $w = w_1 a x w_2$  and  $a$  is of the form  $t(\dots, v, \dots)$  or  $u := f(\dots, v, \dots)$  then there is  $a' \in A$  of the form  $v := f(y_1, y_2, \dots, y_k)$  such that  $w = w' a' w'' a x w_2$ .

As an example, from the Loop-Exit Scheme given above we obtain the following Program Scheme:

```

d:=n1; i:=n2;
LOOP1
  IF1 d=1 THEN1 EXIT1 ENDIF1
  IF2 d>i THEN2 d:=d-i
      ELSE2 t:=i; i:=d; d:=t ENDIF2
ENDLOOP1

div:=d

```

In other words, the definition 5 asks that any working variable is first initialized and then this variable may be used in computation.

The condition of the definition 5, taken from [6], is very strong. An example of a Loop-Exit Program Scheme which do not satisfy this condition but all variables receive their values before their use, is given in [4]. Also, in [4] is shown that a scheme  $S$  is a Program scheme if and only if this condition holds for any  $z \in \text{BRA}(S)$ . It follows that if a variable does not satisfy this condition for every  $z \in \text{BRA}(S)$  then it is certainly an



uninitialised variable. This fact is very important for the verification of the program corectness. Also, it is important for the programmer to be informed about all the uninitialised variables on some branches of the program.

Testing a program [7] means to observe the results obtained if the program is run for some testing data. A run is needed for each complete path. Therefore, for program testing it is very important to know all of its complete paths.

Knowing a complete path is also useful for choosing the coresponding testing data. If the input variables receives these data the program follows this path. That is, all test conditions met in this path are satisfied.

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