

COURSE DESCRIPTION

Modular arithmetics and cryptography

Academic year 2026-2027

1. Programme-related data

| | |
|------------------------------------|----------------------------------|
| 1.1. Higher education institution | Babeş-Bolyai University |
| 1.2. Faculty | Mathematics and Computer Science |
| 1.3. Department | Mathematics |
| 1.4. Field of study | Computer Science |
| 1.5. Study cycle | Master |
| 1.6. Study programme/Qualification | Data bases |
| 1.7. Form of education | Full-time education |

2. Course-related data

| | | | | | |
|--------------------------|---|---------------|------------------|-------------------------|----------------|
| 2.1. Course title | Modular arithmetics and cryptography | | | Course code | MME3051 |
| 2.2. Course coordinator | Prof. PhD. Septimiu Crivei | | | | |
| 2.3. Seminar coordinator | Prof. PhD. Septimiu Crivei | | | | |
| 2.4. Year of study | 1 | 2.5. Semester | 1 | 2.6. Type of assessment | Exam |
| 2.7. Course status | Optional | | 2.8. Course type | Core subject | |

3. Total estimated time (hours per semester of teaching activities)

| | | | | | |
|---|----|-----------------------|----|-----------------------------------|--------------|
| 3.1. Number of hours per week | 3 | of which: 3.2. course | 2 | 3.3. seminar/ laboratory/ project | 1 |
| 3.4. Total of hours in the curriculum | 42 | of which: 3.5. course | 28 | 3.6. seminar/ laboratory | 14 |
| Time allocation for individual study (IS) and self-taught activities (ST) | | | | | hours |
| Learning from textbooks, course materials, bibliography, and notes (IS) | | | | | 28 |
| Additional research in the library, on subject-specific electronic platforms, and on-site | | | | | 28 |
| Preparing seminars/ laboratories/ projects, assignments, reports, portfolios, and essays | | | | | 28 |
| Tutoring (professional guidance) | | | | | 10 |
| Examinations | | | | | 14 |
| Other activities | | | | | 0 |
| 3.7. Total hours of individual study (IS) and self-taught activities (ST) | | | | 108 | |
| 3.8. Total hours per semester | | | | 150 | |
| 3.9. Number of credits | | | | 6 | |

4. Prerequisites (where applicable)

| | |
|-------------------------|--|
| 4.1. curriculum-related | |
| 4.2. skills-related | |

5. Specific conditions (where applicable)

| | |
|---------------------------------|--|
| 5.1. course-related | |
| 5.2. seminar/laboratory-related | |

6.1. Competencies resulting from the completion of the degree programme (as referred to in the curriculum)¹

| Professional competencies | |
|---------------------------|---|
| Competency code | Competency |
| CP1 | Advanced knowledge of theoretical, methodological, and practical developments in computer science |
| CP3 | Use advanced skills to develop and conduct complex software projects, of practical and/or research nature, using a wide range of quantitative and qualitative methods |
| Transversal competencies | |
| Competency code | Competency |
| CT1 | Systematic use of computer science knowledge to model and interpret new situations, within application contexts larger than the known ones |
| CT4 | Team work abilities, assuming different execution and leading roles, performing professional tasks with considerable amounts of autonomy and responsibility |

6.2. Learning outcomes relevant to the degree programme (as referred to in the curriculum)²

| Learning outcomes targeted by the subject | | |
|---|--|--|
| Competency code | Knowledge and comprehension | Specific academic skills |
| CF1 | Absolventul/a posedă cunoștințe fundamentale de modelare prin care analizează probleme din viața reală, le transpune în cerințe concrete și elaborează un model software corespunzător | Absolventul/a demonstrează abilități avansate de programare care vor permite acumularea de cunoștințe solide și înțelegerea rapidă a tehnologiilor moderne din domeniu |

7. Subject-specific learning outcomes

| Knowledge and comprehension |
|--|
| 1. The student is able to ensure the formation of skills specific to the Mathematics and Algorithmics-related disciplines needed to complete the assignments. |
| 2. The student knows fundamental notions related to Cryptography, and methods of applying them to areas of science related to Mathematics and Computer Science. |
| Specific academic skills |
| 1. The graduate will develop mathematical and algorithmical thinking, progressing from a procedural/computational understanding of mathematics to a broad understanding encompassing logical reasoning, generalization, abstraction, and formal proof. |

8. Contents

| 8.1. Course | Teaching and learning methods | Remarks ³ |
|--|-------------------------------|----------------------|
| 1. Algorithm complexity, modular arithmetics | exposition, algorithmization | |
| 2. Primality and factorization | exposition, algorithmization | |

¹ The professional and/or transversal skills targeted by the subject for which the course description is prepared will be copied from the curriculum of the degree programme. For each competency, the complete entry, including the competency code, will be copied with the exact wording that appears in the curriculum, without any changes. If no competency is copied from either of the two categories, the row corresponding to that category is deleted from the table.

² The learning outcomes relevant to the degree programme and targeted by the subject for which the course description is prepared will be listed. The entries, copied without any changes from the Curriculum by subject type (Core Subject/Specialisation Subject/Complementary Subject), are listed under the corresponding competency.

³ For example, organisational aspects, recommendations for students, specific aspects relating to the course/seminar, such as inviting experts in the field, etc.

| | | |
|--|------------------------------|--|
| 3. Finite fields and discrete logarithms | exposition, algorithmization | |
| 4. Classical cryptography | exposition, algorithmization | |
| 5. DES, AES | exposition, algorithmization | |
| 6. Stream ciphers | exposition, algorithmization | |
| 7. Block ciphers | exposition, algorithmization | |
| 8. RSA cryptosystem | exposition, algorithmization | |
| 9. ElGamal cryptosystem | exposition, algorithmization | |
| 10. Hash functions | exposition, algorithmization | |
| 11. Digital signatures | exposition, algorithmization | |
| 12. Key-related protocols | exposition, algorithmization | |
| 13. Elliptic curve cryptography | exposition, algorithmization | |
| 14. Quantum cryptography | exposition, algorithmization | |

Bibliography

1. M. Cozzens, S.J. Miller, *The Mathematics of Encryption: An Elementary Introduction*, American Mathematical Society, 2013.
2. S. Crivei, A. Marcus, C. Sacarea, C. Szanto, *Computational algebra with applications to coding theory and cryptography*, Editura EFES, Cluj-Napoca, 2006.
3. C. Gherghe, D. Popescu, *Criptografie. Coduri. Algoritmi*, Editura Univ. Bucuresti, 2005.
4. A.J. Menezes, P.C. van Oorschot, S.A. Vanstone, *Handbook of Applied Cryptography*, CRC Press, Boca Raton, 1997. [<http://www.cacr.math.uwaterloo.ca/hac>]
5. C. Paar, J. Pelzl, *Understanding Cryptography*, Springer, 2009.

| 8.2. Seminar/ laboratory | Teaching and learning methods | Remarks |
|--|-------------------------------|---|
| 1. Algorithm complexity, modular arithmetics | problematization, exercise | The seminar is scheduled as 2 hours every second week |
| 2. Primality and factorization | problematization, exercise | |
| 3. Finite fields and discrete logarithms | problematization, exercise | |
| 4. Classical cryptography | problematization, exercise | |
| 5. Block ciphers | problematization, exercise | |
| 6. Public-key cryptography | problematization, exercise | |
| 7. Digital signatures | problematization, exercise | |



















Bibliography

1. M. Cozzens, S.J. Miller, *The Mathematics of Encryption: An Elementary Introduction*, American Mathematical Society, 2013.
2. S. Crivei, A. Marcus, C. Sacarea, C. Szanto, *Computational algebra with applications to coding theory and cryptography*, Editura EFES, Cluj-Napoca, 2006.
3. C. Gherghe, D. Popescu, *Criptografie. Coduri. Algoritmi*, Editura Univ. Bucuresti, 2005.
4. A.J. Menezes, P.C. van Oorschot, S.A. Vanstone, *Handbook of Applied Cryptography*, CRC Press, Boca Raton, 1997. [<http://www.cacr.math.uwaterloo.ca/hac>]
5. C. Paar, J. Pelzl, *Understanding Cryptography*, Springer, 2009.

9. Evaluation

| | | | |
|-------------------------------------|---------------------------------------|-------------------------------------|-----------------------------------|
| Type of activity | 9.1 Evaluation criteria ⁴ | 9.2 Evaluation methods ⁵ | 9.3 Percentage in the final grade |
| 9.4. Course | Use of basic concepts in examples | Presentation | 1/3 of the grade |
| | | | |
| 9.5. Seminar/ laboratory | Problem solving, project presentation | Test, practical examination | 2/3 of the grade |
| | | | |
| 9.6 Minimum standard for passing | | | |
| The final grade must be at least 5. | | | |

10. SDG labels (Sustainable Development Goals)⁶

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|--|--|--|--|--|--|--|--|---|
|  | <input type="radio"/> | Sustainable Development Generic Label | | | | | | |
|  |  |  |  |  |  |  |  |  |
| <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | X |
|  |  |  |  |  |  |  |  | No label applies |
| <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> |

Date of entry:
15.04.2026

Signature of course coordinator

Prof. PhD. Septimiu Crivei

Signature of seminar coordinator

Prof. PhD. Septimiu Crivei

Date of approval in the department:
23.04.2026

Signature of the head of department

Prof. PhD. Andrei Mărcuș

⁴ The evaluation criteria must directly reflect the learning outcomes targeted at the level of the degree programme respectively at the level of the subject. More specifically, the learning outcomes set out in the expected learning outcomes are assessed.

⁵ Both final evaluation methods and ongoing evaluation strategies should be established.

⁶ Select a single label which, according to the [Implementation of SDG labels in the academic process](#), best matches the subject. If the subject addresses sustainable development in a generic manner (i.e. by presenting/introducing the general framework of sustainable development, etc.), then the Sustainable Development generic label may be applied. If none of the labels describe the subject, select the last option: “No label applies.”

