

## SYLLABUS

### Probability Theory and Statistics

University year 2025-2026

#### 1. Information regarding the programme

1.1 Higher education institution	<b>Babeş-Bolyai University</b>
1.2 Faculty	<b>Faculty of Mathematics and Computer Science</b>
1.3 Department	<b>Department of Computer Science</b>
1.4 Field of study	<b>Computer and Information Technology</b>
1.5 Study cycle	<b>Bachelor</b>
1.6 Study programme / Qualification	<b>Information Engineering</b>
1.7 Form of education	<b>Full-Time</b>

#### 2. Information regarding the discipline

2.1 Name of the discipline		Probability Theory and Statistics				Discipline code		MLE0090
2.2 Course coordinator			Prof. Sanda Micula, PhD. Habil.					
2.3 Seminar coordinator			Prof. Sanda Micula, PhD. Habil.					
2.4. Year of study	2	2.5 Semester	3	2.6. Type of evaluation	E	2.7 Type of discipline	DF Compulsory	

#### 3. Total estimated time (hours/semester of didactic activities)

3.1 Hours per week	<b>4</b>	Of which: 3.2 course	<b>3</b>	3.3 seminar/laboratory	<b>1 lab</b>
3.4 Total hours in the curriculum	<b>56</b>	Of which: 3.5 course	<b>42</b>	3.6 seminar/laboratory	<b>14</b>
<b>Time allotment for individual study (ID) and self-study activities (SA)</b>					hours
Learning using manual, course support, bibliography, course notes (SA)					25
Additional documentation (in libraries, on electronic platforms, field documentation)					15
Preparation for seminars/labs, homework, papers, portfolios and essays					25
Tutorship					9
Evaluations					20
Other activities: .....					-
3.7 Total individual study hours	94				
3.8 Total hours per semester	150				
3.9 Number of ECTS credits	6				

#### 4. Prerequisites (if necessary)

4.1. curriculum	<ul style="list-style-type: none"> <li>Mathematical Analysis</li> <li>Algebra</li> </ul>
4.2. competencies	<ul style="list-style-type: none"> <li>Logical thinking</li> <li>Average logical programming skills</li> </ul>

#### 5. Conditions (if necessary)

5.1. for the course	<ul style="list-style-type: none"> <li>Lecture room with large blackboard and video projector</li> </ul>
5.2. for the seminar /lab activities	<ul style="list-style-type: none"> <li>For lab: Laboratory with computers having Matlab installed</li> </ul>

## 6. Specific competencies acquired

Professional competencies	<p>C1.1 Recognizing and describing specific concepts to calculability, complexity, programming paradigms and modeling of computing and communication systems</p> <p>C1.2 Using specific theories and tools (algorithms, schemes, models, protocols, etc.) for explaining the structure and the functioning of hardware, software and communication systems</p> <p>C1.3 Building models for various components of computing systems</p> <p>C1.5 Providing theoretical background for the characteristics of the designed systems</p>
Transversal competencies	<p>CT1 Honorable, responsible, ethical behavior, in the spirit of the law, to ensure the professional reputation</p> <p>CT3 Demonstrating initiative and pro-active behavior for updating professional, economical and organizational culture knowledge</p>

## 7. Objectives of the discipline (outcome of the acquired competencies)

7.1 General objective of the discipline	<ul style="list-style-type: none"> <li>Acquire basic knowledge of Probability Theory and Mathematical Statistics, with main focus on applications</li> </ul>
7.2 Specific objective of the discipline	<ul style="list-style-type: none"> <li>Become familiar and be able to work with various probabilistic and statistical models</li> <li>Ability to perform statistical analysis of data</li> <li>Ability to use statistical features of various mathematical software</li> </ul>

## 8. Content

8.1 Course	Teaching methods	Remarks
1. Experiments, events, field of events, operations with events. Axiomatic definition of probability. Poincaré's formula. Classical definition of probability.	<ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul>	
2. Conditional probability. Independent events. Total probability formula. Classical probabilistic models (Binomial, Hypergeometric, Poisson, Pascal, Geometric).	<ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul>	
3. Random variables and random vectors. Discrete random variables. Probability distribution function. Cumulative distribution function. Properties, examples.	<ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul>	
4. Discrete probability laws (Bernoulli, Binomial, Hypergeometric, Poisson, Negative Binomial, Geometric). Discrete random vectors. Operations with discrete random variables.	<ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul>	
5. Continuous random variables. Probability density function. Continuous probability laws (Uniform, Normal, Gamma, Exponential, Chi-square, Student, Fisher). Independent random variables. Functions of continuous random variables.	<ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul>	
6. Numerical characteristics of random variables. Expectation. Variance and standard deviation. Median. Moments (initial, central, absolute).	<ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul>	

7. Quantiles. Covariance and correlation coefficient. Inequalities (Markov, Chebyshev). Central limit theorem.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	
8. Descriptive statistics. Data collection. Graphical display of data. Frequency distribution, histograms, stem-and-leaf plots. Parameters of a statistical distribution. Measures of central tendency.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	
9. Measures of variation. Correlation and regression. Linear regression, least squares estimation.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	
10. Statistical inference. Sample theory. Samples. Sample functions (sample mean, sample variance, sample moments). Estimation theory, basic notions. Confidence intervals for estimating the population mean and the population variance.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	
11. Confidence intervals for comparing two population means and two population variances. Hypothesis testing, basic notions. Rejection region. Type I errors. Significance testing and P-values.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	
12. Tests for the parameters of one population. Tests for comparing the parameters of two populations. Examples. Robust tests. Summary of hypothesis testing.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	
13. Properties of point estimators. Unbiased and minimum variance estimators. Fisher's information. Absolutely correct estimators. The Rao-Cramer inequality. Efficient estimators. Methods of estimation (method of moments, method of maximum likelihood). Examples.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	
14. Type II errors and the power of a test. Most powerful tests and the Neyman-Pearson lemma. Uniformly most powerful tests. Examples.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul>	

#### Bibliography

1. Micula, S., Probability and Statistics for Computational Sciences, Cluj University Press, 2009.
2. Baron, M., Probability and Statistics for Computer Scientists, 3<sup>rd</sup> edition, CRC Press, Taylor and Francis, Boca Raton, FL, 2019.
3. Milton, J.S., Arnold, J. C., Introduction to Probability and Statistics: Principles and Applications for Engineering and the Computing Sciences, 3rd Edition. McGraw-Hill, New York, 1995.
4. Blaga, P., Calculul probabilitatilor si statistica matematica. Vol. II. Curs si culegere de probleme, Universitatea "Babes-Bolyai" Cluj-Napoca, 1994.
5. Feller, W., An introduction to probability theory and its applications, Vol. 1, 3<sup>rd</sup> edition, WSE Wiley, New York, 2008.
6. DeGroot, M. H., Schervish, M. J., Probability and Statistics, Addison-Wesley, Boston, 2012.

8.2 Laboratory	Teaching methods	Remarks
1. Introduction to Matlab.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>	The lab is structured as 2 hours per week, every other week
2. Estimating probability by computer simulations.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> </ul>	

	<ul style="list-style-type: none"> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>	
3. Discrete random variables. PDF and CDF.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>	
4. Continuous random variables. PDF, CDF and Inverse CDF.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Synthesis</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>	
5. Descriptive Statistics. Statistical measures. Correlation and regression.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>	
6. Confidence intervals and tests for the mean and variance.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>	
7. Confidence intervals and tests for the difference of means and ratio of variances.	<ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual work</li> </ul>	
<b>Bibliography</b> <ol style="list-style-type: none"> <li>1. Micula, S., Probability and Statistics for Computational Sciences, Cluj University Press, 2009.</li> <li>2. Baron, M., Probability and Statistics for Computer Scientists, 3<sup>rd</sup> edition, CRC Press, Taylor and Francis, Boca Raton, FL, 2019.</li> <li>3. Blaga, P., Statistica prin Matlab, Presa Universitara Clujeana, Cluj-Napoca, 2002.</li> <li>4. Lisei, H., Micula, S., Soos, A., Probability Theory trough Problems and Applications, Cluj University Press, 2006.</li> <li>5. Milton, J.S., Arnold, J. C., Introduction to Probability and Statistics: Principles and Applications for Engineering and the Computing Sciences, 3rd Edition. McGraw-Hill, New York, 1995.</li> </ol>		

**9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program**


- The course follows the ACM and IEEE Curriculum Recommendations for Information Engineering students;
- The course exists in the studying program of all major universities in Romania and abroad;
- The knowledge and skills acquired in this course give students a foundation for launching a career in scientific research;
- The statistical analysis abilities acquired in this course are useful in any career path students may choose.

## 10. Evaluation

Type of activity	10.1 Evaluation criteria	10.2 Evaluation methods	10.3 Share in the grade (%)
10.4 Course	<ul style="list-style-type: none"> <li>- acquire the basic principles in Probability Theory and Mathematical Statistics;</li> <li>- be able to apply correctly the course concepts on various applications</li> <li>- be able to apply course concepts and techniques on practical problems</li> <li>- problem solving</li> </ul>	<p><b>Written exam</b></p> <ul style="list-style-type: none"> <li>- participation in discussing and solving problems throughout the semester</li> <li>- additional documentation</li> <li>- solving bonus problems</li> </ul>	<p><b>70%</b></p> <p><b>15%</b></p>

10.5 Lab activities	- be able to implement course concepts and algorithms in Matlab - be able to solve numerical statistical problems in Matlab	- participation in discussing and solving problems throughout the semester - individual presentation of solutions	<b>15%</b>
10.7 Minimum performance standards			
➤ A grade of 5 or above (on a scale from 1 to 10) on <b>each</b> of the three activities mentioned above (written test, participation, lab evaluation)			

## 11. Labels ODD (Sustainable Development Goals)<sup>1</sup>

	General label for Sustainable Development							
								

Date

Signature of course coordinator

Signature of seminar coordinator

29.04.2025

Prof. Sanda Micula, PhD. Habil.

Prof. Sanda Micula, PhD. Habil.

Date of approval

Signature of the head of department

Prof. dr. Andrei Mărcuș

<sup>1</sup> Keep only the labels that, according to the [Procedure for applying ODD labels in the academic process](#), suit the discipline and delete the others, including the general one for *Sustainable Development* – if not applicable. If no label describes the discipline, delete them all and write „Not applicable.”.