#### **SYLLABUS**

## 1. Information regarding the programme

1.1 Higher education	Babes-Bolyai University
institution	
1.2 Faculty	Faculty of Mathematics and Computer Science
1.3 Department	Department of Mathematics
1.4 Field of study	Mathematics and Informatics
1.5 Study cycle	Bachelor
1.6 Study programme /	Mathematics and Informatics
Qualification	

## 2. Information regarding the discipline

2.1 Name of the	dis	scipline	Special Chapters of Ordinary Differential Equations					
2.2 Course coordinator Conf. dr. Adriana Buică								
2.3 Seminar coordinator Conf. dr. Adriana Buică								
2.4. Year of	2	2.5	4	2.6. Type of VP 2.7 Type of DS				
study		Semester		evaluation discipline				

### 3. Total estimated time (hours/semester of didactic activities)

3.1 Hours per week	4	Of which: 3.2 course	2	3.3	2
				seminar/laboratory	
3.4 Total hours in the curriculum	56	Of which: 3.5 course	28	3.6	28
				seminar/laboratory	
Time allotment:					hours
Learning using manual, course support, bibliography, course notes					30
Additional documentation (in libraries, on electronic platforms, field documentation)					10
Preparation for seminars/labs, homework, papers, portfolios and essays					40
Tutorship					10
Evaluations					4
Other activities:					-
3.7 Total individual study hours		94			•

3.7 Total individual study hours	94
3.8 Total hours per semester	150
3.9 Number of ECTS credits	6

## 4. Prerequisites (if necessary)

4.1. curriculum	First Course on Differential Equations
4.2. competencies	Mathematical analysis

## **5. Conditions** (if necessary)

5.1. for the course	Classroom with blackboard
5.2. for the seminar /lab	Classroom with blackboard
activities	

6. Specific competencies acquired

Professional competencies	C 2.4. To recognize the main types of mathematical problems and to be able to select the proper techniques and methods for solving them. C 4.2. To explain and give a proper interpretation of the mathematical models. C 5.2. To be able to use the mathematical reasoning in the proofs.
<b>Transversal</b> competencies	<ul> <li>CT1 To apply the rules of organized and efficient work, of responsible attitudes toward the didactic-scientific domain, for the creative valorization of their own potential, respecting the principles and the norms of the professional ethic.</li> <li>CT3 To use some efficient methods and techniques to learn, to inform themselves, to do research and to develop the abilities for the valorization of their knowledges, to adapt to a dynamical society, and to communicate.</li> </ul>

# 7. Objectives of the discipline (outcome of the acquired competencies)

7.1 General objective of the discipline	A deeper understanding of the notions, results and applications of the theory of differential equations
7.2 Specific objective of the discipline	<ul> <li>To understand the different phenomena of dependence on initial conditions and parameters: continuous dependence, stability, topological equivalence, structural stability, bifurcations</li> <li>Introduction to the existence and stability of the equilibria and of the periodic solutions</li> </ul>

### 8. Content

8.1 Course	Teaching methods	Remarks
The first notions and problems in the qualitative theory of scalar nonautonomous differential equations.	<ul> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul>	
2. Maximal solutions.		
<ol> <li>Lower and upper solutions, direction field, symmetries of differential equations</li> </ol>		
4. Continuity and differentiability with respect to the initial data and parameters		
5. Scalar continuous dynamical systems.		
6. Scalar discrete dynamical systems.		
7. Scalar periodic differential equations: Massera's theorem. Test.		
8. Scalar periodic differential equations: The Poincare map.		
<ol><li>Scalar periodic differential equations: The averaging method.</li></ol>		
<ol> <li>Planar autonomous systems: first integrals an conservative systems.</li> </ol>	d	
<ol> <li>11. Linear planar autonomous systems.</li> <li>Topological equivalence.</li> </ol>		

12. Stability of equilibria of planar systems.	
13. Topological equivalence of two planar systems in a neighborhood of a hyperbolic equilibrium point. Test.	
14. Interesting phenomena in the theory of dynamical systems.	

#### **Bibliography**

- 1. A. Buica, Lecture notes available at the webpage <a href="http://www.math.ubbcluj.ro/~abuica/csEcDif.htm">http://www.math.ubbcluj.ro/~abuica/csEcDif.htm</a> or posted in Teams
- 2. P. Blanchard, R.L. Devaney, G.R. Hall, Differential Equations, Brooks/Cole, Cengage Learning, 2012.
- 3. J. Hale, H. Koçak, Dynamics and bifurcations, Springer-Verlag, 1991.

4. R.Precup, Ecuatii diferentiale, Risoprint, Cluj-Napoca, 2011.

8.2 Seminar / laboratory	Teaching methods	Remarks
1-4. The study of scalar nonautonomous differential	• Explanation	
equations.	<ul> <li>Conversation</li> </ul>	
	Didactical	
	demonstration	
5 Scalar autonomous differential equations: the study of		
some population dynamics models depending on some		
parameters.		
6. Scalar discrete dynamical systems: stability of fixed		
points		
7-10. Scalar autonomous periodic equations: the study of		
some population dynamics models.		
11-12. Planar autonomous systems: the harmonic		
oscillator equation, the pendulum equation, the		
Lotka-Volterra system.		
13-14. Planar autonomous systems: stability of equilibria.		

#### **Bibliography**

- 1. Lecture notes posted on the webpage of the course <a href="http://www.math.ubbcluj.ro/~abuica/csEcDif.htm">http://www.math.ubbcluj.ro/~abuica/csEcDif.htm</a> or in Teams
- 2. P. Blanchard, R.L. Devaney, G.R. Hall, Differential Equations, Brooks/Cole, Cengage Learning, 2012.
- 3. J. Hale, H. Koçak, Dynamics and bifurcations, Springer-Verlag, 1991.
- 4. R. Precup, Differential equations, De Gruyter, 2018.

# 9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

The content of this discipline is synchronized with the curriculum of most of the important universities from our country and from abroad where the applied mathematics plays an important role.

#### 10. Evaluation

Type of activity	10.1 Evaluation criteria	10.2 Evaluation methods	10.3 Share in the
10.4 Course	To know the notions and their properties by examples or	Two tests	grade (%) 60%
	counterexamples. To be able to apply the theoretical results in		

	concrete problems.		
10.5 Seminar activities	Solving problems skills through homeworks		30%
10.6 Minimum performance standards			
The minimum passing grade is 5.			

Date Signature of course coordinator Signature of seminar coordinator

20-04-2023 Conf. dr. Adriana Buică Conf. dr. Adriana Buică

Date of approval Signature of the head of department

20-04-2023 Prof. dr. Andrei Mărcuș