SYLLABUS

## 1. Information regarding the programme

| 1.1 Higher education <br> institution | Babeş-Bolyai University |
| :--- | :--- |
| 1.2 Faculty | Faculty of Mathematics and Computer Science |
| 1.3 Department | Department of Mathematics |
| 1.4 Field of study | Mathematics |
| 1.5 Study cycle | Bachelor |
| 1.6 Study programme / <br> Qualification | Mathematics and Computer Science |

## 2. Information regarding the discipline

| 2.1 Name of the dis (ro) |  |  | Geometrie 2 Geometrie 2 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.2 Course coordinator |  |  |  |  | Lect. Dr. Iulian Simion |  |  |  |
| 2.3 Seminar coordinator |  |  |  |  | Lect. Dr. Iulian Simion |  |  |  |
| 2.4 Year of study | 1 |  | Semester | 2 | 2.6. Type of evaluation | VP | 2.7 Type of discipline | Compulsory |
| 2.8 Disciplinei code |  |  | E0015 |  |  |  |  |  |

3. Total estimated time (hours/semester of didactic activities)

| 3.1 Hours per week | 4 | Of which: 3.2 course | 2 | 3.3 seminar | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3.4 Total hours in the curriculum | 56 | Of which: 3.5 course | 28 | 3.6 seminar | 28 |
| Time allotment: |  |  |  |  | hours |
| Learning using manual, course support, bibliography, course notes |  |  |  |  | 20 |
| Additional documentation (in libraries, on electronic platforms, field documentation) |  |  |  |  | 20 |
| Preparation for seminars/labs, homework, papers, portfolios and essays |  |  |  |  | 35 |
| Tutorship |  |  |  |  | 15 |
| Evaluations |  |  |  |  | 3 |
| Other activities: ................ |  |  |  |  | 1 |
| 3.7 Total individual study hours |  | 94 |  |  |  |
| 3.8 Total hours per semester |  | 150 |  |  |  |
| 3.9 Number of ECTS credits |  | 6 |  |  |  |

4. Prerequisites (if necessary)

| 4.1 curriculum | • <br>  <br> • A A first course on analytic geometry |
| :--- | :--- |
| 4.2 competencies |  |

5. Conditions (if necessary)
5.1 for the course
5.2 for the seminar /lab activities
6. Specific competencies acquired

|  | ${ } \wedge$ C1.1 Idetifying the notions, describing the theories and using the specific language <br> $\urcorner_{\imath}$ C2.3 Applying the adequate analytical theoretical methods to a given problem |
| :---: | :---: |
| Transversal competencies | ${ }_{7 \wedge}$ CT1. Applying some rules of precise and efficient work, showing a responsible attitude regarding the the scientific domain and teaching training for an optimal and creative development of the personal potential in specific situations, respecting the deontological norms. |

7. Objectives of the discipline (outcome of the acquired competencies)

| 7.1 General objective of the <br> discipline | Basic notions and methods în the context of affine geometry |
| :--- | :--- |
| 7.2 Specific objective of the <br> discipline | Affine transformations <br> Classification of quadrics <br> Projective transformations |

## 8. Content

| 8.1 Course | Teaching methods | Remarks |
| :--- | :--- | :--- |
| 1-2. Affine spaces <br> - Geometric vectors <br> - Vector space structure <br> - Cartesian coordinate frames <br> - Changing coordinates <br> - Affine subspaces <br> - Hyperplanes | Exposition, proofs, | Two lectures |
| 3-4. Euclidean spaces <br> - Scalar product <br> - Gram matrix |  |  |


| - Orthonormal frames <br> - Gram-Schmidt process <br> - Applications <br> - Spectral Theorem |  |  |
| :---: | :---: | :---: |
| 5. Orientation <br> - Box product <br> - Cross product <br> - Properties <br> - Applications | Exposition, proofs, examples |  |
| 6. Affine maps <br> - Parallel projections and reflections <br> - Orthogonal projections and reflections | Exposition, proofs, examples |  |
| 7. Isometries <br> - Rotations in dimension 2 and 3 <br> - Displacements <br> - Classification of isometries in dimension 2 and 3 | Exposition, proofs, examples |  |
| 8. Hyperquadrics <br> - Reducing to canonical form <br> - Isometric classification of quadrics <br> - Affine classification of quadrics | Exposition, proofs, examples |  |
| 9-10. Quadratic surfaces <br> - Ellipsoid, Cone, Hyperboloid, Paraboloid <br> - Canonical equation <br> - Tangent planes | Exposition, proofs, examples | Two lectures |
| 11-12. Projective Geometry <br> - Projective line, plane and space <br> - Projective transformations | Exposition, proofs, examples | Two lectures |
| 13-14. Quaternions <br> - Algebraic description <br> - Quaternions and rotations | Exposition, proofs, examples | Two lectures |
| Bibliography <br> [1] I. Simion, Geometry - material de curs, 2024. <br> [2] P.A. Blaga, Geometrie - material de curs, 2019. <br> [3] M. Troyanov, Cours de géométrie, Lausanne, 2011. <br> [4] E. Sernesi, Linear Algebra. A geometric Approach (Translated by J. Montaldi), 2009. |  |  |
| 8.2 Seminar | Teaching methods | Remarks |
| 1-2. Affine spaces <br> - Geometric vectors <br> - Vector space structure <br> - Cartesian coordinate frames <br> - Changing coordinates <br> - Affine subspaces <br> - Hyperplanes | Dialog, problem solving | Two tutorials |

3-4. Euclidean spaces

- Scalar product
- Gram matrix
- Orthonormal frames
- Gram-Schmidt process
- Applications
- Spectral Theorem

5. Orientation

- Box product
- Cross product
- Properties
- Applications

6. Affine maps

- Parallel projections and reflections
- Orthogonal projections and reflections

7. Isometries

- Rotations in dimension 2 and 3
- Displacements
- Classification of isometries in dimension 2 and 3

8. Hyperquadrics

- Reducing to canonical form
- Isometric classification of quadrics
- Affine classification of quadrics

9-10. Quadratic surfaces

- Ellipsoid, Cone, Hyperboloid, Paraboloid
- Canonical equation
- Tangent planes

11-12. Projective Geometry

- Projective line, plane and space
- Projective transformations

13-14. Quaternions

- Algebraic description
- Quaternions and rotations

Bibliography
[1] I. Simion, Geometry - material de curs, 2024.
[2] P.A. Blaga, Geometrie - material de curs, 2019.
[3] M. Troyanov, Cours de géométrie, Lausanne, 2011.
[4] E. Sernesi, Linear Algebra. A geometric Approach (Translated by J. Montaldi), 2009.
9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program
$\urcorner$ The material of this course serves other courses
$7 \wedge$ - a deeper understanding of linear algebra
7 - - affine transformations are necessary examples for a group theory course
ᄀ^ - quadrics are necessary examples in analysis courses
$\urcorner$ - coordinate changes, projections, affine and projective transformations are necessary for computer graphics
$\urcorner$ - Building on a previous geometry course, classification results are presented
$7 \wedge$ Applications of the theory are presented wherever appropriate

## 10. Evaluation

| Type of activity | 10.1 Evaluation criteria | 10.2 Evaluation methods | 10.3 Share in the <br> grade (\%) |
| :--- | :--- | :--- | :--- |
| 10.4 Course | Critical grasp of the <br> learned material, ability to <br> use what was learned | Two written partial exams <br> at the middle and at the end <br> of the semester | $40 \%$ and $60 \%$ <br> respectively |
|  |  | Ability to use the theory <br> for solving problems | Points during the tutorial <br> for active participation |
| 10.5 Seminar | Can lead up to one <br> extra point for the <br> final grade |  |  |

Date
21. February 2024

Signature of course coordinator
Lect. Dr. Iulian Simion

Signature of seminar coordinator
Lect. Dr. Iulian Simion

Date of approval
$\qquad$
Signature of the head of department
Prof. Dr. Andrei Mărcuș

