

SYLLABUS

1. Information regarding the programme

| | |
|-------------------------------------|---|
| 1.1 Higher education institution | Babeş-Bolyai University |
| 1.2 Faculty | Faculty of Mathematics and Computer Science |
| 1.3 Department | Department of Mathematics |
| 1.4 Field of study | Computer Science |
| 1.5 Study cycle | Bachelor |
| 1.6 Study programme / Qualification | Computer Science |

2. Information regarding the discipline

| | | | | | | | |
|----------------------------|-------------------------|--------------|---|-------------------------|----|------------------------|------------|
| 2.1 Name of the discipline | Geometry | | | | | | |
| 2.2 Course coordinator | Lect. Dr. Iulian Simion | | | | | | |
| 2.3 Seminar coordinator | Lect. Dr. Iulian Simion | | | | | | |
| 2.4 Year of study | 1 | 2.5 Semester | 2 | 2.6. Type of evaluation | VP | 2.7 Type of discipline | Compulsory |
| 2.8 Disciplinei code | MLE0014 | | | | | | |

3. Total estimated time (hours/semester of didactic activities)

| | | | | | |
|---|----|----------------------|----|-------------|-------|
| 3.1 Hours per week | 4 | Of which: 3.2 course | 2 | 3.3 seminar | 2 |
| 3.4 Total hours in the curriculum | 56 | Of which: 3.5 course | 28 | 3.6 seminar | 28 |
| Time allotment: | | | | | hours |
| Learning using manual, course support, bibliography, course notes | | | | | 20 |
| Additional documentation (in libraries, on electronic platforms, field documentation) | | | | | 10 |
| Preparation for seminars/labs, homework, papers, portfolios and essays | | | | | 14 |
| Tutorship | | | | | 14 |
| Evaluations | | | | | 11 |
| Other activities: | | | | | - |
| 3.7 Total individual study hours | | | | | 69 |
| 3.8 Total hours per semester | | | | | 125 |
| 3.9 Number of ECTS credits | | | | | 5 |

4. Prerequisites (if necessary)

| | |
|------------------|--|
| 4.1 curriculum | <ul style="list-style-type: none"> Basic knowledge in algebra and calculus. |
| 4.2 competencies | <ul style="list-style-type: none"> Competencies of using the above mentioned curricula. |

5. Conditions (if necessary)

| | |
|-------------------------------------|--|
| 5.1 for the course | |
| 5.2 for the seminar /lab activities | |

6. Specific competencies acquired

| | |
|----------------------------------|--|
| Professional competencies | <ul style="list-style-type: none"> • C1.1 Identifying the notions, describing the theories and using the specific language • C2.3 Applying the adequate analytical theoretical methods to a given problem |
| Transversal competencies | CT1. Applying some rules of precise and efficient work, showing a responsible attitude regarding the the scientific domain and teaching training for an optimal and creative development of the personal potential in specific situations, respecting the deontological norms. |

7. Objectives of the discipline (outcome of the acquired competencies)

| | |
|--|---|
| 7.1 General objective of the discipline | Basic notions and methods in the context of analytic geometry |
| 7.2 Specific objective of the discipline | Classification of quadratic curves and surfaces |

8. Content

| 8.1 Course | Teaching methods | Remarks |
|---|------------------------------|--------------|
| 1-2. Affine spaces <ul style="list-style-type: none"> • Geometric vectors • Vector space structure • Cartesian coordinate frames • Changing coordinates • Affine subspaces in dimension 2 and 3 • Hyperplanes | Exposition, proofs, examples | Two lectures |
| 3-4. Euclidean spaces <ul style="list-style-type: none"> • Scalar product • Gram matrix • Orthonormal frames • Gram-Schmidt process • Applications • Spectral Theorem | Exposition, proofs, examples | Two lectures |
| 5. Orientation <ul style="list-style-type: none"> • Box product • Cross product | Exposition, proofs, examples | |

| | | |
|--|------------------------------|---------------|
| <ul style="list-style-type: none"> • Properties • Applications | | |
| 6. Affine maps <ul style="list-style-type: none"> • Parallel projections and reflections • Orthogonal projections and reflections | Exposition, proofs, examples | |
| 7. Isometries <ul style="list-style-type: none"> • Rotations in dimension 2 and 3 • Displacements • Classification of isometries in dimension 2 and 3 | Exposition, proofs, examples | |
| 8-9. Quadratic curves <ul style="list-style-type: none"> • Ellipse, hyperbola, parabola • Canonical equations • Relative position of a line • Tangent lines | Exposition, proofs, examples | Two lectures |
| 10. Classification of quadrics (dimension 2 and 3) <ul style="list-style-type: none"> • Reducing to canonical form • Isometric classification of quadrics • Affine classification of quadrics | Exposition, proofs, examples | |
| 11-12. Quadratic surfaces <ul style="list-style-type: none"> • Ellipsoid, Cone, Hyperboloid, Paraboloid • Canonical equation • Tangent planes | Exposition, proofs, examples | Two lectures |
| 13. Curvatures <ul style="list-style-type: none"> • Curvature of curves • Curvatures of surfaces | Exposition, proofs, examples | |
| 14. Quaternions <ul style="list-style-type: none"> • Algebraic description • Quaternions and rotations | Exposition, proofs, examples | |
| Bibliography [1] I. Simion, Geometry – material de curs, 2024. [2] P.A. Blaga, Geometrie – material de curs, 2019. [3] M. Troyanov, Cours de géométrie, Lausanne, 2011. [4] E. Sernesi, Linear Algebra. A geometric Approach (Translated by J. Montaldi), 2009. | | |
| 8.2 Seminar | Teaching methods | Remarks |
| 1-2. Affine spaces <ul style="list-style-type: none"> • Geometric vectors • Vector space structure • Cartesian coordinate frames • Changing coordinates • Affine subspaces in dimension 2 and 3 • Hyperplanes | Dialog, problem solving | Two tutorials |
| 3-4. Euclidean spaces <ul style="list-style-type: none"> • Scalar product | Dialog, problem solving | Two tutorials |

| | | |
|--|-------------------------|---------------|
| <ul style="list-style-type: none"> • Gram matrix • Orthonormal frames • Gram-Schmidt process • Applications • Spectral Theorem | | |
| 5. Orientation <ul style="list-style-type: none"> • Box product • Cross product • Properties • Applications | Dialog, problem solving | |
| 6. Affine maps <ul style="list-style-type: none"> • Parallel projections and reflections • Orthogonal projections and reflections | Dialog, problem solving | |
| 7. Isometries <ul style="list-style-type: none"> • Rotations in dimension 2 and 3 • Displacements • Classification of isometries in dimension 2 and 3 | Dialog, problem solving | |
| 8-9. Quadratic curves <ul style="list-style-type: none"> • Ellipse, hyperbola, parabola • Canonical equations • Relative position of a line • Tangent lines | Dialog, problem solving | Two tutorials |
| 10. Classification of quadrics (dimension 2 and 3) <ul style="list-style-type: none"> • Reducing to canonical form • Isometric classification of quadrics • Affine classification of quadrics | Dialog, problem solving | |
| 11-12. Quadratic surfaces <ul style="list-style-type: none"> • Ellipsoid, Cone, Hyperboloid, Paraboloid • Canonical equation • Tangent planes | Dialog, problem solving | Two tutorials |
| 13. Curvatures <ul style="list-style-type: none"> • Curvature of curves • Curvatures of surfaces | Dialog, problem solving | |
| 14. Quaternions <ul style="list-style-type: none"> • Algebraic description • Quaternions and rotations | Dialog, problem solving | |

Bibliography

[1] I. Simion, Geometry – material de curs, 2024.

[2] P.A. Blaga, Geometrie – material de curs, 2019.

[3] M. Troyanov, Cours de géométrie, Lausanne, 2011.

[4] E. Sernesi, Linear Algebra. A geometric Approach (Translated by J. Montaldi), 2009.

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

- The material of this course serves other courses
 - a deeper understanding of linear algebra
 - affine transformations are necessary examples for a group theory course
 - quadrics are necessary examples in calculus courses
 - coordinate changes, projections, affine transformations are necessary for computer graphics
- Applications of the theory are presented wherever appropriate

10. Evaluation

| Type of activity | 10.1 Evaluation criteria | 10.2 Evaluation methods | 10.3 Share in the grade (%) |
|---|---|--|--|
| 10.4 Course | Critical grasp of the learned material, ability to use what was learned | Two written partial exams at the middle and at the end of the semester | 40% and 60% respectively |
| 10.5 Seminar | Ability to use the theory for solving problems | Points during the tutorial for active participation | Can lead up to one extra point for the final grade |
| 10.6 Minimum performance standards | | | |
| 75% attendance at the Seminar At least grade 5 for the final grade (excluding the bonus points obtained during the tutorials). | | | |

Date

21. February 2024

Signature of course coordinator

Lect. Dr. Iulian Simion

Signature of seminar coordinator

Lect. Dr. Iulian Simion

Date of approval

.....

Signature of the head of department