

## SYLLABUS

### 1. Information regarding the programme

|                                     |  |
|-------------------------------------|--|
| 1.1 Higher education institution    | Babes-Bolyai University Cluj-Napoca                        |
| 1.2 Faculty                         | Faculty of Mathematics and Computer Science                |
| 1.3 Department                      | Mathematics  |
| 1.4 Field of study                  | Mathematics  |
| 1.5 Study cycle                     | Bachelor   |
| 1.6 Study programme / Qualification | Mathematics and Computer Science (English) / Mathematician |

### 2. Information regarding the discipline

|                                      |  |              |   |                         |    |                        |    |
|--------------------------------------|--|--------------|---|-------------------------|----|------------------------|----|
| 2.1 Name of the discipline (en) (ro) | Complements of geometry / Complemente de geometrie |              |   |                         |    |                        |    |
| 2.2 Course coordinator               | Lect. dr. George Țurcaș                            |              |   |                         |    |                        |    |
| 2.3 Seminar coordinator              | Lect. dr. George Țurcaș                            |              |   |                         |    |                        |    |
| 2.4. Year of study                   | II   | 2.5 Semester | 4 | 2.6. Type of evaluation | VP | 2.7 Type of discipline | DS |
| 2.8 Code of the discipline           | MLE0041  |              |   |                         |    |                        |    |

### 3. Total estimated time (hours/semester of didactic activities)

|   |     |                      |    |                        |       |
|---|-----|----------------------|----|------------------------|-------|
| 3.1 Hours per week  | 4   | Of which: 3.2 course | 2  | 3.3 seminar/laboratory | 2     |
| 3.4 Total hours in the curriculum   | 56  | Of which: 3.5 course | 28 | 3.6 seminar/laboratory | 28    |
| Time allotment:   |     |                      |    |                        | hours |
| Learning using manual, course support, bibliography, course notes                     |     |                      |    |                        | 20    |
| Additional documentation (in libraries, on electronic platforms, field documentation) |     |                      |    |                        | 20    |
| Preparation for seminars/labs, homework, papers, portfolios and essays                |     |                      |    |                        | 20    |
| Tutorials   |     |                      |    |                        | 14    |
| Evaluations   |     |                      |    |                        | 10    |
| Other activities: homework  |     |                      |    |                        | 10    |
| 3.7 Total individual study hours  | 94  |                      |    |                        |       |
| 3.8 Total hours per semester  | 150 |                      |    |                        |       |
| 3.9 Number of ECTS credits  | 6   |                      |    |                        |       |

### 4. Prerequisites (if necessary)

|                   |                  |
|-------------------|------------------|
| 4.1. curriculum   | • None necessary |
| 4.2. competencies | •                |

### 5. Conditions (if necessary)

|                      |   |
|----------------------|---|
| 5.1. for the course  | •   |
| 5.2. for the seminar | • Attendance to at least 75% of the seminars. |

### 6. Specific competencies acquired

|                                  |   |
|----------------------------------|---|
| <b>Professional competencies</b> | <ul style="list-style-type: none"> <li>• The ability to identify concepts, theories and use of specific description language</li> <li>• The ability to produce a mathematical model for a certain problem.</li> <li>• Developing independent learning skills and teamwork for realising projects and solving complex problems.</li> </ul> |
| <b>Transversal competencies</b>  | <ul style="list-style-type: none"> <li>• Applying rigorous and efficient work rules, displaying a responsible attitude towards the scientific and educational and creative order to maximize their potential in specific situations with respect to the basic principles and norms of professional ethics</li> </ul>                      |

## 7. Objectives of the discipline (outcome of the acquired competencies)

|  |   |
|--|---|
| 7.1 General objective of the discipline  | <ul style="list-style-type: none"> <li>• Acquiring theoretical and practical knowledge necessary for understanding the principles and methods of plane geometry.</li> <li>• Developing creative thinking and spatial orientation.</li> <li>• Developing teaching skills.</li> </ul>   |
| 7.2 Specific objective of the discipline | <p>At the end of the course, the students should be able to</p> <ul style="list-style-type: none"> <li>• Correctly identify planar geometric figures and the connections between them.</li> <li>• Combine several results and theorems such as Menelaus' or Ceva's to prove different results.</li> <li>• Use geometric transformations such as homothety and inversion to solve problems in geometry.</li> </ul> |

## 8. Content

| 8.1 Course   | Teaching methods   | Remarks |
|--|--|---------|
| 1. Menelaus' theorem and applications (1 lecture)                                  | Lecture, description, exemplifications by using multimedia tools |         |
| 2. Ceva's theorem and applications (1 lecture)                                     | Lecture, description, exemplifications by using multimedia tools |         |
| 3. Metric problems in the triangle. Cosine theorem, Stewarts' theorem (2 lectures) | Lecture, description, exemplifications by using multimedia tools |         |
| 4. Angle chasing. Cyclic quadrilaterals (2 lecture)                                | Lecture, description, exemplifications by using multimedia tools |         |
| 5. The power of a point with respect to a circle (1 lecture)                       | Lecture, description, exemplifications by using multimedia tools |         |
| 6. The radical axis of two circles (1 lecture)                                     | Lecture, description, exemplifications by                        |         |

|  |  |  |
|--|--|--|
|  | using multimedia tools   |  |
| 7. Isometries and affine transformations in the plane (2 lectures) | Lecture, description, exemplifications by using multimedia tools |  |
| 8. Homothety (1 lecture)   | Lecture, description, exemplifications by using multimedia tools |  |
| 9. Spiral similarity (1 lecture)                                   | Lecture, description, exemplifications by using multimedia tools |  |
| 10. Inversion (1 lecture)  | Lecture, description, exemplifications by using multimedia tools |  |

#### Bibliography

1. D. Andrica – Geometrie. Teme pentru perfectionarea profesorilor de matematică, Casa cărții de știință, Cluj-Napoca, 2017
2. D. Andrica, Cs. Varga, D. Văcărețu, Teme și probleme alese de geometrie, Ed. Plus, București, 2002.
3. T. Andreescu, M. Rolinek, J. Tkadlec, 106 Problems from the AwesomeMath Summer Program, XYZ Press, 2013.
4. T. Andreescu, M. Rolinek, J. Tkadlec, 107 Problems from the AwesomeMath Summer Program, XYZ Press, 2014.
5. M. Berger - Geometry (vol. I and II), Springer, 1987
6. P.A. Blaga – Geometrie și grafica I (lecture notes available on the author website)
7. C. Mihailescu – The Geometry of Remarkable Elements: Points, Lines and Circles, XYZ Press 2016.

| 8.2 Seminar / laboratory   | Teaching methods  | Remarks |
|--|---|---------|
| 1. Problems using Menelaus Theorem (1 seminar)   | Description, explanation, independent and/or team study |         |
| 2. Problems using Ceva's theorem (1 seminar)   | Description, explanation, independent and/or team study |         |
| 3. Applications of cosine theorem, Stewart's theorem and various problems involving metric computations in a triangle (2 seminars) | Description, explanation, independent and/or team study |         |
| 4. Problems with angle chasing and cyclic quadrilaterals (2 seminars)  | Description, explanation, independent and/or team study |         |
| 5. Problems using the power of a and the concept of radical axis (2 seminars)  | Description, explanation,                               |         |

|  |   |  |
|--|---|--|
|  | independent and/or team study                           |  |
| 6. Problems using affine transformations (2 seminars)  | Description, explanation, independent and/or team study |  |
| 7. Problems using homothety (1 seminar)  | Description, explanation, independent and/or team study |  |
| 8. Problems using spiral similarity (1 seminar)  | Description, explanation, independent and/or team study |  |
| 9. Problems using homothety (1 seminar)  | Description, explanation, independent and/or team study |  |
| 10. Problems using inversion (1 seminar)   | Description, explanation, independent and/or team study |  |
| Bibliography<br>1. D. Andrica – Geometrie. Teme pentru perfectionarea profesorilor de matematică, Casa cărții de știință, Cluj-Napoca, 2017<br>2. D. Andrica, Cs. Varga, D. Văcărețu, Teme și probleme alese de geometrie, Ed. Plus, București, 2002.<br>3. T. Andreescu, M. Rolinek, J. Tkadlec, 106 Problems from the AwesomeMath Summer Program, XYZ Press, 2013.<br>4. T. Andreescu, M. Rolinek, J. Tkadlec, 107 Problems from the AwesomeMath Summer Program, XYZ Press, 2014.<br>5. M. Berger - Geometry (vol. I and II), Springer, 1987<br>6. P.A. Blaga – Geometrie si grafica I (lecture notes available on the author website)<br>7. C. Mihailescu – The Geometry of Remarkable Elements: Points, Lines and Circles, XYZ Press 2016. |   |  |

**9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program**

|  |
|--|
| <ul style="list-style-type: none"> <li>The notions assimilated are essential for any prospective mathematician or math teacher. Moreover, these competencies are very useful in activities related to computer graphics, computer aided geometric design or machine learning.</li> </ul> |
|--|

**10. Evaluation**

| Type of activity | 10.1 Evaluation criteria  | 10.2 Evaluation methods | 10.3 Share in the grade (%) |
|------------------|---|-------------------------|-----------------------------|
| 10.4 Course      | Critical grasp of the learned material, ability to use what was learned | Test in week 5          | 25%                         |

|   |  |                                       |     |
|---|--|---------------------------------------|-----|
|   | Critical grasp of the learned material, ability to use what was learned  | Test in the last week of the semester | 50% |
| 10.5 Seminar/lab activities   | Active participation at the seminars, ability to use the methods learned | Discussions in the seminars           |     |
|   |  | Homework                              | 25% |
| 10.6 Minimum performance standards  |  |                                       |     |
| <ul style="list-style-type: none"> <li>➤ The student should attend at least 75% of the seminars.</li> <li>➤ The grade of the written test at the end of the semester should be at least 5 and the weighted average of all grades should be at least 5.</li> </ul> |  |                                       |     |

Date  
April 29, 2022

Signature of course coordinator  
Lect. dr. George Țurcaș



Signature of seminar coordinator  
Lect. dr. George Țurcaș



Date of approval  
April 29, 2022

Signature of the head of department  
Prof. dr. Octavian Agratini