

## SYLLABUS

### 1. Information regarding the programme

1.1 Higher education institution	Babeş-Bolyai University
1.2 Faculty	Faculty of Mathematics and Computer Science
1.3 Department	Department of Mathematics
1.4 Field of study	Mathematics
1.5 Study cycle	Bachelor
1.6 Study programme / Qualification	Computer Science

### 2. Information regarding the discipline

2.1 Name of the discipline	Geometry						
2.2 Course coordinator	Lect. Dr. Iulian Simion						
2.3 Seminar coordinator	Lect. Dr. Iulian Simion						
2.4 Year of study	1	2.5 Semester	2	2.6. Type of evaluation	VP	2.7 Type of discipline	Compulsory
2.8 Disciplinei code	MLE0014						

### 3. Total estimated time (hours/semester of didactic activities)

3.1 Hours per week	4	Of which: 3.2 course	2	3.3 seminar	2
3.4 Total hours in the curriculum	56	Of which: 3.5 course	28	3.6 seminar	28
Time allotment:					hours
Learning using manual, course support, bibliography, course notes					20
Additional documentation (in libraries, on electronic platforms, field documentation)					10
Preparation for seminars/labs, homework, papers, portfolios and essays					14
Tutorship					14
Evaluations					11
Other activities: .....					-
3.7 Total individual study hours					69
3.8 Total hours per semester					125
3.9 Number of ECTS credits					5

### 4. Prerequisites (if necessary)

4.1 curriculum	<ul style="list-style-type: none"> <li>Basic knowledge in algebra and calculus.</li> </ul>
4.2 competencies	<ul style="list-style-type: none"> <li>Competencies of using the above mentioned curricula.</li> </ul>

### 5. Conditions (if necessary)

5.1 for the course	
5.2 for the seminar /lab activities	

## 6. Specific competencies acquired

<b>Professional competencies</b>	<ul style="list-style-type: none"> <li>• C1.1 Identifying the notions, describing the theories and using the specific language</li> <li>• C2.3 Applying the adequate analytical theoretical methods to a given problem</li> </ul>
<b>Transversal competencies</b>	CT1. Applying some rules of precise and efficient work, showing a responsible attitude regarding the the scientific domain and teaching training for an optimal and creative development of the personal potential in specific situations, respecting the deontological norms.

## 7. Objectives of the discipline (outcome of the acquired competencies)

7.1 General objective of the discipline	Basic notions and methods in the context of analytic geometry
7.2 Specific objective of the discipline	Classification of quadratic curves and surfaces

## 8. Content

8.1 Course	Teaching methods	Remarks
1. Geometric vectors <ul style="list-style-type: none"> <li>• Vector space structure</li> <li>• Cartesian coordinate frames</li> </ul>	Exposition, proofs, examples	
2-3. Scalar product and vector product <ul style="list-style-type: none"> <li>• Orthonormal frames</li> <li>• Box product</li> <li>• Classical identities</li> </ul>	Exposition, proofs, examples	Two lectures
4-5. Lines in dimension 2 <ul style="list-style-type: none"> <li>• Different equations for a line</li> <li>• Normal vectors</li> <li>• Relative positions of lines</li> <li>• Pencils of lines</li> </ul> Planes in dimension 3 <ul style="list-style-type: none"> <li>• Different equations for a plane</li> <li>• Normal vectors</li> </ul> Lines in dimension 3 <ul style="list-style-type: none"> <li>• Different equations for a line</li> </ul>	Exposition, proofs, examples	Two lectures

<ul style="list-style-type: none"> <li>Relative positions of lines and planes</li> </ul>		
6. Affine maps <ul style="list-style-type: none"> <li>Changing coordinates</li> <li>Parallel projections and reflections</li> </ul>	Exposition, proofs, examples	
7. Isometries <ul style="list-style-type: none"> <li>Rotations in dimension 2 and 3</li> <li>Spectral theorem</li> </ul>	Exposition, proofs, examples	
8-9. Quadratic curves <ul style="list-style-type: none"> <li>Ellipse, hyperbola, parabola</li> <li>Canonical equations</li> <li>Relative position of a line</li> <li>Tangent lines</li> </ul>	Exposition, proofs, examples	Two lectures
10. Classification of quadrics (dimension 2 and 3) <ul style="list-style-type: none"> <li>Reducing to canonical form</li> <li>Isometric classification of quadrics</li> <li>Affine classification of quadrics</li> </ul>	Exposition, proofs, examples	
11-12. Quadratic surfaces <ul style="list-style-type: none"> <li>Ellipsoid, Cone, Hyperboloid, Paraboloid</li> <li>Canonical equation</li> <li>Tangent planes</li> </ul>	Exposition, proofs, examples	Two lectures
13-14. Quaternions <ul style="list-style-type: none"> <li>Algebraic description</li> <li>Quaternions and rotations</li> </ul>	Exposition, proofs, examples	Two lectures
<b>Bibliography</b> [1] I. Simion, Geometry – material de curs, 2021. [2] P.A. Blaga, Geometrie – material de curs, 2019. [3] M. Troyanov, Cours de géométrie, Lausanne, 2011. [4] E. Sernesi, Linear Algebra. A geometric Approach (Translated by J. Montaldi), 2009.		
8.2 Seminar	Teaching methods	Remarks
1. Geometric vectors <ul style="list-style-type: none"> <li>Vector space structure</li> <li>Cartesian coordinate frames</li> </ul>	Dialog, problem solving	
2-3. Scalar product and vector product <ul style="list-style-type: none"> <li>Orthonormal frames</li> <li>Box product</li> <li>Classical identities</li> </ul>	Dialog, problem solving	Two tutorials
4-5. Lines in dimension 2 <ul style="list-style-type: none"> <li>Different equations for a line</li> <li>Normal vectors</li> <li>Relative positions of lines</li> <li>Pencils of lines</li> </ul> Planes in dimension 3 <ul style="list-style-type: none"> <li>Different equations for a plane</li> <li>Normal vectors</li> </ul>	Dialog, problem solving	Two tutorials

Lines in dimension 3		
<ul style="list-style-type: none"> <li>• Different equations for a line</li> <li>• Relative positions of lines and planes</li> </ul>		
6. Affine maps	Dialog, problem solving	
<ul style="list-style-type: none"> <li>• Changing coordinates</li> <li>• Parallel projections and reflections</li> </ul>		
7. Isometries	Dialog, problem solving	
<ul style="list-style-type: none"> <li>• Rotations in dimension 2 and 3</li> <li>• Spectral theorem</li> </ul>		
8-9. Quadratic curves	Dialog, problem solving	Two tutorials
<ul style="list-style-type: none"> <li>• Ellipse, hyperbola, parabola</li> <li>• Canonical equations</li> <li>• Relative position of a line</li> <li>• Tangent lines</li> </ul>		
10. Classification of quadrics (dimension 2 and 3)	Dialog, problem solving	
<ul style="list-style-type: none"> <li>• Reducing to canonical form</li> <li>• Isometric classification of quadrics</li> <li>• Affine classification of quadrics</li> </ul>		
11-12. Quadratic surfaces	Dialog, problem solving	Two tutorials
<ul style="list-style-type: none"> <li>• Ellipsoid, Cone, Hyperboloid, Paraboloid</li> <li>• Canonical equation</li> <li>• Tangent planes</li> </ul>		
13-14. Quaternions	Dialog, problem solving	Two tutorials
<ul style="list-style-type: none"> <li>• Algebraic description</li> <li>• Quaternions and rotations</li> </ul>		

#### Bibliography

[1] I. Simion, Geometry – material de curs, 2021.

[2] P.A. Blaga, Geometrie – material de curs, 2019.

[3] M. Troyanov, Cours de géométrie, Lausanne, 2011.

[4] E. Sernesi, Linear Algebra. A geometric Approach (Translated by J. Montaldi), 2009.

### **9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program**

- The material of this course serves other courses
  - a deeper understanding of linear algebra
  - affine transformations are necessary examples for a group theory course
  - quadrics are necessary examples in analysis courses
  - coordinate changes, projections, affine transformations are necessary for computer graphics
- Applications of the theory are presented wherever appropriate

### **10. Evaluation**

Type of activity	10.1 Evaluation criteria	10.2 Evaluation methods	10.3 Share in the grade (%)
10.4 Course	Critical grasp of the learned material, ability to	Two written partial exams at the middle and at the end	each 50%

	use what was learned	of the semester	
10.5 Seminar	Ability to use the theory for solving problems	Points during the tutorial for active participation	Can lead up to one extra point for the final grade
10.6 Minimum performance standards			
At least grade 5 for the final grade.			

Date

12. February 2022

Signature of course coordinator

Lect. Dr. Iulian Simion

Signature of seminar coordinator

Lect. Dr. Iulian Simion

Date of approval

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Signature of the head of department

Prof. Dr. Octavian Agratini