

## SYLLABUS

### 1. Information regarding the programme

|                                     |   |
|-------------------------------------|---|
| 1.1 Higher education institution    | <b>Babeş-Bolyai University</b>                          |
| 1.2 Faculty                         | <b>Faculty of Mathematics and Computer Science</b>      |
| 1.3 Department                      | <b>Department of Mathematics</b>                        |
| 1.4 Field of study                  | <b>Computer Science</b>                                 |
| 1.5 Study cycle                     | <b>Master</b>   |
| 1.6 Study programme / Qualification | <b>High Performance Computing and Big Data Analysis</b> |

### 2. Information regarding the discipline

|                            |          |  |          |                         |          |                        |                 |
|----------------------------|----------|--|----------|-------------------------|----------|------------------------|-----------------|
| 2.1 Name of the discipline |          | <b>Statistical Computational Methods</b>     |          |                         |          |                        |                 |
| 2.2 Course coordinator     |          | <b>Assoc. Prof. PhD. Habil. Sanda Micula</b> |          |                         |          |                        |                 |
| 2.3 Seminar coordinator    |          | <b>Assoc. Prof. PhD. Habil. Sanda Micula</b> |          |                         |          |                        |                 |
| 2.4. Year of study         | <b>2</b> | 2.5 Semester                                 | <b>3</b> | 2.6. Type of evaluation | <b>E</b> | 2.7 Type of discipline | <b>Optional</b> |
| 2.8 Course Code            | MME8088  |  |          |                         |          |                        |                 |

### 3. Total estimated time (hours/semester of didactic activities)

|   |    |                      |     |                        |       |
|---|----|----------------------|-----|------------------------|-------|
| 3.1 Hours per week  | 3  | Of which: 3.2 course | 2   | 3.3 seminar/laboratory | 1     |
| 3.4 Total hours in the curriculum   | 42 | Of which: 3.5 course | 28  | 3.6 seminar/laboratory | 14    |
| Time allotment:   |    |                      |     |                        | hours |
| Learning using manual, course support, bibliography, course notes                     |    |                      |     |                        | 41    |
| Additional documentation (in libraries, on electronic platforms, field documentation) |    |                      |     |                        | 15    |
| Preparation for seminars/labs, homework, papers, portfolios and essays                |    |                      |     |                        | 35    |
| Tutorship   |    |                      |     |                        | 19    |
| Evaluations   |    |                      |     |                        | 23    |
| Other activities: .....   |    |                      |     |                        | -     |
| 3.7 Total individual study hours  |    |                      | 133 |                        |       |
| 3.8 Total hours per semester  |    |                      | 175 |                        |       |
| 3.9 Number of ECTS credits  |    |                      | 7   |                        |       |

### 4. Prerequisites (if necessary)

|                   |  |
|-------------------|--|
| 4.1. curriculum   | <ul style="list-style-type: none"> <li>• Probability and Statistics</li> </ul>                                     |
| 4.2. competencies | <ul style="list-style-type: none"> <li>• Logical thinking</li> <li>• Average logical programming skills</li> </ul> |

### 5. Conditions (if necessary)

|                           |  |
|---------------------------|--|
| 5.1. for the course       | <ul style="list-style-type: none"> <li>• Lecture room with large blackboard and video projector, laptop, beamer</li> </ul> |
| 5.2. for the seminar /lab | <ul style="list-style-type: none"> <li>• For seminar: Laboratory with computers having Matlab installed</li> </ul>         |

## 6. Specific competencies acquired

|                                  |   |
|----------------------------------|---|
| <b>Professional competencies</b> | C4.3 Identifying the appropriate models and methods for solving real-life problems<br>C4.4 Using simulations in order to study and elaborate models and evaluate their performance  |
| <b>Transversal competencies</b>  | CT1 Ability to conform to the requirements of organized and efficient work, to develop a responsible approach towards the academic and scientific fields, in order to make the most of one's own creative potential, while obeying the rules and principles of professional ethic<br><br>CT3 Using efficient methods and techniques for learning, information, research and developing capabilities for using knowledge, for adapting to a dynamic society and for communicating in Romanian and in a worldwide spoken language |

## 7. Objectives of the discipline (outcome of the acquired competencies)

|  |   |
|--|---|
| 7.1 General objective of the discipline  | <ul style="list-style-type: none"> <li>Acquire basic knowledge of Probability Theory and Mathematical Statistics applications and models</li> </ul>   |
| 7.2 Specific objective of the discipline | <ul style="list-style-type: none"> <li>Ability to use Monte Carlo methods and simulations for solving real-life problems and perform statistical analysis of data</li> <li>Become familiar and be able to work with various probabilistic and statistical models</li> <li>Ability to use statistical features of various mathematical software</li> </ul> |

## 8. Content

| 8.1 Course   | Teaching methods  | Remarks |
|--|---|---------|
| 1. <b>Review of Probability and Statistics.</b> Probability space. Rules of probability. Conditional probability. Probabilistic models. Random variables and random vectors. | <ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul> |         |
| 2. Common discrete and continuous distributions. PDF and CDF. Examples, applications, properties.  | <ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul> |         |
| 3. Random samples. Sample functions. Estimators. Confidence intervals. Hypothesis and significance testing.  | <ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> </ul>                                   |         |
| 4. <b>Computer simulations and Monte Carlo methods.</b> MC methods and random number generators. Discrete methods. Examples.   | <ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Description</li> </ul>              |         |
| 5. Inverse transform and discrete inverse transform method. Rejection method. Special methods. Examples.   | <ul style="list-style-type: none"> <li>Interactive exposure</li> <li>Explanation</li> <li>Conversation</li> <li>Didactical demonstration</li> </ul> |         |

|  |   |  |
|--|---|--|
| 6. Accuracy of an MC study. Estimating probabilities, means, variances. Size of an MC study. Other applications of MC methods.                         | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul> |  |
| 7. <b>Stochastic processes.</b> Definitions, classifications. Markov processes and Markov chains. Transition probability matrix. Properties, examples. | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Description</li> </ul>              |  |
| 8. Steady-state distribution. Regular Markov chains. Periodic Markov chains. Simulation of Markov chains.  | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul> |  |
| 9. Counting processes. Binomial and Poisson counting processes. Gamma-Poisson formula. Simulation of counting processes. Examples.                     | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul> |  |
| 10. <b>Queuing systems.</b> Basic notions, main components, Little's law. Bernoulli single-server QS. Systems with limited capacity.                   | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> </ul>                                     |  |
| 11. M/M/1 QS. Evaluation of a system's performance. Examples.  | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul> |  |
| 12. Multiserver QS's. Bernoulli k-server and M/M/k QS's. M/M/∞ QS's. Simulation of QS's.   | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> </ul>                                     |  |
| 13. <b>Statistical inference.</b> Nonparametric tests, Chi-square-tests, Wilcoxon tests. Bootstrapping. Applications, examples, simulations.           | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Description</li> </ul>              |  |
| 14. Regression and correlation. Fitting models. Analysis of variance (ANOVA), prediction. Examples.  | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Didactical demonstration</li> </ul> |  |

#### Bibliography

1. Micula, S., Probability and Statistics for Computational Sciences, Cluj University Press, 2009.
2. Baron, M., Probability and Statistics for Computer Scientists, CRC Press, Taylor and Francis, Boca Raton, FL, 2014.
3. Milton, J.S., Arnold, J. C., Introduction to Probability and Statistics: Principles and Applications for Engineering and the Computing Sciences, 3rd Edition. McGraw-Hill, New York, 1995.
4. Gentle, J. E., Elements of Computational Statistics, Springer-Verlag, New York, 2002.
5. Matloff, N., From Algorithms to Z-Scores: Probabilistic and Statistical Modelling in Computer Science, Orange Grove Texts Plus, Gainesville, FL, 2009.
6. Gentle, J. E., Hardle, W., Mori, Y., Handbook of Computational Statistics, Springer, Heidelberg, 2004.

| 8.2 Seminar /Laboratory   | Teaching methods  | Remarks   |
|---|---|---|
| 1. Random variables and applications.                                   | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> </ul> | The seminar is structured as 2 hours per week, every other week |
| 2. Computer simulations of discrete random variables. Discrete methods. | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> </ul>                         |   |

|   |   |  |
|---|---|--|
|   | <ul style="list-style-type: none"> <li>• Conversation</li> <li>• Individual and group work</li> </ul>   |  |
| 3. Computer simulations of random variables and Monte Carlo studies. Inverse transform method, rejection method, special methods.   | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Conversation</li> <li>• Synthesis</li> <li>• Individual and group work</li> </ul>                          |  |
| 4. Markov chains. Applications and simulations.   | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>                        |  |
| 5. Counting processes. Bernoulli and Poisson counting processes. Applications and simulations.  | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>                        |  |
| 6. Queuing systems. Examples and simulations.   | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Individual and group work</li> </ul>                        |  |
| 7. Statistical inference. Applications and simulations.   | <ul style="list-style-type: none"> <li>• Interactive exposure</li> <li>• Explanation</li> <li>• Conversation</li> <li>• Description</li> <li>• Individual and group work</li> </ul> |  |
| <b>Bibliography</b> <ol style="list-style-type: none"> <li>1. Baron, M., Probability and Statistics for Computer Scientists, CRC Press, Taylor and Francis, Boca Raton, FL, 2014.</li> <li>2. Blaga, P., Statistica prin Matlab, Presa Universitara Clujeana, Cluj-Napoca, 2002.</li> <li>3. Lisei, H., Micula, S., Soos, A., Probability Theory through Problems and Applications, Cluj University Press, 2006.</li> <li>4. Milton, J.S., Arnold, J. C., Introduction to Probability and Statistics: Principles and Applications for Engineering and the Computing Sciences, 3rd Edition. McGraw-Hill, New York, 1995.</li> <li>5. Gentle, J. E., Elements of Computational Statistics, Springer-Verlag, New York, 2002.</li> <li>6. Matloff, N., From Algorithms to Z-Scores: Probabilistic and Statistical Modelling in Computer Science, Orange Grove Texts Plus, Gainesville, FL, 2009.</li> </ol> |   |  |

**9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program**

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|---|
| <ul style="list-style-type: none"> <li>• The course gives students solid statistical background for computational intelligence.</li> <li>• The knowledge and skills acquired in this course give students a foundation for launching a career in scientific research.</li> <li>• The statistical analysis abilities acquired in this course are useful in any career path students may choose.</li> </ul> |
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**10. Evaluation**

| Type of activity   | 10.1 Evaluation criteria  | 10.2 Evaluation methods  | 10.3 Share in the grade (%) |
|--|---|--|-----------------------------|
| 10.4 Course  | - acquire the basic principles in Computational Statistics, with emphasis on simulations and Monte Carlo studies;<br>- be able to apply correctly the course concepts on various applications and problem solving | <b>Written exam</b> on problems only (a sheet with the main formulas is available)   | 60%                         |
| 10.5 Seminar/Lab activities  | - be able to apply course concepts and techniques on practical problems<br>- be able to implement course concepts and algorithms in Matlab<br>- be able to solve numerical statistical problems in Matlab         | - participation in discussing, solving and implementing problems throughout the semester<br>- individual presentation of solutions<br>- <b>lab exam</b> (numerical statistical applications and simulations) | 40%                         |
| 10.7 Minimum performance standards   |   |  |                             |
| ➤ A grade of 5 or above (on a scale from 1 to 10) on <b>each</b> activity mentioned above (written test, seminar/lab evaluation) |   |  |                             |

Date

Signature of course coordinator

Signature of seminar coordinator

11.04.2021

Assoc. Prof. PhD. Habil. Sanda Micula

Assoc. Prof. PhD. Habil. Sanda Micula

Date of approval

Signature of the head of department

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