

SYLLABUS

1. Information regarding the programme

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| 1.1 Higher education institution | Babeş-Bolyai University |
| 1.2 Faculty | Mathematics and Computer Science |
| 1.3 Department | Mathematics |
| 1.4 Field of study | Mathematics |
| 1.5 Study cycle | Bachelor |
| 1.6 Study programme / Qualification | Mathematics - Computer Science |

2. Information regarding the discipline

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| 2.1 Name of the discipline | Partial Differential Equations | | | | | | |
| 2.2 Course coordinator | Prof. Dr. Radu Precup | | | | | | |
| 2.3 Seminar coordinator | Prof. Dr. Radu Precup | | | | | | |
| 2.4. Year of study | 3 | 2.5 Semester | 5 | 2.6. Type of evaluation | Exam | 2.7 Type of discipline | Compulsory |

3. Total estimated time (hours/semester of didactic activities)

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| 3.1 Hours per week | 4 | Of which: 3.2 course | 2 | 3.3 seminar/laboratory | 2 | |
| 3.4 Total hours in the curriculum | 56 | Of which: 3.5 course | 28 | 3.6 seminar/laboratory | 28 | |
| Time allotment: | | | | | | hours |
| Learning using manual, course support, bibliography, course notes | | | | | | 10 |
| Additional documentation (in libraries, on electronic platforms, field documentation) | | | | | | 6 |
| Preparation for seminars/labs, homework, papers, portfolios and essays | | | | | | 10 |
| Tutorship | | | | | | 4 |
| Evaluations | | | | | | 14 |
| Other activities: | | | | | | |
| 3.7 Total individual study hours | | | | | | 44 |
| 3.8 Total hours per semester | | | | | | 100 |
| 3.9 Number of ECTS credits | | | | | | 4 |

4. Prerequisites (if necessary)

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| 4.1. curriculum | <ul style="list-style-type: none"> • Ordinary differential equations; Measure theory |
| 4.2. competencies | <ul style="list-style-type: none"> • |

5. Conditions (if necessary)

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| 5.1. for the course | <ul style="list-style-type: none"> • |
| 5.2. for the seminar /lab activities | <ul style="list-style-type: none"> • |

6. Specific competencies acquired

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| Professional competencies | <ul style="list-style-type: none"> • Basic theory of linear second-order partial differential equations • Capacity to frame physical models in one of the following classes of PDEs: elliptic, parabolic, and hyperbolic. |
| Transversal competencies | <p>CT3 Utilizarea unor metode și tehnici eficiente de învățare, informare, cercetare și dezvoltare a capacităților de valorificare a cunoștințelor, de adaptare la cerințele unei societăți dinamice și de comunicare în limba română și într-o limbă de circulație internațională</p> |

7. Objectives of the discipline (outcome of the acquired competencies)

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| 7.1 General objective of the discipline | <ul style="list-style-type: none"> • Basic theory of linear second-order partial differential equations |
| 7.2 Specific objective of the discipline | <ul style="list-style-type: none"> • Properties of harmonic functions. • The notion of weak solution. • Fourier series method for solving boundary value problems. • Fourier transform method. |

8. Content

| 8.1 Course | Teaching methods | Remarks |
|---|---|---------|
| 1. Preliminaries. Classifications. Particular equations. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 2. Mathematical models expressed by partial differential equations | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 3. Green's formula. The fundamental solution of the Laplace equation. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 4. Mean value theorems for harmonic functions | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 5. The maximum principle. Uniqueness and continuous dependence on data for the Dirichlet problem. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |

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| 6. Green's functions of the Dirichlet problem. Poisson's formula. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 7. Dirichlet's principle. The generalized solution of the Dirichlet problem. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 8. Fourier Series. The eigenvalues and eigenfunctions of the Dirichlet problem. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 9. The maximum principle for the heat equation. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 10. The Cauchy-Dirichlet problem for the heat equation. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 11. The Cauchy-Dirichlet problem for the wave equation. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 12. The Cauchy problem for evolution equations. The Fourier transform. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 13. The Cauchy problem for the heat equation. | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| 14. Nonhomogeneous equations: Duhamel's principle | <ul style="list-style-type: none"> • Interactive exposure • Explanation • Conversation • Didactical demonstration | |
| Bibliography | | |
| <ol style="list-style-type: none"> 1. R. Precup, Lectii de ecuatii cu derivate partiale, Presa Universitara Clujeana, 2004. 2. R. Precup, Linear and Semilinear Partial Differential Equations, De Gruyter, Berlin, 2012. 3. L.C. Evans, Partial Differential Equations, Amer. Math. Soc., Providence, 1998. | | |
| 8.2 Seminar / laboratory | Teaching methods | Remarks |
| 1. The canonical form of linear second-order PDEs. | Exercise, explanation, dialogue, team work | |

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| 2. The method of separation of variables: cases of rectangular and circular domains. | Exercise, explanation, dialogue, team work | |
| 3. Properties of the harmonic functions. Exercises. | Exercise, explanation, dialogue, team work | |
| 4. Mean value theorems. Exercises. | Exercise, explanation, dialogue, team work | |
| 5. The maximum principle. Applications. | Exercise, explanation, dialogue, team work | |
| 6. Green's function for particular domains. | Exercise, explanation, dialogue, team work | |
| 7. Dirichlet's principle. Generalized solutions. Examples. | Exercise, explanation, dialogue, team work | |
| 8. Elliptic equations in the divergence form. | Exercise, explanation, dialogue, team work | |
| 9. The generalized solution of Neumann's problem. | Exercise, explanation, dialogue, team work | |
| 10. The eigenvalues and eigenfunctions for particular domains. | Exercise, explanation, dialogue, team work | |
| 11. Mixed problems for the heat equation. | Exercise, explanation, dialogue, team work | |
| 12. Mixed problems for the wave equation. | Exercise, explanation, dialogue, team work | |
| 13. The Fourier transform. Examples. | Exercise, explanation, dialogue, team work | |
| 14. The Cauchy problem for the heat equation. Particular cases. | Exercise, explanation, dialogue, team work | |
| Bibliography <ol style="list-style-type: none"> 1. R. Precup, Lectii de ecuatii cu derivate partiale, Presa Universitara Clujeana, 2004. 2. R. Precup, Linear and Semilinear Partial Differential Equations, De Gruyter, Berlin, 2012. 3. L.C. Evans, Partial Differential Equations, Amer. Math. Soc., Providence, 1998. 4. V.S. Vladimirov s.a., Culegere de probleme de ecuatiile fizicii matematice, Ed. St. Encicl., Bucuresti, 1981. | | |

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

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10. Evaluation

| Type of activity | 10.1 Evaluation criteria | 10.2 Evaluation methods | 10.3 Share in the grade (%) |
|--|--------------------------|-------------------------|-----------------------------|
| 10.4 Course | | Continuous observations | 10% |
| | | Written exam | 50% |
| 10.5 Seminar/lab activities | | Continuous observations | 10% |
| | | Practical examination | 30% |
| 10.6 Minimum performance standards | | | |
| <ul style="list-style-type: none">• Method of separation of variables.• Properties of the harmonic functions (mean value theorem; maximum principle).• Solving of mixed problems for evolution equations.• Fourier transform. | | | |

Date

29 Aprilie 2020

Signature of course coordinator

..Radu Precup

Signature of seminar coordinator

Radu Precup.....

Date of approval

4 Mai 2020

Signature of the head of department

Octavian Agratini.....