SYLLABUS

1. Information regarding the programme

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ty of Mathematics and Computer Science
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nced Mathematics

2. Information regarding the discipline

2.1 Name of the dis	of the discipline Vector Optimization			Vector Optimization			
2.2 Course coordinator		Prof. Nicolae Popovici, PhD. habil.					
2.3 Seminar coordi	nato	or	Prof. Nicolae Popovici, PhD. habil.				
2.4. Year of study	2	2.5 Semester	3 2.6. Type of VP 2.7 Type of Optional				Optional
			evaluation discipline				

3. Total estimated time (hours/semester of didactic activities)

3.1 Hours per week	3	Of which: 3.2 course	2	3.3 seminar	1
3.4 Total hours in the curriculum	42	Of which: 3.5 course	28	3.6 seminar	14
Time allotment:					hours
Learning using manual, course suppor	t, bił	oliography, course notes	5		28
Additional documentation (in libraries	s, on	electronic platforms, fie	eld do	cumentation)	28
Preparation for seminars/labs, homework, papers, portfolios and essays					
Tutorship					
Evaluations					
Other activities:					-
3.7 Total individual study hours 133					
3.8 Total hours per semester		175			
3.9 Number of ECTS credits		7			

4. Prerequisites (if necessary)

4.1. curriculum	• Mathematical analysis 1 (Analysis on R);		
	• Mathematical analysis 2 (Differential Calculus on R ⁿ).		
4.2. competencies	Ability to use abstract notions, theoretical results and practical		
	methods of Mathematical Analysis.		

5. Conditions (if necessary)

5.1. for the course	Lecture room equipped with a beamer
5.2. for the seminar /lab	Standard room
activities	

6. Specific competencies acquired

Professional competencies	Ability to use appropriate mathematical methods and implementable algorithms for solving practical vector optimization problems.
Transversal competencies	To apply rigorous and efficient work rules, by adopting a responsible attitude towards the scientific and didactic activities. To develop the own creative potential in specific areas, following the professional ethical norms and principles.

7. Objectives of the discipline (outcome of the acquired competencies)

7.1 General objective of the	Students should acquire knowledge about vector (multicriteria) optimization.
discipline	
7.2 Specific objective of the	Students will study several classes of practical vector optimization problems.
discipline	

8. Content

8.1 Course	Teaching methods	Remarks
1. Preorder relations; maximal elements of a set with	Direct instruction,	
respect to a preference relation; formulation of general	mathematical proof,	
optimization problems. Linear prorder relations	exemplification	
(compatible with the vector addition and		
multiplication of vectors by scalars).		
2. Cones; characterizations of (convex, pointed,	Direct instruction,	
generating, totally-generating) cones; the relationship	mathematical proof,	
between linear preorder relations and convex cones.	exemplification	
Topological properties of convex cones: (relative)		
solid and closed convex cones; the polar cone of a set;		
polyhedral cones.		
3. Concepts of efficiency in vector optimization;	Direct instruction,	
efficient points and weakly efficient points w.r.t. a	mathematical proof,	
convex cone; efficient solutions and weakly efficient	exemplification	
solutions of vector optimization problems.		
4. Monotone and strictly monotone scalar functions	Direct instruction,	
(w.r.t. a preorder relation) and the their extremum	mathematical proof,	
points; examples of linear/nonlinear monotone	exemplification	
functions; conical sections of a set; the existence of		
efficient/weakly efficient points.		
5. Sufficient conditions for efficiency and weak	Direct instruction,	
efficiency. Cone-convex sets; necessary conditions for	mathematical proof,	
weak-efficiency. Proper efficient points.	exemplification	
6. Cone-convex vector-valued functions, their	Direct instruction,	
characterizations by means of the epigraph and the	mathematical proof,	
polar cone; the cone-convexity of the images of	exemplification	
convex sets by cone-convex functions.		
7. Explicitly cone-quasiconvex functions and	Direct instruction,	
lexicographic quasiconvex vector-valued functions,	mathematical proof,	
their characterization and some of important	exemplification	
properties; the relationship between explicit cone-		
convexity and lexicographic quasiconvexity.		

8. Scalarization methods for vector optimization	Direct instruction,	
problems: the weighting method (for convex objective	mathematical proof,	
functions); the parametric method (for quasiconvex/,	exemplification	
explicitly quasiconvex/ explicitly quasiaffine objective		
functions).		
9. The geometric and topological structure of the	Direct instruction,	
boundary of a closed radiant set (the homeomorphism	mathematical proof,	
of Bonnisseau-Cornet).	exemplification	
10. Simply shaded and completely shaded sets (w.r.t. a	Direct instruction,	
convex cone) and their characterizations. The	mathematical proof,	
connectedness /contractibility of the sets of efficient	exemplification	
points.		
11. The role of Helly's Theorem in reducing the	Direct instruction,	
number of criteria involved in vector optimization	mathematical proof,	
with convex/quasiconvex objective functions.	exemplification	
12. Pareto reducible vector optimization problems	Direct instruction,	
involving explicitly / lexicographic quasiconvex	mathematical proof,	
objective functions.	exemplification	
13. Approximate efficient / weakly efficient solutions	Direct instruction,	
and their role in numerical methods.	mathematical proof,	
	exemplification	
14. Efficient sequences and their relationship with the	Direct instruction.	
minimizing sequences of certain scalarization	mathematical proof.	
functions.	exemplification	
Bibliography		
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2006		ii, Ei ES, Ciuj Hupoeu,
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convex/polyhedral sets by certain cone-convex	instruction debate	
functions and their (weakly) efficient points	mathematical proofs	
8 Geometric representation of the level sets of cortain	Problem based	
8. Geometric representation of the level sets of certain	r iobienii-based	
cone-quasiconvex vector-valued functions.	instruction, debate,	
	mathematical proofs	
9. Exercises concerning explicitly quasiconvex	Problem-based	
functions (in particular, lexicographic convex	instruction, debate,	
functions and linear-fractional functions).	mathematical proofs	
10. Bicriteria optimization problems solved by a	Problem-based	
geometrical approach.	instruction, debate,	
	mathematical proofs	
11. Linear vector optimization problems solved by the	Problem-based	
weighting scalarization method.	instruction, debate,	
	mathematical proofs	
12. Nonlinear vector optimization problems solved by	Problem-based	
the weighting scalarization method.	instruction, debate,	
	mathematical proofs	
13. Linear vector optimization problems solved by the	Problem-based	
parametric method.	instruction, debate,	
-	mathematical proofs	
14. Nonlinear vector optimization problems solved by	Problem-based	
the parametric method.	instruction, debate,	
	mathematical proofs	

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9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

The course ensures a solid theoretical background, according to national and international standards

10. Evaluation					
Type of activity	10.1 Evaluation criteria	10.2 Evaluation methods	10.3 Share in the grade (%)		
10.4 Course	 Knowledge of theoretical concepts and capacity to rigorously prove the main theorems; Ability to solve practical exercises and theoretical problems 	Written tests	75%		
10.5 Seminar/lab activities	- Attendance and active class participation	Continuous evaluation	25%		
10.6 Minimum performance standards					
The final grade should be greater than or equal to 5.					

Date	Signature of course coordinator	Signature of seminar coordinator
29.04.2020	Prof. Nicolae Popovici, Ph.D. Habil.	Prof. Nicolae Popovici, Ph.D. Habil.
Date of approval		Signature of the head of department
		Prof. Octavian Agratini, Ph.D.