#### **SYLLABUS**

# 1. Information regarding the programme

| 1.1 Higher education  | Babeş-Bolyai University                     |
|-----------------------|---|
| institution           |   |
| 1.2 Faculty           | Faculty of Mathematics and Computer Science |
| 1.3 Department        | Department of Mathematics                   |
| 1.4 Field of study    | Mathematics                                 |
| 1.5 Study cycle       | Master                                      |
| 1.6 Study programme / | Advanced Mathematics                        |
| Qualification         |   |

# 2. Information regarding the discipline

| 2.1 Name of the discipline Category theory        |     |          |   |                      |       |             |          |
|---|-----|----------|---|----------------------|-------|-------------|----------|
| 2.2 Course coor                                   | din | ator     |   | Prof.PhD. Septimiu ( | Crive | i           |          |
| 2.3 Seminar coordinator Prof.PhD. Septimiu Crivei |     |          |   |                      |       |             |          |
| 2.4. Year of                                      | 2   | 2.5      | 2 | 2.6. Type of         | E     | 2.7 Type of | Optional |
| study   |     | Semester |   | evaluation           |       | discipline  |          |

### **3. Total estimated time** (hours/semester of didactic activities)

| 3.1 Hours per week  | 3      | Of which: 3.2 course     | 2  | 3.3                | 1     |
|---|--------|--------------------------|----|--------------------|-------|
|   |        |                          |    | seminar/laboratory |       |
| 3.4 Total hours in the curriculum   | 42     | Of which: 3.5 course     | 28 | 3.6                | 14    |
|   |        |                          |    | seminar/laboratory |       |
| Time allotment:   |        |                          |    |                    | hours |
| Learning using manual, course suppor  | t, bit | oliography, course notes | 5  |                    | 28    |
| Additional documentation (in libraries, on electronic platforms, field documentation) |        |                          |    |                    |       |
| Preparation for seminars/labs, homework, papers, portfolios and essays                |        |                          |    |                    |       |
| Tutorship   |        |                          |    |                    |       |
| Evaluations   |        |                          |    |                    |       |
| Other activities:   |        |                          |    |                    |       |
| 3.7 Total individual study hours 133  |        |                          |    |                    |       |
| 3.8 Total hours per semester 175  |        |                          |    |                    |       |
| 3.9 Number of ECTS credits 7  |        |                          |    |                    |       |

# **4. Prerequisites** (if necessary)

| 4.1. curriculum   | Algebraic structures |
|-------------------|----------------------|
| 4.2. competencies | •                    |

# **5. Conditions** (if necessary)

| ·                         |   |  |
|---------------------------|---|--|
| 5.1. for the course       | • |  |
| 5.2. for the seminar /lab | • |  |
| activities                |   |  |

# 6. Specific competencies acquired

| <b>Professional</b> competencies | <ul> <li>Ability to operate with abstract concepts.</li> <li>Ability to apply the acquired knowledge to subdomains of mathematics.</li> </ul> |
|----------------------------------|---|
| Transversal competencies         | <ul> <li>Development of abstract thinking.</li> <li>Ability to perform research.</li> </ul>   |

#### 7. Objectives of the discipline (outcome of the acquired competencies)

| •                             |   | 1 /  |
|-------------------------------|---|--|
| 7.1 General objective of the  | • | To acquire the basic knowledge on category theory. |
| discipline                    |   |  |
|                               |   |  |
| 7.2 Specific objective of the | • | To acquire specific working techniques.            |
| discipline                    |   |  |
|                               |   |  |

#### 8. Content

| 8.1 Course |                                      | Teaching methods            | Remarks |
|------------|--------------------------------------|-----------------------------|---------|
| 1.         | Categories - definition and examples | Exposition, proof, examples |         |
| 2.         | Special objects and morphisms        | Exposition, proof, examples |         |
| 3.         | Constructions on categories          | Exposition, proof, examples |         |
| 4.         | Products and coproducts              | Exposition, proof, examples |         |
| 5.         | Equalizers and coequalizers          | Exposition, proof, examples |         |
| 6.         | Pullbacks and pushouts               | Exposition, proof, examples |         |
| 7.         | Limits and colimits                  | Exposition, proof, examples |         |
| 8.         | Natural transformations              | Exposition, proof, examples |         |
| 9.         | Equivalence of categories            | Exposition, proof, examples |         |
| 10.        | Yoneda Lemma                         | Exposition, proof, examples |         |
| 11.        | Adjoint functors                     | Exposition, proof, examples |         |
| 12.        | Grothendieck categories              | Exposition, proof, examples |         |
| 13.        | Abelian categories                   | Exposition, proof, examples |         |
| 14.        | Exact categories                     | Exposition, proof, examples |         |

#### Bibliography

- 1. S. Awodey, Category theory, Oxford University Press, 2010.
- 2. S. Mac Lane, Categories for the working mathematician, Springer, 1998.
- 3. B. Mitchell, Theory of categories, Academic Press, New York, London, 1965.
- 4. C. Nastasescu, Inele, module, categorii (in Romanian), Editura Academiei, Bucuresti, 1976.
- 5. I. Purdea, Tratat de algebra moderna, vol. II (in Romanian), Editura Academiei, Bucuresti, 1982.

| 8.2 Seminar / | laboratory                    | Teaching methods                        | Remarks |
|---------------|-------------------------------|---|---------|
| 1.            | Categories - definition and   | Explanation, problematization, examples |         |
| exam          | ples                          |   |         |
| 2.            | Special objects and morphisms | Explanation, problematization, examples |         |
| 3.            | Constructions on categories   | Explanation, problematization, examples |         |
| 4.            | Products and coproducts       | Explanation, problematization, examples |         |
| 5.            | Equalizers and coequalizers   | Explanation, problematization, examples |         |

| 6.  | Pullbacks and pushouts    | Explanation, problematization, examples |
|-----|---------------------------|---|
| 7.  | Limits and colimits       | Explanation, problematization, examples |
| 8.  | Natural transformations   | Explanation, problematization, examples |
| 9.  | Equivalence of categories | Explanation, problematization, examples |
| 10. | Yoneda Lemma              | Explanation, problematization, examples |
| 11. | Adjoint functors          | Explanation, problematization, examples |
| 12. | Grothendieck categories   | Explanation, problematization, examples |
| 13. | Abelian categories        | Explanation, problematization, examples |
| 14. | Exact categories          | Explanation, problematization, examples |

#### **Bibliography**

- 1. S. Awodey, *Category theory*, Oxford University Press, 2010.
- 2. S. Mac Lane, Categories for the working mathematician, Springer, 1998.
- 3. B. Mitchell, *Theory of categories*, Academic Press, New York, London, 1965.
- 4. C. Nastasescu, *Inele, module, categorii* (in Romanian), Editura Academiei, Bucuresti, 1976.
- 5. I. Purdea, Tratat de algebra moderna, vol. II (in Romanian), Editura Academiei, Bucuresti, 1982.

# 9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

• The contents is directed towards theory and applications of categories. The topic is present in many master programs from other universities.

#### 10. Evaluation

| Type of activity                   | 10.1 Evaluation criteria | 10.2 Evaluation methods    | 10.3 Share in the |  |  |  |
|------------------------------------|--------------------------|----------------------------|-------------------|--|--|--|
|                                    |                          |                            | grade (%)         |  |  |  |
| 10.4 Course                        | Use of basic concepts,   | Test, project.             | 25                |  |  |  |
|                                    | examples                 |                            |                   |  |  |  |
| 10.5 Seminar/lab activities        | Problem solving          | Presentation, assignments. | 75                |  |  |  |
| 10.6 Minimum performance standards |                          |                            |                   |  |  |  |
| Grade 5                            |                          |                            |                   |  |  |  |

Date Signature of course coordinator Signature of seminar coordinator

19.04.2018 Prof.PhD. Septimiu CRIVEI Prof.PhD. Septimiu CRIVEI

Date of approval Signature of the head of department

Prof.PhD. Octavian AGRATINI