SYLLABUS

1. Information regarding the programme

1.1 Higher education institution	**Babeş Bolyai University**
1.2 Faculty	**Faculty of Mathematics and Computer Science**
1.3 Department	**Department of Mathematics**
1.4 Field of study	**Mathematics**
1.5 Study cycle	**Master**
1.6 Study programme / Qualification	**Mathematics**

2. Information regarding the discipline

2.1 Name of the discipline	**MME3122 Representations of groups and algebras**						
2.2 Course coordinator	prof. dr. Andrei Marcus						
2.3 Seminar coordinator	prof. dr. Andrei Marcus						
2.4. Year of study	**1**	2.5 Semester	**2**	2.6. Type of evaluation	**E**	2.7 Type of discipline	**Optional**

3. Total estimated time (hours/semester of didactic activities)

3.1 Hours per week	4	Of which: 3.2 course	2	3.3 seminar/laboratory	1+1
3.4 Total hours in the curriculum	56	Of which: 3.5 course	28	3.6 seminar/laboratory	14+14
Time allotment:					hours
Learning using manual, course support, bibliography, course notes					24
Additional documentation (in libraries, on electronic platforms, field documentation)					24
Preparation for seminars/labs, homework, papers, portfolios and essays					28
Tutorship					7
Evaluations					5
Other activities: **project**					**7**

3.7 Total individual study hours	88
3.8 Total hours per semester	130
3.9 Number of ECTS credits	7

4. Prerequisites (if necessary)

4.1. curriculum	- deep knowledge of bachelor level algebra, especially of the following subjects: - algebraic structures - linear algebra
4.2. competencies	- ability to perform symbolic calculations ability to operate with abstract concepts - ability to do logical deductions - ability to solve mathematics problems bases on aquired notions

5. Conditions (if necessary)

5.1. for the course	• blackboard, projector
5.2. for the seminar /lab activities	• blackboard

6. Specific competencies acquired

Professional competencies	• ability to perform symbolic calculations in various structures (groups, rings and fields, vector spaces, algebras, matrix algebras etc) • ability to operate with abstract concepts • ability to complex logical deductions • ability to solve mathematics problems bases on aquired notions	
Transversal competencies	- abstract reasoning - applying mathematics in real life - ability to solve problems	

7. Objectives of the discipline (outcome of the acquired competencies)

7.1 General objective of the discipline	• Advanced knowledge on group theory. Ability to solve more difficult problems
7.2 Specific objective of the discipline	• students will operate with fundamental concepts of group theory • students will aquire knowlegde regarding the structure of groups from various important classes. • students solve problems, theoretical and practical, using instruments of modern algebra, regarding matrix representations and characters.

8. Content

8.1 Course	Teaching methods	Remarks
Week 1. Algebras, subalgebras, homomorphisms, ideals, factor algebras.	Explanation, dialogue, examples, proofs	
Week 2. Examples. Group algebra. Path algebra of a quiver.	Explanation, dialogue, examples, proofs	
Week 3. Representations and modules. Simple modules (irreducible representations) and indecomposable modules.	Explanation, dialogue, examples, proofs	
Week 4. Tensor products. Enveloping algebra of a Lie algebra.	Explanation, dialogue, examples, proofs	
Week 5. Hopf algebras.	Explanation, dialogue, examples, proofs	
Week 6. Semisimple algebras and modules.	Explanation, dialogue, examples, proofs	
Week 7. The Jordan-Holder and Krull-Schmidt Theorems.	Explanation, dialogue, examples, proofs	
Week 8. Representations of finite groups. Characters.	Explanation, dialogue, examples, proofs	
Week 9. Orthogonality of characters.	Explanation, dialogue, examples, proofs	

Week 10. Character table of a finite group.	Explanation, dialogue, examples, proofs	
Week 11. Products of characters.	Explanation, dialogue, examples, proofs	
Week 12. Induced characters. Frobenius reciprocity.	Explanation, dialogue, examples, proofs	
Week 13. Burnside's Theorem.	Explanation, dialogue, examples, proofs	
Week 14. Representations ot the symmetric group.	Explanation, dialogue, examples, proofs	

Bibliography

[1] J.L. Alperin and R.B. Bell. *Groups and representatons*. Springer-Verlag. 1995.
[2] P. Etingof et al. *Introduction to representation theory*. American Mathematical Society 2011.

8.2 Seminar / laboratory	Teaching methods	Remarks
Week 1. Algebras, subalgebras, homomorphisms, ideals, factor algebras.	dialogue, examples, proofs	
Week 2. Examples. Group algebra. Path algebra of a quiver.	dialogue, examples, proofs	
Week 3. Representations and modules. Simple modules (irreducible representations) and indecomposable modules.	dialogue, examples, proofs	
Week 4. Tensor products. Enveloping algebra of a Lie algebra.	dialogue, examples, proofs	
Week 5. Hopf algebras.	dialogue, examples, proofs	
Week 6. Semisimple algebras and modules.	dialogue, examples, proofs	
Week 7. The Jordan-Holder and Krull-Schmidt Theorems.	dialogue, examples, proofs	
Week 8. Representations of finite groups. Characters.	dialogue, examples, proofs	
Week 9. Orthogonality of characters.	dialogue, examples, proofs	
Week 10. Character table of a finite group.	dialogue, examples, proofs	
Week 11. Products of characters.	dialogue, examples, proofs	
Week 12. Induced characters. Frobenius reciprocity.	dialogue, examples, proofs	
Week 13. Burnside's Theorem.	dialogue, examples, proofs	
Week 14. Representations ot the symmetric group.	dialogue, examples, proofs	

Bibliography

3. B.E. Sagan. *The symmetric group*. Springer-Verlag. 2001.
4. I.Assem. *Algebres et modules*. Univ. Ottawa. 1997.
5. T.Y. Lam. *A first course in noncommutative rings*. 2nd ed. Springer Verlag 2001.
6. M. Auslander, I. Reiten, S.O. Smalø. *Representation Theory of Artin Algebras*, Cambridge Univ. Press, 1995.
7. D.J. Benson, *Representations and Cohomology, vol. I, II*. Cambridge Univ. Press, 1998.

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

- Such a course exists in the curricula of all major universities in Romania and abroad;
- Groups are fundamental mathematical structures and have multiple applications in geometry, number theory, cryptography, chemistry and physics, as they measure symmetry.

10. Evaluation

Type of activity	10.1 Evaluation criteria	10.2 Evaluation methods	10.3 Share in the grade (%)
10.4 Course	- know the basic principles of the field; - apply the new concepts	- written exam	75%
10.5 Seminar/lab activities	- problem solving	- homeworks	25%
10.6 Minimum performance standards			
➢ to aquire 5 points to pass the exam			

Date	Signature of course coordinator	Signature of seminar coordinator
17.04.2018	Prof.dr. Andrei Mărcuș	Prof.dr. Andrei Mărcuș

Date of approval ..... Signature of the head of department

Prof. dr. Octavian Agratini