SYLLABUS

1.1 Higher education	Babeş-Bolyai University Cluj-Napoca
institution	
1.2 Faculty	Faculty of Mathematics and Computer Science
1.3 Department	Department of Mathematics
1.4 Field of study	Mathematics
1.5 Study cycle	Master
1.6 Study programme /	Advanced Mathematics (Matematici avansate)
Qualification	

1. Information regarding the programme

2. Information regarding the discipline

2.1 Name of the	dis	cipline	Ge	Geometric function theory in several complex variables (Teoria				
			geo	geometricã a funcțiilor de mai multe variabile complexe)				
2.2 Course coor	dina	ator	Professor Gabriela KOHR					
2.3 Seminar coordinator				Professor Gabriela KOHR				
2.4. Year of	2	2.5	4	2.6. Type of	Ε	2.7 Type of	Optional/DS	
study		Semester		evaluation		discipline		

3. Total estimated time (hours/semester of didactic activities)

3.1 Hours per week	3	Of which: 3.2 course	2	3.3	1 sem
				seminar/laboratory	
3.4 Total hours in the curriculum	36	Of which: 3.5 course	24	3.6	12
				seminar/laboratory	
Time allotment:					hours
Learning using manual, course support, bibliography, course notes					42
Additional documentation (in libraries, on electronic platforms, field documentation)					35
Preparation for seminars/labs, homework, papers, portfolios and essays					42
Tutorship					25
Evaluations					20
Other activities:					-
3 7 Total individual study hours		164			•

3.7 Total individual study hours	164
3.8 Total hours per semester	200
3.9 Number of ECTS credits	8

4. Prerequisites (if necessary)

4.1. curriculum	•	Complex analysis; Real functions; Functional analysis.
4.2. competencies	•	The are useful logical thinking and mathematical notions and
	results from the above mentioned fields	

5. Conditions (if necessary)

5.1. for the course	Classroom with blackboard/video projector
5.2. for the seminar /lab	Classroom with blackboard/video projector
activities	

6. Specific competencies acquired

		The second field of the second s
Professional competencies	•	Ability to understand and manipulate concepts, individual results and advanced mathematical theories. Ability to use scientific language and to write scientific reports and papers.
Transversal competencies	•	Ability to inform themselves, to work independently or in a team in order to carry out studies and to solve complex problems.Ability to use advanced and complementary knowledge in order to obtain a PhD in Pure Mathematics, Applied Mathematics, or in other fields that use concepts of complex analysis.Ability for continuous self-perfecting and study.

7. Objectives of the discipline (outcome of the acquired competencies)

710 11: .: 6.1			
7.1 General objective of the	• Knowledge, understanding and use of main concepts and results of geometric		
discipline	function theory of several complex variables.		
	• Knowledge, understanding and use of methods of complex analysis in one or		
	higher dimensions in the study of special problems in pure and applied mathematics		
	Ability to use and apply concepts and fundamental results of advanced		
	mathematics in the study of specific problems of function theory in \mathbb{C}^n .		
7.2 Specific objective of the	• Acquiring basic and advanced knowledge in geometric function theory in C ⁿ .		
discipline	• Understanding of main concepts and results in the theory of holomorphic mappings on the unit ball in C ⁿ .		
	 Knowledge understanding and use of advanced topics in mathematics in the 		
	study of special problems in several complex variables.		
	• Ability student involvement in scientific research.		

8. Coi	ntent		
8.1 Co	ourse	Teaching methods	Remarks
1.	The Carathéodory family <i>M</i> of holomorphic	Lectures, modeling,	
	mappings in several complex variables. Growth	didactical demonstration,	
	and distortion results, coefficient bounds.	conversation. Presentation	
	Compactness of the family M.	of alternative explanations.	
2.	Starlike mappings on the unit ball in C ⁿ . Necessary	Lectures, modeling,	
	and sufficient conditions for starlikeness. Growth,	didactical demonstration,	
	distortion and coefficient bounds.	conversation. Presentation	
		of alternative explanations.	
3.	Convex mappings on the unit ball in \mathbb{C}^n . Necessary	Lectures, modeling,	
	and sufficient conditions for convexity on the	didactical demonstration,	
	Euclidean unit ball and the unit polydisc in \mathbb{C}^n .	conversation. Presentation	

		of alternative explanations.			
4.	Growth, distortion and coefficient bounds for	Lectures, modeling,			
	convex mappings on the unit ball in \mathbf{C}^{n} .	didactical demonstration,			
		conversation. Presentation			
		of alternative explanations.			
5.	Loewner chains and transition mappings (evolution	Lectures, modeling,			
	families) in \mathbb{C}^n .	didactical demonstration.			
	,	conversation. Presentation			
		of alternative explanations.			
6	Loewner chains Herglotz vector fields and the	Lectures modeling			
0.	generalized L oewner differential equation in \mathbf{C}^n	didactical demonstration			
	Seneralized Dee wher anterential equation in e :	conversation Presentation			
		of alternative explanations			
7	Kernel convergence and hiholomorphic	Lectures modeling			
/.	monnings on the unit hall in \mathbf{C}^n Applications	didactical demonstration			
	mappings on the unit ban in \mathbb{C} . Applications	conversation Presentation			
	in the theory of Loewner chains.	of alternative explanations			
Q	The solutions of the generalized Leowner	L acturas modeling			
0.	differential equation in C^n	didactical demonstration			
	unierentiai equation in C.	didactical demonstration,			
		conversation. Presentation			
		of alternative explanations.			
9.	The family $S^{*}(B^{*})$ of biholomorphic mappings with	Lectures, modeling,			
	parametric representation on the unit ball in C ² .	didactical demonstration,			
	Characterizations in terms of Loewner chains.	conversation. Presentation			
	Compactness of the family S ^o (B ⁿ). Open problems.	of alternative explanations.			
10.	Extreme points and support points associated with	Lectures, modeling,			
	the family S [°] (B ⁿ). Open problems and conjectures.	didactical demonstration,			
		conversation. Presentation			
		of alternative explanations.			
11	. Univalence criteria on the unit ball in \mathbf{C}^n via	Lectures, modeling,			
	the theory of Loewner chains. Parametric	didactical demonstration,			
	representation and asymptotic starlikeness in	conversation. Presentation			
	higher dimensions.	of alternative explanations.			
12	Extension operators that preserve analytic and	Lectures, modeling.			
	geometric properties (starlikeness, convexity	didactical demonstration.			
	L course choing nonematric representation)	conversation Presentation			
	Loewner chains, parametric representation).	of alternative explanations			
Biblio	granhy	of uternarite enplanations.			
1	I Graham G Kohr Geometric Function Theory in (One and Higher Dimensions M	arcel Dekker Inc New		
1.	Vork 2003	The and Higher Dimensions, M	larcer Derker me., wew		
	101k, 2005.				
2.	G. Kohr. Basic Topics in Holomorphic Functions of	Several Complex Variables. Cl	ui University Press, Clui-		
	Napoca. 2003.				
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3.	G. Kohr, P. Liczberski, Univalent Mappings of Sever	al Complex Variables, Cluj Ur	niversity Press, Cluj-		
	Napoca, 1998.				
4.	4. S. Gong, <i>Convex and Starlike Mappings in Several Complex Variables</i> , Kluwer Acad. Publ., Dordrecht, 1998.				
5.	5. P. Duren, Univalent Functions, Springer-Verlag, New York, 1983.				
6.	6. S.G. Krantz, <i>Function Theory of Several Complex Variables</i> , Reprint of the 1992 Edition, AMS Chelsea Publishing, Providence, Rhode Island, 2001.				
7.	7. R. Narasimhan, Several Complex Variables, The University of Chicago Press, Chicago, 1971.				
8.	Ch. Pommerenke, Univalent Functions, Vandenhoec	k & Ruprecht, Göttingen, 1975	i.		
9.	T. Poreda, On generalized differential equations in B 1-50.	Banach spaces, Dissertationes M	Mathematicae, 310 (1991),		

- 10. M. Range, *Holomorphic Functions and Integral Representations in Several Complex Variables* Springer-Verlag, New York, 1986.
- 11. S. Reich, D. Shoikhet, *Nonlinear Semigroups, Fixed Points, and Geometry of Domains in Banach Spaces*, Imperial College Press, London, 2005.
- 12. W. Rudin, Function Theory in the Unit Ball of Cⁿ, Springer-Verlag, New York, 1980.

8.2 Sen	ninar	Teaching methods	Remarks
1.	Examples of mappings in the Carathéodory family	Applications of course	1 hour/week
	<i>M</i> . Special subclasses of <i>M</i> . Distortion and	concepts. Description of	
	coefficient bounds.	arguments and proofs for	
		solving problems.	
		Homework assignments.	
		Direct answers to students	
2	Sufficient conditions of starlikeness on the unit	Applications of course	1 hour/week
2.	ball in C^n Examples of starlike mappings	concepts Description of	
	ball in C. Examples of startike mappings.	arguments and proofs for	
		solving problems	
		Homework assignments	
		Direct answers to students	
2	Sufficient conditions of convertity on the unit	Applications of course	1 hour/wook
5.	Sufficient conditions of convexity on the unit C^n . Examples of convexity on the unit	concepts Description of	1 Hour/week
	ball in C. Examples of convex mappings.	concepts. Description of	
		arguments and proofs for	
		Solving problems.	
		Direct or success to students.	
4		Direct answers to students.	11 / 1
4.	Starlike mappings of order α on the Euclidean	Applications of course	1 hour/week
	unit ball in \mathbb{C}^n , $0 \le \alpha < 1$. Growth and coefficient	concepts. Description of	
	bounds. Examples.	arguments and proofs for	
		solving problems.	
		Homework assignments.	
		Direct answers to students.	
5.	Loewner chains and transition mappings (evolution	Applications of course	1 hour/week
	families) in several complex variables. Examples.	concepts. Description of	
		arguments and proofs for	
		solving problems.	
		Homework assignments.	
		Direct answers to students.	
6.	Loewner chains and the associated Loewer	Applications of course	1 hour/week
	PDE in higher dimensions. Applications.	concepts. Description of	
	o 11	arguments and proofs for	
		solving problems.	
		Homework assignments.	
		Direct answers to students.	
7.	The analytical characterizations of starlikeness	Applications of course	1 hour/week
	and spirallikeness of type α on the unit ball in	concepts. Description of	
	\mathbf{C}^{n} in terms of Loewner chains.	arguments and proofs for	
		solving problems.	
		Homework assignments.	
		Direct answers to students.	
8.	Variation of Loewner chains in C ⁿ .	Applications of course	1 hour/week
	Applications.	concepts. Description of	
		arguments and proofs for	
		solving problems.	
		Homework assignments.	
		Direct answers to students.	
9.	Bounded mappings with parametric representation	Applications of course	1 hour/week
	on the unit ball in \mathbf{C}^n . Growth and coefficient	concepts. Description of	
		arguments and proofs for	

bounds. Applications to extremal problems.	solving problems. Homework assignments. Direct answers to students.	
10. Univalence criteria on the unit ball in Cⁿ via the theory of Loewner chains (I).	Applications of course concepts. Description of arguments and proofs for solving problems. Homework assignments. Direct answers to students.	1 hour/week
 Univalence criteria on the unit ball in Cⁿ via the theory of Loewner chains (II). 	Applications of course concepts. Description of arguments and proofs for solving problems. Homework assignments. Direct answers to students.	1 hour/week
12. Extension operators that preserve analytic and geometric properties.	Applications of course concepts. Description of arguments and proofs for solving problems. Homework assignments. Direct answers to students.	1 hour/week

Bibliography

- 1. I. Graham, G. Kohr, *Geometric Function Theory in One and Higher Dimensions*, Marcel Dekker Inc., New York, 2003.
- 2. G. Kohr, *Basic Topics in Holomorphic Functions of Several Complex Variables*, Cluj University Press, Cluj-Napoca, 2003.
- 3. P. Duren, I. Graham, H. Hamada, G. Kohr, *Solutions for the generalized Loewner differential equation in several complex variables*, Math. Ann. **347** (2010), 411-435.
- 4. I. Graham, H. Hamada, G. Kohr, M. Kohr, *Extremal properties associated with univalent subordination chains in* Cⁿ, Math. Ann., **359** (2014), 61-99.
- 5. G. Kohr, P. Liczberski, *Univalent Mappings of Several Complex Variables*, Cluj University Press, Cluj-Napoca, 1998.
- 6. P. Curt, *Special Chapters in Geometric Function Theory of Several Complex Variables*, Editura Albastrã, Cluj-Napoca, 2001 (in Romanian).
- 7. S. Gong, Convex and Starlike Mappings in Several Complex Variables, Kluwer Acad. Publ., Dordrecht, 1998.
- 8. S. Gong, The Bieberbach Conjecture, Amer. Math. Soc. Intern. Press, Providence, R.I., 1999.
- 9. S.G. Krantz, *Function Theory of Several Complex Variables*, Reprint of the 1992 Edition, AMS Chelsea Publishing, Providence, Rhode Island, 2001.
- 10. Ch. Pommerenke, Univalent Functions, Vandenhoeck & Ruprecht, Göttingen, 1975.
- 11. T. Poreda, *On generalized differential equations in Banach spaces*, Dissertationes Mathematicae, **310** (1991), 1-50.
- 12. W. Rudin, Function Theory in the Unit Ball of Cⁿ, Springer-Verlag, New York, 1980.

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

• The content of this discipline is in accordance with the curricula of the most important universities in Romania and abroad, where the advanced mathematics plays an essential role. This discipline is useful in preparing future researchers in pure and applied mathematics, as well as those who use mathematical models and advanced methods of study in other areas.

10. Evaluation

Type of activity	10.1 Evaluation criteria	10.2 Evaluation methods	10.3 Share in the grade (%)	
10.4 Course	Knowledge of concepts and basic results	Written exam.	60%	
	Ability to justify by proofs theoretical results			
10.5 Seminar/lab activities	Ability to apply concepts and results acquired in the course in mathematical modeling and analysis of problems in fluid mechanics	Evaluation of reports and homework during the semester, and active participation in the seminar activity. A midterm written test.	15% 25%	
	There are valid the official rules of the faculty concerning the attendance of students to teaching activities.			
10.6 Minimum performance standards				
• At least grade 5 (from a scale of 1 to 10) at both final written exam and seminar activity during the semester.				

Date	Signature of course coordinator	Signature of seminar coordinator
4.05.2017	Professor PhD Gabriela KOHR	Professor PhD Gabriela KOHR
Date of approval	Signature of the head of department	

Professor Octavian AGRATINI