SYLLABUS

1. Information regarding the programme

| 1.1 Higher education institution | Babeş Bolyai University |
|-------------------------------------|---|
| 1.2 Faculty | Faculty of Mathematics and Computer Science |
| 1.3 Department | Department of Mathematics |
| 1.4 Field of study | Computer Science |
| 1.5 Study cycle | Master |
| 1.6 Study programme / Qualification | Component-based programming |

2. Information regarding the discipline

| 2.1 Name of the discipline | | | Mathematical foundations of the decision-making process | | | | |
|-----------------------------------|------|---|---|--------------|------------|-------------|------------|
| 2.2 Course coordinator | | | Assoc. Prof. Nicolae Popovici, Ph.D. | | | | |
| 2.3 Seminar coordi | nato | r | Assoc. Prof. Nicolae Popovici, Ph.D. | | | | |
| 2.4. Year of study 1 2.5 Semester | | | 1 | 2.6. Type of | Exam | 2.7 Type of | Compulsory |
| | | | evaluation | | discipline | | |

3. Total estimated time (hours/semester of didactic activities)

| 3.1 Hours per week | 3 | Of which: 3.2 course | 2 | 3.3 seminar | 1 |
|---|--------|------------------------|----|-------------|-------|
| 3.4 Total hours in the curriculum | 42 | Of which: 3.5 course | 28 | 3.6 seminar | 14 |
| Time allotment: | | | | | hours |
| Learning using manual, course suppor | t, bib | oliography, course not | es | | 56 |
| Additional documentation (in libraries, on electronic platforms, field documentation) | | | | | 7 |
| Preparation for seminars/labs, homework, papers, portfolios and essays | | | | | 28 |
| Tutorship | | | | | 7 |
| Evaluations | | | | | 35 |
| Other activities: | | | | | |
| 0.5.5. 11. 11. 1. 1. 1. 1. | | 100 | | | |

| 3.7 Total individual study hours | 133 |
|----------------------------------|-----|
| 3.8 Total hours per semester | 175 |
| 3.9 Number of ECTS credits | 7 |

4. Prerequisites (if necessary)

| 4.1. curriculum | Algebra |
|-------------------|---|
| | Geometry |
| | Mathematical Analysis |
| 4.2. competencies | Basic notions of linear algebra, analytical geometry and differential |
| | calculus in the n-dimensional Euclidean space |

5. Conditions (if necessary)

| 5.1. for the course | • |
|---------------------------|---|
| 5.2. for the seminar /lab | • |
| activities | |

6. Specific competencies acquired

| Professional competencies | • | Ability to understand and manipulate advanced concepts and results in the field of optimization theory. Ability to use mathematical methods for solving optimization problems. |
|---------------------------|---|---|
| Transversal competencies | • | Ability to model and analyze from a mathematical point of view practical decision-making processes from other sciences, economics and engineering. |

7. Objectives of the discipline (outcome of the acquired competencies)

| 7.1 General objective of the | The study of fundamental mathematical concepts and practical methods | | |
|-------------------------------|--|--|--|
| discipline | relevant to the decision-making processes. | | |
| 7.2 Specific objective of the | Students should acquire knowledge about: | | |
| discipline | Partially ordered sets; | | |
| | Convex sets, cones and convex functions; | | |
| | Scalar optimization; | | |
| | Vector (multicriteria) optimization. | | |

8. Content

| 8.1 Course | Teaching methods | Remarks |
|--|---------------------|---------|
| 1. Partially ordered sets. | Direct instruction, | |
| | mathematical proof, | |
| | exemplification | |
| 2. Convex sets and cones. | Direct instruction, | |
| | mathematical proof, | |
| | exemplification | |
| 3. Convex functions. | Direct instruction, | |
| | mathematical proof, | |
| | exemplification | |
| 4. Preference relations induced by a scalar | Direct instruction, | |
| function. Scalar optimization problems. | mathematical proof, | |
| | exemplification | |
| 5. Characterization of optimal solutions by means | Direct instruction, | |
| of level sets. Existence and unicity of optimal | mathematical proof, | |
| solutions. | exemplification | |
| 6. Sufficient and necessary optimality conditions. | Direct instruction, | |
| | mathematical proof, | |
| | exemplification | |
| 7. Partially ordered linear spaces. | Direct instruction, | |
| | mathematical proof, | |
| | exemplification | |
| 8. Preference relations induced by a vector | Direct instruction, | |
| function. Vector (multicriteria) optimization | mathematical proof, | |
| problems. | exemplification | |
| 9. Characterization of strongly/ weakly efficient | Direct instruction, | |
| solutions by means of level sets. Existence of | mathematical proof, | |
| efficient solutions | exemplification | |

| 10. Sufficient and necessary conditions for | Direct instruction, |
|---|---------------------|
| strong/weak efficiency. | mathematical proof, |
| | exemplification |
| 11. Scalarization methods. | Direct instruction, |
| | mathematical proof, |
| | exemplification |
| 12. Proper efficient solutions, compromise | Direct instruction, |
| solutions. | mathematical proof, |
| | exemplification |
| 13. The structure of efficiency sets in the | Direct instruction, |
| outcome/decision space. | mathematical proof, |
| | exemplification |
| 14. Decomposition of multicriteria optimization | Direct instruction, |
| problems. | mathematical proof, |
| | exemplification |

Bibliography

- 1. ANDERSON, D.R., SWEENEY, D.J., WILLIAMS, T.A., An Introduction to Management Science. Quantitative Approaches to Decision Making, South-Western College Publishing, Cincinnati, 2000.
- 2. BRECKNER, B.E., POPOVICI, N.: Convexity and Optimization. An Introduction, EFES, Cluj-Napoca, 2006.
- 3. BRECKNER, W.W.: Cercetare operațională, Universitatea Babeș-Bolyai, Cluj-Napoca, 1981.
- 4. POPOVICI, N.: Optimizare vectoriala, Casa Cartii de Stiinta, Cluj-Napoca, 2005.
- 5. VANDERBEI, R.: Linear Programming. Foundations and Extensions, Springer, Boston, 2008.
- 6. YU, P.L.: Multiple Criteria Decision Making: Concepts, Techniques and Extensions, Plenum Press, New York London, 1985.

| Tork London, 1905. | | |
|--|----------------------|---------|
| 8.2 Seminar | Teaching methods | Remarks |
| 1. Preorder relations. | Problem-based | 2 hours |
| | instruction, debate, | |
| | mathematical proofs | |
| 2. Convex sets and cones. | Problem-based | 2 hours |
| | instruction, debate, | |
| | mathematical proofs | |
| 3. Convex functions. | Problem-based | 2 hours |
| | instruction, debate, | |
| | mathematical proofs | |
| 4. Geometric interpretation of the level sets. | Problem-based | 2 hours |
| | instruction, debate, | |
| | mathematical proofs | |
| 5. Scalar optimization problems solved by a | Problem-based | 2 hours |
| geometric approach | instruction | |
| 6. Scalar optimization problems solved by means | Problem-based | 2 hours |
| of optimality conditions. | instruction, debate, | |
| | mathematical proofs | |
| 7. Multicriteria optimization problems solved by | Problem-based | 2 hours |
| a geometric approach. | instruction, debate, | |
| | mathematical proofs | |

Bibliography

- 1. BRECKNER, B.E., POPOVICI, N.: Probleme de cercetare operationala, EFES, Cluj-Napoca, 2006.
- 2. BRECKNER, W.W., DUCA, D.: Culegere de probleme de cercetare operationala, Universitatea Babes-Bolyai, Facultatea de Matematica, Cluj-Napoca, 1983.
- 3. MORDUKHOVICH, B.S., NAM, N.M., An easy path to convex analysis and applications, Morgan & Claypool Publishers, Milton Keynes, 2014.
- 4. POPOVICI, N.: Optimizare vectoriala, Casa Cartii de Stiinta, Cluj-Napoca, 2005.

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

The course ensures a solid theoretical background, according to national and international standards

10. Evaluation

| Type of activity | 10.1 Evaluation criteria | 10.2 Evaluation methods | 10.3 Share in the grade (%) | | | |
|---|--|-------------------------|-----------------------------|--|--|--|
| 10.4 Course | Knowledge of theoretical concepts and capacity to rigorously prove the main theorems; Ability to solve practical exercises and theoretical problems | Written exam | 70% | | | |
| 10.5 Seminar/lab activities | Attendance and active class participation | Continuous evaluation | 30% | | | |
| 10.6 Minimum performance standards | | | | | | |
| The final grade should be greater than or equal to 5. | | | | | | |

| Date | Signature of course coordinator | Signature of seminar coordinator |
|------------------|--------------------------------------|--------------------------------------|
| 15.04.2016 | Assoc. Prof. Nicolae Popovici, Ph.D. | Assoc. Prof. Nicolae Popovici, Ph.D. |
| Date of approval | | Signature of the head of department |
| | | Prof. Octavian Agratini, Ph.D. |