

SYLLABUS

1. Information regarding the programme

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| 1.1 Higher education institution | Babeş Bolyai University |
| 1.2 Faculty | Faculty of Mathematics and Computer Science |
| 1.3 Department | Department of Mathematics |
| 1.4 Field of study | Computer Science |
| 1.5 Study cycle | Master |
| 1.6 Study programme / Qualification | Software Engineering |

2. Information regarding the discipline

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|----------------------------|---|--------------|---|-------------------------|------|------------------------|------------|
| 2.1 Name of the discipline | Mathematical foundations of the decision-making process | | | | | | |
| 2.2 Course coordinator | Assoc. Prof. Nicolae Popovici, Ph.D. | | | | | | |
| 2.3 Seminar coordinator | Assoc. Prof. Nicolae Popovici, Ph.D. | | | | | | |
| 2.4. Year of study | 1 | 2.5 Semester | 1 | 2.6. Type of evaluation | Exam | 2.7 Type of discipline | Compulsory |

3. Total estimated time (hours/semester of didactic activities)

| | | | | | |
|---|-----|----------------------|----|-------------|-------|
| 3.1 Hours per week | 3 | Of which: 3.2 course | 2 | 3.3 seminar | 1 |
| 3.4 Total hours in the curriculum | 42 | Of which: 3.5 course | 28 | 3.6 seminar | 14 |
| Time allotment: | | | | | Hours |
| Learning using manual, course support, bibliography, course notes | | | | | 63 |
| Additional documentation (in libraries, on electronic platforms, field documentation) | | | | | 7 |
| Preparation for seminars/labs, homework, papers, portfolios and essays | | | | | 21 |
| Tutorship | | | | | 7 |
| Evaluations | | | | | 35 |
| Other activities: | | | | | - |
| 3.7 Total individual study hours | 133 | | | | |
| 3.8 Total hours per semester | 175 | | | | |
| 3.9 Number of ECTS credits | 7 | | | | |

4. Prerequisites (if necessary)

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| 4.1. curriculum | <ul style="list-style-type: none"> • Algebra • Geometry • Mathematical Analysis |
| 4.2. competencies | Basic notions of linear algebra, analytical geometry and differential calculus in the n-dimensional Euclidean space |

5. Conditions (if necessary)

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| 5.1. for the course | • |
| 5.2. for the seminar /lab activities | • |

6. Specific competencies acquired

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| Professional competencies | <ul style="list-style-type: none"> • Ability to understand and manipulate advanced concepts and results in the field of optimization theory. • Ability to use mathematical methods for solving optimization problems. |
| Transversal competencies | <ul style="list-style-type: none"> • Ability to model and analyze from a mathematical point of view practical decision-making processes from other sciences, economics and engineering. |

7. Objectives of the discipline (outcome of the acquired competencies)

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| 7.1 General objective of the discipline | The study of fundamental mathematical concepts and practical methods relevant to the decision-making processes. |
| 7.2 Specific objective of the discipline | Students should acquire knowledge about: <ul style="list-style-type: none"> • Partially ordered sets; • Convex sets, cones and convex functions; • Scalar optimization; • Vector (multicriteria) optimization. |

8. Content

| 8.1 Course | Teaching methods | Remarks |
|--|---|---------|
| 1. Partially ordered sets. | Direct instruction, mathematical proof, exemplification | |
| 2. Convex sets and cones. | Direct instruction, mathematical proof, exemplification | |
| 3. Convex functions. | Direct instruction, mathematical proof, exemplification | |
| 4. Preference relations induced by a scalar function. Scalar optimization problems. | Direct instruction, mathematical proof, exemplification | |
| 5. Characterization of optimal solutions by means of level sets. Existence and unicity of optimal solutions. | Direct instruction, mathematical proof, exemplification | |
| 6. Sufficient and necessary optimality conditions. | Direct instruction, mathematical proof, exemplification | |
| 7. Partially ordered linear spaces. | Direct instruction, mathematical proof, exemplification | |
| 8. Preference relations induced by a vector function. Vector (multicriteria) optimization problems. | Direct instruction, mathematical proof, exemplification | |
| 9. Characterization of strongly/ weakly efficient solutions by means of level sets. Existence of efficient solutions.. | Direct instruction, mathematical proof, exemplification | |

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|---|---|--|
| 10. Sufficient and necessary conditions for strong/weak efficiency. | Direct instruction, mathematical proof, exemplification | |
| 11. Scalarization methods. | Direct instruction, mathematical proof, exemplification | |
| 12. Proper efficient solutions, compromise solutions. | Direct instruction, mathematical proof, exemplification | |
| 13. The structure of efficiency sets in the outcome/decision space. | Direct instruction, mathematical proof, exemplification | |
| 14. Decomposition of multicriteria optimization problems. | Direct instruction, mathematical proof, exemplification | |

Bibliography

1. ANDERSON, D.R., SWEENEY, D.J., WILLIAMS, T.A., An Introduction to Management Science. Quantitative Approaches to Decision Making, South-Western College Publishing, Cincinnati, 2000.
2. BRECKNER, B.E., POPOVICI, N.: Convexity and Optimization. An Introduction, EFES, Cluj-Napoca, 2006.
3. BRECKNER, W.W.: Cercetare operațională, Universitatea Babeș-Bolyai, Cluj-Napoca, 1981.
4. POPOVICI, N.: Optimizare vectorială, Casa Cartii de Stiinta, Cluj-Napoca, 2005.
5. VANDERBEI, R.: Linear Programming. Foundations and Extensions, Springer, Boston, 2008.
6. YU, P.L.: Multiple Criteria Decision Making: Concepts, Techniques and Extensions, Plenum Press, New York - London, 1985.

| 8.2 Seminar | Teaching methods | Remarks |
|---|--|---------|
| 1. Preorder relations. | Problem-based instruction, debate, mathematical proofs | 2 hours |
| 2. Convex sets and cones. | Problem-based instruction, debate, mathematical proofs | 2 hours |
| 3. Convex functions. | Problem-based instruction, debate, mathematical proofs | 2 hours |
| 4. Geometric interpretation of the level sets. | Problem-based instruction, debate, mathematical proofs | 2 hours |
| 5. Scalar optimization problems solved by a geometric approach | Problem-based instruction | 2 hours |
| 6. Scalar optimization problems solved by means of optimality conditions. | Problem-based instruction, debate, mathematical proofs | 2 hours |
| 7. Multicriteria optimization problems solved by a geometric approach. | Problem-based instruction, debate, mathematical proofs | 2 hours |

Bibliography

1. BRECKNER, B.E., POPOVICI, N.: Probleme de cercetare operationala, EFES, Cluj-Napoca, 2006.
2. BRECKNER, W.W., DUCA, D.: Culegere de probleme de cercetare operationala, Universitatea Babeș-Bolyai, Facultatea de Matematica, Cluj-Napoca, 1983.
3. MORDUKHOVICH, B.S., NAM, N.M., An easy path to convex analysis and applications, Morgan & Claypool Publishers, Milton Keynes, 2014.
4. POPOVICI, N.: Optimizare vectorială, Casa Cartii de Stiinta, Cluj-Napoca, 2005.

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

The course ensures a solid theoretical background, according to national and international standards

10. Evaluation

| Type of activity | 10.1 Evaluation criteria | 10.2 Evaluation methods | 10.3 Share in the grade (%) |
|---|--|-------------------------|-----------------------------|
| 10.4 Course | - Knowledge of theoretical concepts and capacity to rigorously prove the main theorems; - Ability to solve practical exercises and theoretical problems | Written exam | 70% |
| 10.5 Seminar/lab activities | Attendance and active class participation | Continuous evaluation | 30% |
| 10.6 Minimum performance standards | | | |
| The final grade should be greater than or equal to 5. | | | |

Date

Signature of course coordinator

Signature of seminar coordinator

15.04.2016

Assoc. Prof. Nicolae Popovici, Ph.D.

Assoc. Prof. Nicolae Popovici, Ph.D.

Date of approval

Signature of the head of department

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Prof. Octavian Agratini, Ph.D.