## Admission exam - September 8 ${ }^{\text {th }} 2023$ <br> Written Exam for Computer Science

## IMPORTANT NOTE:

In the absence of other specifications:

- Assume that all arithmetic operations are performed on unlimited data types (there is no overflow / underflow).
- The indexing of all arrays begins at 1 .
- All restrictions refer to the values of the actual parameters at the moment of the initial call.
- A subsequence of an array consists of elements of that array that occupy consecutive positions.

1. Let us consider the algorithm ceFace $(\mathrm{a}, \mathrm{b})$, where $\boldsymbol{a}$ and $\boldsymbol{b}$ are natural numbers $\left(0 \leq \boldsymbol{a}, \boldsymbol{b} \leq 10^{4}\right)$.
Algorithm ceFace(a, b):
Algorithm ceFace(a, b):
c}\leftarrow
c}\leftarrow
bc}\leftarrow\textrm{b
bc}\leftarrow\textrm{b
While bc \not= 0 execute
While bc \not= 0 execute


bc}\leftarrow\textrm{bc}\mathrm{ DIV 10
bc}\leftarrow\textrm{bc}\mathrm{ DIV 10
EndWhile
EndWhile
If c \# a then
If c \# a then
Return ceFace(a - 1, b - 1)
Return ceFace(a - 1, b - 1)
EndIf
EndIf
Return a
Return a
EndAlgorithm
EndAlgorithm

What is the effect of the call ceFace $(a, a)$ ?
A. The algorithm returns the smallest palindrome that is greater or equal to $\boldsymbol{a}$.
B. The algorithm returns the largest palindrome that is less or equal to $\boldsymbol{a}$.
C. The algorithm returns the smallest palindrome that is greater than $\boldsymbol{a}$.
D. The algorithm returns the largest even number that is less or equal to $\boldsymbol{a}$.
2. Let us consider the algorithm creareTablou( $n, m, x$ ), where $\boldsymbol{n}$, $\boldsymbol{m}$ are natural numbers $(1 \leq \boldsymbol{n}, \boldsymbol{m} \leq 100)$, and $\boldsymbol{x}$ is a bidimensional array with $\boldsymbol{n} * \boldsymbol{m}$ integer number elements $\left(\boldsymbol{x}[1][1], \boldsymbol{x}[1][2], \ldots, \boldsymbol{x}[\boldsymbol{n}][\boldsymbol{m}], 0 \leq \boldsymbol{x}[\boldsymbol{i}][\boldsymbol{j}] \leq 10^{4}\right.$, for $\boldsymbol{i}=1,2, \ldots, \boldsymbol{n} ; \boldsymbol{j}=1,2, \ldots, \boldsymbol{m})$.

```
Algorithm creareTablou( \(n, m, x\) ):
    \(k \leftarrow 0\)
    For \(\mathrm{i} \leftarrow 1\), n execute
        For \(j \leftarrow 1\), \(m\) execute
            If \(k\) MOD \(2 \neq 0\) then
                \(x[i][j] \leftarrow k * k\)
            EndIf
            Write \(x[i][j]\), " "
            \(k \leftarrow k+1\)
        EndFor
        Write new line
    EndFor
EndAlgorithm
```

What does the algorithm display if the elements of the array $\boldsymbol{x}$ are initialized with 0 ?
A. The algorithm displays the elements of the bidimensional array $\boldsymbol{x}$, in which there are elements equal to 0 and the first $(\boldsymbol{n} * \boldsymbol{m})$ DIV 2 odd perfect squares.
B. The algorithm displays the elements of the bidimensional array $\boldsymbol{x}$, in which there are values equal to 0 and the first even perfect squares.
C. The algorithm displays the elements of the bidimensional array $\boldsymbol{x}$, in which there are the first $(\boldsymbol{n} * \boldsymbol{m})$ DIV 2 even perfect squares.
D. The algorithm displays the elements of the bidimensional array $\boldsymbol{x}$, in which - if we laid out the elements one line after the other - the odd perfect squares would be in ascending order, possibly preceded and/or succeeded by values equal to 0 .
3. Let us consider the algorithm something $(n, x)$, where $\boldsymbol{n}$ is a natural number $\left(1 \leq \boldsymbol{n} \leq 10^{4}\right)$, and $\boldsymbol{x}$ is an array of $\boldsymbol{n}$ natural numbers $\left(\boldsymbol{x}[1], \boldsymbol{x}[2], \ldots, \boldsymbol{x}[\boldsymbol{n}], 1 \leq \boldsymbol{x}[\boldsymbol{i}] \leq 10^{6}\right.$, for $\boldsymbol{i}=1,2, . ., n$ ).

```
Algorithm something(n, x):
    s}\leftarrow
    For i}\leftarrow1, n execut
        nr}\leftarrow
        While x[i] > 9 execute
            nr}\leftarrownr+
            x[i]}\leftarrowx[i] DIV 10
        EndWhile
        s}\leftarrow\textrm{s}+\textrm{nr
    EndFor
    Return s
EndAlgorithm return?
A. 16
B. 10
C. 11
D. 15
```


## EndWhile

```
s + nr
EndFor
Return s
```

What does the call something(5, [222, 2043, 29, 2, 20035])
4. Let us consider the algorithm ceFace( $n, v, a$ ), where $\boldsymbol{n}$ and $\boldsymbol{v}$ are two natural numbers $\left(1 \leq \boldsymbol{n}, \boldsymbol{v} \leq 10^{4}\right)$, and $\boldsymbol{a}$ is an array of natural numbers with $\boldsymbol{n}$ elements (a[1], $\boldsymbol{a}[2], \ldots, \boldsymbol{a}[\boldsymbol{n}])$.

```
Algorithm ceFace(n, v, a):
    For i}\leftarrow1,n execut
        d}\leftarrow
        If a[i] # 0 then
            găsit \leftarrowFalse
            While (d \leq v * a[i]) AND (NOT găsit) execute
                If ((d DIV a[i]) * a[i] = d) AND ((d DIV v) * v = d) then
                    găsit \leftarrow True
                Else
                    d}\leftarrowd+
                EndIf
                EndWhile
        EndIf
        v}\leftarrow
    EndFor
    Return v
EndAlgorithm
```

What is the value returned by the algorithm, if $\boldsymbol{n}=4, \boldsymbol{v}=3$ and $\boldsymbol{a}=[5,4,2,10]$ ?
A. 20
B. 120
C. 60
D. 15
5. Let us consider the algorithm calcul( $v, n$ ), where $\boldsymbol{n}$ is a natural number $\left(1 \leq \boldsymbol{n} \leq 10^{4}\right)$, and $\boldsymbol{v}$ is an array with $\boldsymbol{n}$ elements which are natural numbers $\left(v[1], v[2], \ldots, v[n], 1 \leq v[i] \leq 10^{4}\right.$, for $\boldsymbol{i}=1,2, \ldots, n$ ):

```
Algorithm calcul(v, n):
    i}\leftarrow
    While i \leq n DIV 2 execute
        p}\leftarrow
        While v[i] & 0 execute
            p}\leftarrowp+
            v[i] \leftarrowv[i] DIV 10
        EndWhile
        q}\leftarrow
        While v[n + 1 - i] # 0 execute
            q}\leftarrowq+
            v[n+1 - i] \leftarrowv[n + 1 - i] DIV 10
        EndWhile
        If p & q then
            Return False
        EndIf
        i}\leftarrow i + 1
    EndWhile
    Return True
EndAlgorithm
```

In which of the following situations the algorithm returns True?
A. If the array $\boldsymbol{v}$ consists of the values $[12,12,2,5466,3,111,1,3,44]$ and $\boldsymbol{n}=9$.
B. If the array $\boldsymbol{v}$ consists of the values $[12,345,2,5466,3,111,10]$ and $\boldsymbol{n}=7$.
C. If the elements of the array $v$ have the same number of digits.
D. If the array consisting of the number of digits of the elements of array $v$ forms a palindrome; for example, from $v=[8,37,3]$ the array $[1,2,1]$ is formed, which is a palindrome.
6. Let us consider the algorithm $\operatorname{alg}(\mathrm{n})$, where $\boldsymbol{n}$ is a natural number $\left(0 \leq \boldsymbol{n} \leq 10^{4}\right)$.

```
Algorithm alg(n):
    If n = 0 then
        Return 0
    Else
        If n MOD 2 = 0 then
            Return alg(n DIV 10) + n MOD 10
        Else
            Return alg(n DIV 10)
        EndIf
    EndIf
EndAlgorithm
```

Which of the following statements are true?
A. The call alg(123) returns 6 .
B. The algorithm calculates the sum of the digits found on even positions in the given number.
C. The algorithm calculates the sum of the even digits from the given number.
D. The algorithm calculates the sum of the digits of the given number.
7. Let us consider the algorithm $f(x)$, where $\boldsymbol{x}$ is a non-zero natural number $\left(1 \leq \boldsymbol{x} \leq 10^{5}\right)$.

```
Algorithm f(x):
    If }x>0\mathrm{ then
        x}\leftarrowx\mathrm{ DIV 2
        f(x)
        Write x, " "
        x}\leftarrowx\mathrm{ DIV 2
        f(x)
    EndIf
EndAlgorithm
```

What will be displayed after the call $f(10)$ ?
A. 0120501
B. 012510
C. 121521
D. 1211512
8. Let us consider the square matrix $\boldsymbol{M}$ of size $\boldsymbol{n}$ that contains natural numbers, where $\boldsymbol{n}$ is a non-zero natural number $\left(1 \leq \boldsymbol{n} \leq 10^{4}, \boldsymbol{M}[1][1], \ldots, \boldsymbol{M}[1][\boldsymbol{n}], \boldsymbol{M}[2][1], \ldots, \boldsymbol{M}[2][n], \ldots, \boldsymbol{M}[\boldsymbol{n}][1], \ldots, \boldsymbol{M}[\boldsymbol{n}][\boldsymbol{n}], 1 \leq \boldsymbol{M}[\boldsymbol{i}][j] \leq 10^{4}\right.$, for $\boldsymbol{i}=1,2, \ldots$, $\boldsymbol{n}, \boldsymbol{j}=1,2, \ldots, \boldsymbol{n})$. Let us consider the following algorithm:

```
Algorithm what(M, n):
    up }\leftarrow
    down }\leftarrow\textrm{n
    left }\leftarrow
    right \leftarrow n
    While left \leq right AND up \leq down execute
        For i }\leftarrowleft, right execut
                Write M[up][i], " "
        EndFor
        up \leftarrowup + 1
        For i }\leftarrowup, down execut
                Write M[i][right], " " C. 1 2 3 4 5 8 9 7 6
        EndFor
        right \leftarrow right - 1
        For i \leftarrow right, left, -1 execute
            Write M[down][i], " "
        EndFor
        down \leftarrow down - 1
        For i }\leftarrow\mathrm{ down, up, -1 execute
            Write M[i][left], " "
        EndFor
        left \leftarrow left + 1
    EndWhile
EndAlgoritm
```

9. Let us consider the algorithm ce_face(a, b), where $\boldsymbol{a}$ and $\boldsymbol{b}$ are natural numbers $\left(1 \leq \boldsymbol{a}, \boldsymbol{b} \leq 10^{4}\right)$.
```
Algorithm ce_face(a, b):
    If \(a=1\) then
    Return 1
    Else
        If a MOD b = 0 then
            Return ce_face(a DIV b, b)
        Else
            Return 0
        EndIf
    EndIf
EndAlgorithm
```

10. Let us consider the algorithms decide ( $n$ ) and compute $(m)$, where $\boldsymbol{n}$ and $\boldsymbol{m}$ are non-zero natural numbers $\left(1 \leq \boldsymbol{n}, \boldsymbol{m} \leq 10^{4}\right)$ :
```
Algorithm decide(n):
    result \leftarrow-1
    m}\leftarrow
    While n > 0 execute
        m \leftarrow m * 10 + n MOD 10
        n}\leftarrow\textrm{n}\mathrm{ DIV 10
    EndWhile
    If m MOD 3 = 0 then
        result \leftarrow 1
    EndIf
    Return result
EndAlgorithm
```

Algorithm compute(m):
cnt $\leftarrow 0$
For $k \leftarrow 0, m-1$ execute cnt $\leftarrow$ cnt + decide(k)
EndFor
Return cnt
EndAlgorithm

For what values of $\boldsymbol{m}$ the algorithm compute (m) will return -33?
A. 100
B. 99
C. 98
D. 101
11. Let us consider the algorithm $f(n, x)$, where $\boldsymbol{n}$ and $\boldsymbol{x}$ are natural numbers $\left(1 \leq \boldsymbol{n} \leq 10^{5}, 2 \leq \boldsymbol{x} \leq 10\right)$ :

```
Algorithm f(n,x): Which of the following statements are true?
    If n > 0 then
        f(n DIV x, x)
        Write n MOD x
    EndIf
EndAlgorithm
Which of the following statements are true?
A. The algorithm displays the representation of the number \(\boldsymbol{n}\) in base \(\boldsymbol{x}\).
B. The algorithm displays the remainder of the integer division of the number \(\boldsymbol{x}\) to number \(\boldsymbol{n}\).
C. The algorithm displays the number of digits from the representation in base \(\boldsymbol{x}\) of number \(\boldsymbol{n}\).
D. The algorithm checks if the number \(\boldsymbol{n}\) is divisible by \(\boldsymbol{x}\).
```

12. Let us consider the algorithm ceFace( n ), where $\boldsymbol{n}$ is a natural number ( $1 \leq \boldsymbol{n} \leq 10^{9}$ ).
```
Algorithm ceFace(n):
    If n s 9 then
        If n MOD 2 = 0 then
            Return n
        Else
            Return -1
        EndIf
    EndIf
    x \leftarrown MOD 10
    y ceFace(n DIV 10)
    If x MOD 2 f 0 then
        Return y
    EndIf
    If x > y then
        Return x
    EndIf
    Return y
EndAlgorithm
If x MOD \(2 \neq 0\) then
```

Which of the following statements are true?
A. The algorithm returns a number containing a single digit or -1 .
B. The algorithm returns an odd number.
C. The algorithm returns the maximum odd digit from the number $\boldsymbol{n}$, or -1 .
D. The algorithm returns the maximum even digit from the number $\boldsymbol{n}$, or -1 .
13. Let us consider the algorithm decide( $n, x)$, where $\boldsymbol{n}$ is a natural number ( $1 \leq \boldsymbol{n} \leq 10^{4}$ ), and $\boldsymbol{x}$ is an array with $\boldsymbol{n}$ integer numbers as elements ( $\boldsymbol{x}[1], \boldsymbol{x}[2], \ldots, x[\boldsymbol{n}],-100 \leq \boldsymbol{x}[i] \leq 100$, for $\boldsymbol{i}=1,2, \ldots, \boldsymbol{n}$ ):

```
Algorithm decide(n, x):
    b}\leftarrowTru
    i}\leftarrow
    While b = True AND i < n execute
        If x[i] < x[i + 1] then
            b}\leftarrowTru
        Else
            b}\leftarrowFals
        EndIf
        i}\leftarrow i + 1
    EndWhile
    Return b
EndAlgorithm
```

14. Let $\boldsymbol{x}$ and $\boldsymbol{y}$ be two positive natural numbers with the following properties: $\boldsymbol{x}$ is a power of 2 and $\boldsymbol{y}$ is a multiple of 3. Let us consider the following logical expression:
$((x * y+3) \operatorname{DIV} 6=10)$ OR (( $(x * y) \operatorname{MOD} 6=0)$ AND $((x+y)$ MOD $4=0))$
Which of the following statements are true for pairs of numbers that follow the previously mentioned properties?
A. There exists a pair $(\boldsymbol{x}, \boldsymbol{y})$ for which the expression is true.
B. There exists a pair $(\boldsymbol{x}, \boldsymbol{y})$ for which the expression is false.
C. There exist the pairs $\left(\boldsymbol{x}_{1}, \boldsymbol{y}_{1}\right)$ and $\left(\boldsymbol{x}_{2}, \boldsymbol{y}_{2}\right)$, with $\boldsymbol{x}_{\mathbf{1}} \neq \boldsymbol{x}_{\mathbf{2}}$ and $\boldsymbol{y}_{\mathbf{1}} \neq \boldsymbol{y}_{\mathbf{2}}$ such that the expression is true for both pairs.
D. The expression is false for any pair $(\boldsymbol{x}, \boldsymbol{y})$.
15. Let us consider two natural numbers $\boldsymbol{n}$ and $\boldsymbol{m}(1 \leq \boldsymbol{n}, \boldsymbol{m} \leq 256)$ and the arrays of characters $\boldsymbol{a}$, with $\boldsymbol{n}$ characters $(\boldsymbol{a}[1], \boldsymbol{a}[2], \ldots, \boldsymbol{a}[\boldsymbol{n}])$ and $\boldsymbol{b}$ having $\boldsymbol{m}$ characters $(\boldsymbol{b}[1], \boldsymbol{b}[2], \ldots, \boldsymbol{b}[\boldsymbol{m}])$.
Which of the following algorithms return True if the array $\boldsymbol{a}$ can be obtained starting from array $\boldsymbol{b}$ and eliminating some characters without modifying the relative positions of the remaining characters, and False otherwise. For example, the array "ace" can be formed by eliminating characters from the array "abcde", but the array "aec" cannot be obtained in the same manner.
A.
```
    Algorithm hasProperty(a, b, n, m):
        If n = 0 then
            Return True
        EndIf
        If m = 0 then
            Return False
        EndIf
        If a[n] = b[m] then
            Return hasProperty(a, b, n - 1, m - 1)
        EndIf
        Return hasProperty(a, b, n, m - 1)
    EndAlgorithm
```

B.

```
Algorithm hasProperty(a, b, n, m):
    \(i \leftarrow 1\)
    \(j \leftarrow 1\)
    While \(i \leq n\) AND \(j \leq m\) execute
        If \(a[i]=b[j]\) then
                \(i \leftarrow i+1\)
        EndIf
        \(j \leftarrow j+1\)
    EndWhile
    If \(i>n\) then
        Return True
    Else
        Return False
    EndIf
EndAlgorithm
```

C.

```
Algorithm hasProperty( \(a, b, n, m)\) :
    \(i \leftarrow n\)
    \(j \leftarrow m\)
    While \(\mathrm{i}^{*} \mathrm{j}>0\) execute
        If \(a[i]=b[j]\) then
                \(i \leftarrow i-1\)
            EndIf
            \(j \leftarrow j-1\)
    EndWhile
    If \(i=0\) then
        Return True
    Else
        Return False
    EndIf
EndAlgorithm
```

D.
Algorithm hasProperty (a, b, $n, m$ ):
If $n>m$ then
Return False
EndIf
$i \leftarrow 1$
$j \leftarrow 1$
While $i<n$ execute
If $a[i]=b[j]$ then
$i \leftarrow i+1$
EndIf
$j \leftarrow j+1$
EndWhile
If $i>m$ then
Return True
Else
Return False
EndIf
EndAlgorithm
16. Let us consider the algorithm ceva( $\mathrm{x}, \mathrm{n}$, e), where $\boldsymbol{x}$ is an array with $\boldsymbol{n}$ distinct integer elements ( $\boldsymbol{x}[1], \boldsymbol{x}[2], \ldots$, $\boldsymbol{x}[\boldsymbol{n}], 1 \leq \boldsymbol{n} \leq 10^{3}$ and $\boldsymbol{x}[\boldsymbol{i}] \neq \boldsymbol{x}[\boldsymbol{j}]$, for $\left.1 \leq \boldsymbol{i}<\boldsymbol{j} \leq \boldsymbol{n}\right)$ and $\boldsymbol{e}$ is an integer number. The algorithm searches for element $\boldsymbol{e}$ in array $\boldsymbol{x}$, and if it finds it, moves the element to the first position in the array and returns True, without modifying the relative order of the other elements. If $\boldsymbol{e}$ is not found in array $\boldsymbol{x}$, the algorithm returns False and does not modify the array. For example, for array $\boldsymbol{x}$ with elements $[-100,2,71,31,-62,51]$ and $\boldsymbol{e}=31$, the algorithm will return True and the array $\boldsymbol{x}$ will become [31, -100, 2, 71, -62,51]. Which of the following variants represent a correct implementation for the ceva( $\mathrm{x}, \mathrm{n}, \mathrm{e}$ ) algorithm that also has time complexity $O(\boldsymbol{n})$ ?
A.

```
Algorithm ceva(x, n, e):
    index \leftarrow 1
    While index \leq n execute
        If x[index] = e then
            tmp }\leftarrowx[\mathrm{ index]
            x[index]}\leftarrowx[1
            x[1]}\leftarrow tm
            Return True
        EndIf
        index \leftarrow index + 1
    EndWhile
    Return False
EndAlgorithm
```

B.

```
Algorithm ceva(x, n, e):
    index \leftarrow 2
    tmp \leftarrow x[1]
    While index \leq n execute
        If }x[\mathrm{ index] = e then
            x[1]}\leftarrow
            x[index] \leftarrow tmp
            Return True
        EndIf
            tmp2 \leftarrowx[index]
            x[index] \leftarrow tmp
            tmp \leftarrow tmp2
            index \leftarrow index + 1
    EndWhile
    Return False
EndAlgorithm
```

```
C.
Algorithm ceva(x, n, e):
        index \leftarrow n
        While index > 1 execute
            If x[index] = e then
                index2 \leftarrow index
                While index2 > 1 execute
                    x[index2] \leftarrow x[index2 - 1]
                index2 \leftarrow index2 - 1
                EndWhile
                x[index2] \leftarrowe
        EndIf
        index \leftarrow index - 1
    EndWhile
    If }x[1]=e the
        Return True
    Else
        Return False
    EndIf
EndAlgorithm
```

17. Let us consider the algorithm expresie( $x, y, z$ ), where $\boldsymbol{x}, \boldsymbol{y}, \boldsymbol{z}$ are natural numbers $\left(0 \leq \boldsymbol{x}, \boldsymbol{y}, z \leq 10^{4}\right)$ :
```
Algorithm expresie(x, y, z):
    If }x=0\mathrm{ then
            Return z
    Else
        Return expresie(x - 1, y, x * x + y * y + z)
    EndIf
EndAlgorithm
```

Specify which expression value is calculated and returned by the algorithm:
A. $\sum_{i=1}^{x} i^{2}+\sum_{i=1}^{y} x * y+\sum_{k=1}^{z} 1$
B. $\sum_{i=1}^{x} i^{2}+\sum_{j=1}^{y} j^{2}+z$
C. $\sum_{i=1}^{x} i^{2}+x * y^{2}+z$
D. $\sum_{i=1}^{x} i^{2}+\sum_{j=1}^{y} j^{2}+\sum_{k=1}^{x} k$
18. Let us consider the algorithm ceFace $(v, a, b)$, where $\boldsymbol{v}$ is an array of $\boldsymbol{n}$ elements with values from the set $\{0,1\}$, $\left(1 \leq \boldsymbol{n} \leq 10^{4}, \boldsymbol{v}[1], \ldots, \boldsymbol{v}[\boldsymbol{n}]\right)$, and $\boldsymbol{a}$ and $\boldsymbol{b}$ are natural non-zero numbers. The array $\boldsymbol{v}$ is sorted in ascending order.

```
Algorithm ceFace(v, a, b):
    If b - a + 1 = 0 then
            Return 0
    EndIf
    If v[a] = 1 then
        Return b - a + 1
    EndIf
    If v[b] = 0 then
        Return 0
    EndIf
    c}\leftarrow(a+b) DIV 2,
    Return ceFace(v, a, c) + ceFace(v, c + 1, b)
EndAlgorithm
```

considering that the initial call is ceFace $(v, 1, n)$ ?
A. If the array $\boldsymbol{v}$ contains at least one element with value 1 , then the algorithm returns the length of the array.
B. If the array $v$ contains only elements with value 1 , then the algorithm returns the value of $\boldsymbol{n}$.
C. If the array $v$ contains only elements with value 0 , then the algorithm returns 0 .
D. The algorithm returns the number of elements with value 1 contained by array $v$.
19. It is known that the total number of binary arrays (that contain only the characters $\theta$ and 1 ) of length $\boldsymbol{n}$ is $2^{n}$. For example, for $\boldsymbol{n}=2$ those arrays are $00,01,10$ and 11 , their number being $2^{2}=4$. The array 100011 has length 6 and contains as subsequences all of the 4 possible arrays of length $\boldsymbol{n}=2$, since starting from the first position we have 10 , starting with the second position we have 00 , starting from the fourth position we have 01 and starting with the fifth position we have 11.
What is the minimal length of an array that contains as subsequences all the $2^{n}$ possible binary arrays for $\boldsymbol{n}=4$ ?
A. 18
B. 19
C. 20
D. 21
20. Let us consider the algorithm $\mathrm{t}(\mathrm{q}, \mathrm{x}, \mathrm{y})$, where $\boldsymbol{q}$ is a character, and $\boldsymbol{x}$ and $\boldsymbol{y}$ are non-zero natural numbers $(1 \leq \boldsymbol{x}, \boldsymbol{y} \leq 100)$.

```
Algorithm t(q, x, y):
    If }x\leqy\mathrm{ then
        Write q
    Else
        If x MOD y = 0 then
            t(q, x + 1, y - 2)
        Else
            If (x DIV y) MOD 2 f 0 then
                t(q, x - 1, y + 2)
                Write 'c'
            Else
                t(q, x - 1, y - 1)
                    Write "cc"
            EndIf
        EndIf
    EndIf
EndAlgorithm
```

Which of the following statements are true?
A. Calling $\mathrm{t}\left(\mathrm{C}^{\prime}\right.$ ', 33, 28), $\mathrm{t}\left(\mathrm{C}^{\prime}\right.$ ', 10, 6) and $\mathrm{t}\left(\mathrm{c}^{\prime}\right.$, 22,16 ) will result in the same characters being displayed.
B. Calling $\mathrm{t}\left(\mathrm{'c}^{\prime}, 33,28\right)$ and $\mathrm{t}\left(\mathrm{'c}^{\prime}, 45,40\right)$ will not display the same characters.
C. After the call $\mathrm{t}\left(\mathrm{'c}^{\prime}, 11,8\right)$ " cc " will be displayed.
D. After the call $t(' c$ ', 25,16$)$ "ccccc" will not be displayed.
21. Let us consider the algorithm hindex $(x, n)$, where $\boldsymbol{x}$ is an array with $\boldsymbol{n}\left(1 \leq \boldsymbol{n} \leq 10^{5}\right)$ non-zero natural numbers as elements $(\boldsymbol{x}[1], \boldsymbol{x}[2], \ldots, \boldsymbol{x}[\boldsymbol{n}])$. We define the $\boldsymbol{h}$-index of array $\boldsymbol{x}$, as being the greatest value $\boldsymbol{v}$ for which there are at least $\boldsymbol{v}$ values in $\boldsymbol{x}$ that are greater or equal to $\boldsymbol{v}$. For example, for $\boldsymbol{x}=[3,10,2,7,10,8,50,1,1,5]$ the $\boldsymbol{h}$-index is 5 .

```
Algorithm hIndex(x, n):
    h}\leftarrow
    cont & True
    While cont = True AND h \leq n execute
        pos \leftarrowh
        For i & h + 1, n execute
                If x[i] > x[pos] then
                pos }\leftarrow
                EndIf
        EndFor
        If pos # h then
            tmp }\leftarrowx[pos
            x[pos] \leftarrowx[h]
            x[h]}\leftarrow tm
        EndIf
        If }x[h]\geqh the
            h}\leftarrowh+
        Else
            cont \leftarrowFalse
        EndIf
    EndWhile
    ...
EndAlgorithm
```

Which of the following statements are true?
A. At the point when line 22 would be executed, the array $\boldsymbol{x}$ is sorted in descending order.
B. The algorithm $h \operatorname{Index}(x, n)$ returns the $h$-index of array $\boldsymbol{x}$ if on line 22 we add the instruction Return $h$.
C. The algorithm hIndex $(x, n)$ returns the $\boldsymbol{h}$-index of array $\boldsymbol{x}$ if on line 22 we add the instruction Return h-1.
D. If the algorithm $h \operatorname{Index}(x, n)$ is called for an array $\boldsymbol{x}$ that is sorted in strictly descending order, then the algorithm does not return the $\boldsymbol{h}$-index of array $\boldsymbol{x}$, regardless of what instruction we add on line 22.
22. Let us consider the algorithm ceFace(n, k, x, p), where $\boldsymbol{n}, \boldsymbol{k}$ and $\boldsymbol{p}$ are non-zero natural numbers ( $1 \leq \boldsymbol{n}, \boldsymbol{k}$, $\boldsymbol{p} \leq 10, \boldsymbol{p} \leq \boldsymbol{n})$, and $\boldsymbol{x}$ is an array of $\boldsymbol{p}+1$ elements that are natural numbers $(\boldsymbol{x}[0], \boldsymbol{x}[1], \ldots, \boldsymbol{x}[\boldsymbol{p}])$. We assume that $\boldsymbol{x}[0]$ is initialized with the value 0 .

```
Algorithm ceFace(n, k, x, p):
    If k > p then
        For i & 1, p execute
            Write x[i]
        EndFor
        Write " " //one space
    Else
        For i & x[k - 1] + 1, n execute
            x[k]}\leftarrow
            ceFace(n, k + 1, x, p)
        EndFor
    EndIf
EndAlgorithm
```

Specify which of the following statements are correct.
A. After the algorithm is called with ceFace(3, 1, x, 3) it will call itself 6 more times.
B. If $\boldsymbol{x}[0]$ is initialized with a value different than 0 , after the call ceFace ( $5,1, x, 3$ ) the number of spaces displayed is different than 10.
C. If the algorithm is called with ceFace ( $5,1, x, 4$ ) the following numbers are displayed 1245123413451235 2345, but in a different order.
D. If the algorithm is called with ceFace (5, $1, x, 3)$ the displayed result is 123124125134135145234235 in this order.
23. Let us consider the algorithm $f(\operatorname{sir}, s, d, p)$, where $\operatorname{sir}$ is an array of characters, and $\boldsymbol{s}, \boldsymbol{d}, \boldsymbol{p}$ are non-zero natural numbers $\left(0<\boldsymbol{s}, \boldsymbol{d}, \boldsymbol{p}<10^{9}\right)$. The operator " + " represents the operator for concatenating two arrays of characters. The algorithm print(a) displays the array of characters $\boldsymbol{a}$, then moves to a new line.

```
Algorithm f(sir, s, d, p):
    If s = p AND d = p then
        print(sir)
    EndIf
    If s < p then
        f(sir + "-1 ", s + 1, d, p)
    EndIf
    If s > d then
        f(sir + " 1 ", s, d + 1, p)
    EndIf
. EndAlgorithm
```

Specify which of the following statements are true after the call f("", 0, 0, 2):
A. Two arrays of characters are displayed on separate lines, each array containing 4 numbers whose sum is 0 (for example, the sum of the numbers from the string "-1 1 -1 $1 "$ is 0 ).
B. Only "-1-1 11 " is displayed.
C. Only "-1 $-1 \begin{array}{lll}1 & 1 "\end{array}$ is displayed, but the algorithm does not finish its execution due to an error.
D. If on line 2 the AND operator were replaced with the OR operator, then only "-1-1" would be displayed.
24. Let us consider the algorithm ceFace(a, i, n), where $\boldsymbol{i}$ and $\boldsymbol{n}$ are natural numbers ( $1 \leq \boldsymbol{i}, \boldsymbol{n} \leq 100$ ), and $\boldsymbol{a}$ is an array of $\boldsymbol{n}$ integer numbers $(\boldsymbol{a}[1], \boldsymbol{a}[2], \ldots, \boldsymbol{a}[\boldsymbol{n}],-100 \leq \boldsymbol{a}[\boldsymbol{i}] \leq 100)$. In array $\boldsymbol{a}$ there is at least one positive number. The algorithm $\max (x, y, z)$ returns the maximum between three integer numbers $\boldsymbol{x}, \boldsymbol{y}$ and $\boldsymbol{z}\left(-10^{4} \leq \boldsymbol{x}, \boldsymbol{y}, \boldsymbol{z} \leq 10^{4}\right)$. The algorithm ceFace (a, 1, n) calls the intermediar (a, i, m, n) algorithm, where the parameters $\boldsymbol{a}, \boldsymbol{i}$ and $\boldsymbol{n}$ have the meaning described above, and $\boldsymbol{m}$ is a natural number $(1 \leq \boldsymbol{m} \leq \boldsymbol{n})$.

```
Algorithm intermediar(a, i, m, n):
    s}\leftarrow
    left \leftarrowa[m]
    For k }\leftarrow\textrm{m}, i, -1 execut
        s}\leftarrow\textrm{s}+\textrm{a}[k
        If s > left then
                left \leftarrow s
        EndIf
    EndFor
    s}\leftarrow
    right }\leftarrow\textrm{a}[\textrm{m}
    For i}\leftarrowm, n execut
        s}\leftarrows+a[i
        If s > right then
            right }\leftarrow\textrm{s
        EndIf
    EndFor
    Return max(left, right, left + right - a[m])
EndAlgorithm
```

Specify which of the following statements are true if the algorithm is called with ceFace $(a, i, n)$ :
A. The algorithm identifies a position $\boldsymbol{m}$ of array $\boldsymbol{a}$ such that either the sum of all the elements on positions 1 , $2, \ldots, \boldsymbol{m}$, either the sum of all the elements on positions $\boldsymbol{m}, \boldsymbol{m}+1, \ldots, \boldsymbol{n}$ be the maximum that can be obtained for any $1 \leq \boldsymbol{m} \leq \boldsymbol{n}$, and returns the maximum sum that is obtained like this.
B. The algorithm returns the maximum sum that can be obtained by summing the elements of a subset of the values of array $\boldsymbol{a}$.
C. The algorithm returns the maximum sum that can be obtained for a subsequence of array $\boldsymbol{a}$.
D. In case that all the elements of array $\boldsymbol{a}$ are positive, the algorithm returns the sum of all the elements of array $\boldsymbol{a}$.

# Admission Exam - September 8 ${ }^{\text {th }}, 2023$ <br> Written Exam for Computer Science <br> GRADING AND SOLUTIONS 

DEFAULT: 10 points

| 1. | B | 3.75 points |
| :--- | :---: | :--- |
| 2. | AD | 3.75 points |
| 3. | D | 3.75 points |
| 4. | C | 3.75 points |
| $\mathbf{5 .}$ | BCD | 3.75 points |
| 6. | C | 3.75 points |
| 7. | A | 3.75 points |
| $\mathbf{8 .}$ | B | 3.75 points |
| 9. | AB | 3.75 points |
| 10. | BD | 3.75 points |
| 11. | A | 3.75 points |
| 12. | AD | 3.75 points |
| 13. | AB | 3.75 points |
| 14. | ABC | 3.75 points |
| 15. | ABC | 3.75 points |
| 16. | C | 3.75 points |
| 17. | AC | 3.75 points |
| 18. | BCD | 3.75 points |
| 19. | B | 3.75 points |
| 20. | ACD | 3.75 points |
| 21. | C | 3.75 points |
| 22. | BC | 3.75 points |
| 23. | A | 3.75 points |
| 24. | CD | 3.75 points |

