

Admission Exam – July 19 2022
Written Exam for Computer Science

IMPORTANT NOTE:

Unless further clarification is provided, assume that arithmetical operations are performed over boundless data types (no *overflow* / *underflow*).

Furthermore, arrays and vectors are indexed starting from 1.

1. Let us consider the algorithm $\text{ceFace}(a, b)$, where a and b are natural numbers ($1 \leq a, b \leq 10000$ at the initial call).

```
Algorithm ceFace(a, b):
  While (a MOD 10 = b MOD 10) AND (a ≠ 0) AND (b ≠ 0) execute
    a ← a DIV 10
    b ← b DIV 10
  EndWhile
  If ((a = 0) AND (b = 0)) then
    return True
  else
    return False
  EndIf
EndAlgorithm
```

The algorithm $\text{ceFace}(a, b)$ returns *True* if and only if:

- A. a and b have the same number of digits
- B. a and b are equal
- C. a and b are written using the same digits, but in different sequence
- D. the last digit of a is equal with the last digit of b

2. Let us consider the algorithm $f(a, n)$ where n is a natural number ($2 \leq n \leq 10000$) and a is an array of n natural numbers ($a[1], a[2], \dots, a[n]$, $-100 \leq a[i] \leq 100$, for $i = 1, 2, \dots, n$). The local variable b is an array.

```
Algorithm f(a, n):
  i ← 2
  b[1] ← a[1]
  While i ≤ n execute
    b[i] ← b[i - 1] + a[i]
    i ← i + 1
  EndWhile
  return b[n]
EndAlgorithm
```

Which of the following statements are true?

- A. The algorithm returns the sum of all elements of array a .
- B. The algorithm returns the sum of the last two elements of array a .
- C. The algorithm returns the last element of array a .
- D. The algorithm returns the sum of the last $n - 1$ elements of array a .

3. Which of the following algorithms returns the number of distinct prime factors of a given natural number n ($5 < n < 10^5$ at the initial call).

A.

```
// The length of array prime is n
// prime[i] is True, if
// the number i is prime and False
// otherwise
Algorithm nrFactoriPrimi_A(n, prime):
  d ← 2
  nr ← 0
  p ← 0
  While n > 0 execute
    While n MOD d = 0 execute
      p ← p + 1
      n ← n DIV d
    EndWhile
    If p ≠ 0 then
      nr ← nr + 1
    EndIf
    d ← d + 1
    While prime[d] = False execute
      d ← d + 1
    EndWhile
  EndWhile
  p ← 0
EndWhile
return nr
EndAlgorithm
```

C.

```
Algorithm nrFactoriPrimi_C(n):
  nr ← 0
  For d ← 2, n execute
    If n MOD d = 0 then
      nr ← nr + 1
    EndIf
    While n MOD d = 0 execute
      n ← n DIV d
    EndWhile
  EndFor
  return nr
EndAlgorithm
```

B.

```
Algorithm nrFactoriPrimi_B(n):
  d ← 2
  nr ← 0
  While n > 1 execute
    p ← 0
    While n MOD d = 0 execute
      p ← p + 1
      n ← n DIV d
    EndWhile
    If p > 0 then
      nr ← nr + 1
    EndIf
    If d = 2 then
      d ← d + 1
    else
      d ← d + 2
    EndIf
  EndWhile
  return nr
EndAlgorithm
```

D.

```
Algorithm nrFactoriPrimi_D(n):
  nr ← 0
  d ← 2
  While d * d ≤ n execute
    If n MOD d = 0 then
      nr ← nr + 1
    EndIf
    While n MOD d = 0 execute
      n ← n DIV d
    EndWhile
    d ← d + 1
  EndWhile
  return nr
EndAlgorithm
```

4. Let us consider the algorithm $ceFace(n, m)$, where n is a natural number ($0 \leq n \leq 1000$) with the last digit not equal to 0.

```
Algorithm ceFace(n, m):
  If n = 0 then
    return m
  else
    return ceFace(n DIV 10, m * 10 + n MOD 10)
  EndIf
EndAlgorithm
```

What is the result of the call $ceFace(n, 0)$?

- A. 0 (regardless of the value of n)
- B. n (regardless of the value of n)
- C. The sum of the digits of n
- D. The reverse of number n

5. Let us consider the algorithm $f(x, n)$ where n is a natural number ($2 \leq n \leq 10000$), and x is an array of n natural numbers ($x[1], x[2], \dots, x[n]$, $1 \leq x[i] \leq 10000$, for $i = 1, 2, \dots, n$).

```

Algorithm f(x, n):
  For i = 1, n - 1 execute
    If x[i] = x[i + 1] then
      return False
    EndIf
  EndFor
  return True
EndAlgorithm

```

Which of the following statements are true?

- A. The algorithm returns *False* if two random elements of the array x are distinct.
- B. The algorithm returns *False* if two random elements of the array x are equal.
- C. The algorithm returns *False* if two consecutive elements of the array x are equal.
- D. The algorithm returns *False* if the first two elements of the array x are equal.

6. Let us consider the algorithm $f(x, n)$ where x and n are natural numbers ($0 \leq n \leq 10000$, $0 < x \leq 10000$).

```

1. Algorithm f(x, n):
2.   If n = 0 then
3.     return 1
4.   EndIf
5.   m ← n DIV 2
6.   p ← f(x, m)
7.   If n MOD 2 = 0 then
8.     return p * p
9.   EndIf
10.  return x * p * p
11. EndAlgorithm

```

Which of the following statements are true?

- A. The algorithm returns x at the power of n .
- B. If on line 7, we replace $n \text{ MOD } 2$ with $m \text{ MOD } 2$, then the algorithm returns x at the power of n .
- C. Because of the recursive call on line 6, the lines 7, 8, 9, 10 will never be executed.
- D. The algorithm returns 1 if n is an even number or it returns x if n is an odd number.

7. Considering that all multiplications and divisions require a constant amount of time, what can be stated about the time complexity of the algorithm considered in problem statement 6?

- A. The time complexity depends on parameters x and n .
- B. The time complexity does not depend on the parameter x .
- C. The time complexity is $O(\log \log n)$.
- D. The time complexity is logarithmic based on the parameter n ($O(\log n)$).

8. Let us consider the algorithm $afişare(n)$, where n is a natural number ($1 \leq n \leq 10000$).

```

Algorithm afişare(n):
  If n ≤ 4000 then
    Write n, " "
    afişare(2 * n)
    Write n, " "
  EndIf
EndAlgorithm

```

What will be displayed for the call $afişare(1000)$?

- A. 1000 2000 4000
- B. 1000 2000 4000 4000 2000 1000
- C. 1000 2000 4000 2000 1000
- D. 1000 2000 2000 1000

9. Which could be the values of an array so that, applying the binary search method for value 36, it will be successively compared with values 12, 24, 36:

- A. [2, 4, 7, 12, 24, 36, 50]
- B. [2, 4, 8, 9, 12, 16, 20, 24, 36, 67]
- C. [4, 8, 9, 12, 16, 24, 36]
- D. [12, 24, 36, 42, 54, 66]

10. Which of the following mathematical expressions are equivalent to $x \text{ MOD } y$ for all strictly positive natural numbers x and y ($0 < x, y \leq 10000$)?

- A. $x \text{ DIV } y$
- B. $x - (y * (x \text{ DIV } y))$
- C. $x - (x * (x \text{ DIV } y))$
- D. $x \text{ DIV } y + y \text{ DIV } x$

11. Let us consider variable n that stores a natural number. Which of the following expressions is *True* if and only if n is divisible by 2 and by 3?

- A. $(n \text{ DIV } 2 = 0) \text{ OR } (n \text{ DIV } 3 \neq 0)$
- B. $(n \text{ MOD } 3 = 2) \text{ OR } (n \text{ MOD } 2 = 3)$
- C. $(n \text{ MOD } 2 \neq 1) \text{ AND } (n \text{ MOD } 3 = 0)$
- D. $(n \text{ MOD } 2 = 0) \text{ AND } (n \text{ MOD } 3 \neq 1)$

12. Let us consider variable n that stores a natural number. Which of the following expressions is *True* if and only if n is divisible by 2 and by 3?

- A. $(n \text{ MOD } 2) - (n \text{ MOD } 3) = 0$
- B. $(n \text{ MOD } 2) - (n \text{ MOD } 3) < 0$
- C. $(n \text{ MOD } 2) + (n \text{ MOD } 3) > 0$
- D. $(n \text{ MOD } 2) + (n \text{ MOD } 3) = 0$

13. Let us consider the algorithm $f(n)$, where n is a natural number ($1 \leq n \leq 100$). The operator $"/$ stands for real division (ex. $3 / 2 = 1,5$). State the effect of the algorithm.

```

Algorithm f(n):
  s ← 0; p ← 1;
  For i ← 1, n execute
    s ← s + i
    p ← p * (1 / s)
  EndFor
  return p
EndAlgorithm

```

- A. Evaluates the expression $1/1 * 1/2 * 1/3 * \dots * 1/n$
- B. Evaluates the expression $1/1 * 1/(1*2) * 1/(1*2*3) * \dots * 1/(1*2*3*\dots*n)$
- C. Evaluates the expression $1/1 * 1/(1+2) * 1/(1+2+3) * \dots * 1/(1+2+3+\dots+n)$
- D. Evaluates the expression $1/1 + 1/(1*2) + 1/(1*2*3) + \dots + 1/(1*2*3*\dots*n)$

14. Let us consider the algorithm `prelucrare(s1, lung1, s2, lung2)`, where $s1$ and $s2$ are two arrays of characters of length $lung1$, respectively $lung2$ ($1 \leq lung1, lung2 \leq 1000$). The two strings contain only characters having ASCII codes in the interval $[1, 125]$. The local variable x is an array. Let us consider the algorithm `ascii(s, i)`, which returns the ASCII code of the i -th character of array s .

```

Algorithm prelucreare(s1, lung1, s2, lung2):
  For i = 1, 125 execute
    x[i] ← 0
  EndFor
  For i = 1, lung1 execute
    x[ascii(s1, i)] ← x[ascii(s1, i)] + 1
  EndFor
  For i = 1, lung2 execute
    x[ascii(s2, i)] ← x[ascii(s2, i)] - 1
  EndFor
  ok ← True
  For i = 1, 125 execute
    If x[i] ≠ 0 then
      ok ← False
    EndIf
  EndFor
  return ok
EndAlgorithm

```

What is the result of the algorithm?

- A. The algorithm returns *True* if the arrays of characters *s1* and *s2* have the same length and *False* otherwise.
- B. The algorithm returns *True* if the arrays of characters *s1* and *s2* contain the same characters having the same corresponding frequency and *False* otherwise.
- C. The algorithm returns *True* if in both arrays of characters *s1* and *s2* all characters having ASCII codes in the interval [1, 125] appear and *False* otherwise.
- D. The algorithm returns *True* if the two arrays of characters *s1* and *s2* use different characters and *False* otherwise.

15. What is the result of converting the binary number 100101100111 into base 10?

- A. 2407
- B. 2408
- C. 1203
- D. None of the answers A., B., C.

16. Let us consider an array *a* of *n* natural numbers (*a*[1], *a*[2], ..., *a*[*n*]), the natural number *n* ($1 \leq n \leq 10000$) and a natural number *x*. Which of the following code sequences display the position having the minimal index where the value *x* is situated in the array *a*, or displays -1 if *x* is not found in *a*?

- | | |
|--|--|
| <p>A.</p> <pre> i ← 1 While (i ≤ n) AND (a[i] = x) execute i ← i + 1 EndWhile If i ≤ n then Write i else Write -1 EndIf </pre> | <p>B.</p> <pre> i ← 1 While (i ≤ n) AND (a[i] ≠ x) execute i ← i + 1 EndWhile If i = n + 1 then Write i else Write -1 EndIf </pre> |
| <p>C.</p> <pre> i ← 1 While (i ≤ n) AND (a[i] = x) execute i ← i + 1 EndWhile If i = n + 1 then Write i else Write -1 EndIf </pre> | <p>D.</p> <pre> i ← 1 While (i ≤ n) AND (a[i] ≠ x) execute i ← i + 1 EndWhile If i ≤ n then Write i else Write -1 EndIf </pre> |

17. Let us consider the algorithm $f(x)$, where x is an integer:

```

Algorithm f(x):
  If x = 0 then
    return 0
  else
    If x MOD 3 = 0 then
      return f(x DIV 10) + 1
    else
      return f(x DIV 10)
    EndIf
  EndIf
EndAlgorithm

```

For which value of x does the algorithm return the value 4?

- A. 13369 B. 21369 C. 4 D. 1233

18. Let us consider the algorithm $f(n, i, j)$ where n, i and j are natural numbers ($1 \leq n, i, j \leq 10000$ at the initial call).

```

Algorithm f(n, i, j):
  If i > j then
    Write '*'
  else
    If n MOD i = 0 then
      f(n, i - 1, j)
    else
      If n DIV i ≠ j then
        f(n, i + 1, j - 1)
        Write '0'
      else
        f(n, i + 2, j - 2)
        Write '#'
      EndIf
    EndIf
  EndIf
EndAlgorithm

```

What will be displayed upon the execution of the call $f(15, 3, 10)$?

- A. *000000
 B. *0#000
 C. *0#0000
 D. *0000000

19. Let us consider algorithm $ceFace(n, x)$, where n is a natural number ($1 \leq n \leq 100$) and x is an array of n natural numbers ($x[1], x[2], \dots, x[n]$).

```

Algorithm ceFace(n, x):
  For i = 1, n execute
    c ← x[i]
    x[i] ← x[n - i + 1]
    x[n - i + 1] ← c
  EndFor
EndAlgorithm

```

What will be the new content of array x after executing the algorithm if $n = 6$ and $x = [5, 3, 2, 1, 1, 1]$?

- A. [1, 1, 2, 1, 3, 5] B. [1, 1, 1, 2, 3, 5] C. [5, 3, 2, 1, 1, 1]
 D. None of the other options is correct.

20. Let us consider the algorithm `what(n)`, where n is a natural number ($1 \leq n \leq 1000$ at the initial call).

```

Algorithm what(n):
  If n = 0 then
    return True
  EndIf
  If (n MOD 10 = 3) OR (n MOD 10 = 7) then
    return what(n DIV 10)
  else
    return False
  EndIf
EndAlgorithm

```

Which of the following statements are true?

- A. The algorithm returns *True* if and only if either n can be written using only the digit 3, or n can be written using only the digit 7
 B. The algorithm returns *False* if n contains at least an even digit
 C. The algorithm returns *False* if and only if n contains at least one digit c where $c \neq 3$ and $c \neq 7$
 D. The algorithm returns *True* if and only if n does not contain any digit from the set $\{0, 1, 2, 4, 5, 6, 8, 9\}$

21. Let us consider the algorithm `calcul(x, n)`, where x and n are natural numbers ($1 \leq x \leq 10000$, $1 \leq n \leq 10000$), and $x \leq n$.

```

Algorithm calcul(x, n):
  b ← 1
  For i ← 1, n - x execute
    b ← b * i
  EndFor
  a ← b
  For i ← n - x + 1, n execute
    a ← a * i
  EndFor
  return a DIV b
EndAlgorithm

```

Which of the following statements are true?

- A. If $x = 2$ and $n = 5$, then the algorithm returns 10.
 B. The algorithm returns the number of subsets having x elements from the set $\{1, 2, \dots, n\}$.
 C. The algorithm returns the number of partial permutations of n elements taken x at a time.
 D. The algorithm returns the number of combinations of n elements taken x at a time.

22. At a farm there are chickens and rabbits, each chicken has two legs and each rabbit has four legs. The total number of heads is n and the total number of legs is m ($0 \leq n, m \leq 10^4$). Which of the following algorithms returns *True* and displays all possible pairs of numbers of chickens and rabbits at the farm, or returns *False* if there are no solutions?

A.

```

Algorithm ferma_A(n, m):
  found = False
  For i ← 0, n execute
    j ← n - i
    If 2 * i + 4 * j = m then
      found ← True
      Write i, ' ', j
      Write newline
    EndIf
  EndFor
  return found
EndAlgorithm

```

B.

```

Algorithm ferma_B(n, m):
  found ← False
  For i ← 0, n execute
    For j ← 0, n execute
      If 2 * i + 4 * j = m AND
          i + j = n then
        found ← True
        Write i, ' ', j
        Write newline
      EndIf
    EndFor
  EndFor
  return found
EndAlgorithm

```

C.

```

Algorithm ferma_C(n, m):
  found ← False
  For i ← 0, n execute
    For j ← 0, n - i execute
      If 2 * i + 4 * j = m AND
          i + j = n then
        found ← True
        Write i, ' ', j
        Write newline
      EndIf
    EndFor
  EndFor
  return found
EndAlgorithm

```

D.

```

Algorithm ferma_D(n, m):
  found ← False
  For i ← 0, n execute
    For j ← 0, i execute
      If 2 * i + 4 * j = m AND
          i + j = n then
        found ← True
        Write i, ' ', j
        Write newline
      EndIf
    EndFor
  EndFor
  return found
EndAlgorithm

```

23. Let us consider a natural number n , which can be written as the product of three natural numbers a, b, c , ($n = a * b * c$). Which of the following expressions has as result the remainder of the division of n by the natural number d ($1 \leq n, a, b, c, d \leq 10000$)?

- A. $(a \text{ MOD } d) * b * c$
- B. $((a \text{ MOD } d) * (b \text{ MOD } d) * (c \text{ MOD } d)) \text{ MOD } d$
- C. $(a \text{ MOD } d) * (b \text{ MOD } d) * (c \text{ MOD } d)$
- D. $(a \text{ DIV } d) * (b \text{ DIV } d) * (c \text{ DIV } d)$

24. Let us consider the algorithm $\text{det}(a, n, m)$, where a is an array of n natural numbers ($a[1], a[2], \dots, a[n]$ if $n \geq 1$) or an empty array if $n = 0$. n and m are natural numbers ($0 \leq n \leq 100, 0 \leq m \leq 10^6$).

```

1. Algorithm det(a, n, m):
2.   For i ← 1, n - 1 execute
3.     For j ← i + 1, n execute
4.       If a[i] > a[j] then
5.         tmp ← a[i]
6.         a[i] ← a[j]
7.         a[j] ← tmp
8.       EndIf
9.     EndFor
10.  EndFor
11.  i ← 1
12.  j ← n
13.  b ← False
14.  While i < j execute
15.    If a[i] + a[j] = m then
16.      b ← True
17.    EndIf

```



```

18.      If a[i] + a[j] < m then
19.          i ← i + 1
20.      else
21.          j ← j - 1
22.      EndIf
23.  EndWhile
24.  return b
25. EndAlgorithm

```

Which of the following statements are true?

- A. The algorithm returns *True* if array a contains a pair of numbers having their sum equal to m .
- B. The algorithm always returns *False*.
- C. The algorithm returns *False* if $n = 0$.
- D. Lines 2, ..., 10 of the algorithm sort array a in ascending order.

25. Let us consider the algorithm $\text{magic}(n, a)$, where a is an array of n natural numbers ($a[1], a[2], \dots, a[n]$, $1 \leq n \leq 10000$).

```

Algorithm magic(n, a):
  If n < 2 then
    return False
  EndIf
  For i ← 2, n execute
    If a[i - 1] = a[i] then
      return True
    EndIf
  EndFor
  return False
EndAlgorithm

```

Which of the following statements are true?

- A. For $\text{magic}(5, [2, 5, 4, 5, 4])$ the algorithm returns *False*.
- B. The algorithm indicates if there are duplicates in the array a , if and only if array a is sorted ascending/descending.
- C. For $\text{magic}(9, [1, 2, 3, 4, 4, 5, 6, 7, 9])$ the algorithm returns *True*.
- D. For $\text{magic}(5, [9, 5, 5, 2, 4])$ the algorithm returns *True*.

26. Let us consider the algorithm $f(n, a, b, c)$ where n is a natural number ($n \leq 20$) and a, b, c three integer numbers.

```

Algorithm f(n, a, b, c):
  If n = 0 then
    return 1
  else
    return f(n - 1, a * a, b + 1, c * 2) + f(n - 1, a - 1, b * b, c + 1) + 1
  EndIf
EndAlgorithm

```

What is the return value of the call $f(n, 1, 1, 2)$?

- A. $2^{n+1} - 1$
- B. n
- C. $2^0 + 2^1 + 2^2 + \dots + 2^n$
- D. 2^{n+1}

27. Let us consider the algorithms $f(n, p)$ and $g(n)$, where n and p are initially natural numbers ($1 \leq n, p \leq 10^6$ at the initial call).

```

Algorithm g(n):
  If n < 2 then
    return False
  EndIf
  i ← 2
  While i * i ≤ n execute
    If n MOD i = 0 then
      return False
    EndIf
    i ← i + 1
  EndWhile
  return True
EndAlgorithm

```

```

Algorithm f(n, p):
  If n = 0 then
    return 1
  EndIf
  If n > 0 AND n ≥ p then
    c ← 0
    If g(p) = True then
      c ← c + f(n - p, p + 1)
    EndIf
    return c + f(n, p + 1)
  EndIf
  return 0
EndAlgorithm

```

Which of the following statements are true?

- A. The algorithm $g(n)$ returns *True* if n is prime and *False* otherwise.
- B. The call $f(n, 2)$ returns the number of distinct ways of writing n as a sum of at least one term of distinct prime numbers in strictly ascending order.
- C. The call $f(n, 2)$ returns the sum of the prime divisors of n .
- D. The calls $f(n, 1)$ and $f(n, 2)$ will return the same result, regardless of n .

28. Let us consider the algorithm AlexB(value, n, k, p), where *value* is an array of n natural numbers ($value[1], value[2], \dots, value[n]$), and n, k and p are natural numbers. Initially the array *value* has n elements equal to zero. The algorithm afişare(value, n) displays the array *value* on a single line.

```

Algorithm AlexB(value, n, k, p):
  p ← p + 1
  value[k] ← p
  If p = n then
    afişare(value, n)
  else
    For i ← 1, n execute
      If value[i] = 0 then
        AlexB(value, n, i, p)
      EndIf
    EndFor
  EndIf
  p ← p - 1
  value[k] ← 0
EndAlgorithm

```

What will be displayed on the 10th line, if $n = 5$ and the algorithm is called like: AlexB(value, 5, 1, 0).

- A. 1 5 2 3 4
- B. 1 5 4 0 4
- C. 5 5 5 5 5
- D. 1 2 5 4 3

29. Let us consider the algorithm $f(n)$ where n is a natural number ($1 \leq n \leq 10000$ at the initial call).

```

Algorithm f(n):
  c ← 0
  If n ≠ 0 then
    c ← c + 1
    n ← n & (n - 1) // bitwise AND
    While n ≠ 0 execute
      c ← c + 1
      n ← n & (n - 1) // bitwise AND
    EndWhile
  EndIf
  return c
EndAlgoritm

```

The & operator is the bitwise AND operator; the truth table is:

&	0	1
0	0	0
1	0	1

Example:

2 & 7 in binary: 010 & 111 = 010 which is 2 in base 10.

6 & 1 in binary: 110 & 001 = 000 which is 0 in base 10.

Which of the following statements are **NOT** true?

- A. If n is a power of 2, then $f(n)$ returns value 1.
- B. If $n > 16$ and $n < 32$, then $f(n)$ returns a value from the $\{2, 3, 4, 5\}$ set.
- C. The algorithm returns the number of even numbers strictly smaller than n .
- D. The algorithm returns the number of odd numbers smaller than n .

30. Let us consider algorithm `calcul(v, n)`, where n is a non zero natural number ($1 \leq n \leq 10000$) and v is an array of n integer numbers ($v[1], v[2], \dots, v[n]$). The instruction `return x, y` returns the pair of values (x, y) .

```

Algorithm calcul(v, n):
  i ← n DIV 2 + 1
  j ← i + 1
  k ← i
  p ← j
  While j ≤ n execute
    While (j ≤ n) AND (v[i] = v[j]) execute
      j ← j + 1
    EndWhile
    If j - i > p - k then
      k ← i
      p ← j
    EndIf
    i ← j
    j ← j + 1
  EndWhile
  If j - i > p - k then
    k ← i
    p ← j
  EndIf
  return p - k, k
EndAlgorithm

```

Which of the following statements are true?

- A. If the array contains only one element, the algorithm returns 0, -1
- B. If $n = 2$ and the array's two elements are symmetric with respect to 0 (for example -5, 5), the result will be -1, 1
- C. If $n = 2$ and the array's two elements have consecutive values (for example 3, 4), the algorithm will always return the values 1, 2
- D. One of the numbers returned by the algorithm represents the length of the longest sequence containing equal values from the second half of the array for any even number $n > 1$