SYLLABUS

1. Information regarding the programme

| 1.1 Higher education institution | Babes-Bolyai University, Cluj-Napoca |
|----------------------------------|--------------------------------------|
| 1.2 Faculty | Mathematics and Computer Science |
| 1.3 Department | Department of Mathematics |
| 1.4 Field of study | Mathematics and Computer Science |
| 1.5 Study cycle | Bachelor |
| 1.6 Study programme / | Mathematics and Computer Science |
| Qualification | |

2. Information regarding the discipline

| 2.1 Name of the discipline Complements of Mathematical Analysis | | | | |
|---|--|--|--|--|
| 2.2 Course coordinator | Lect. dr. Berinde Stefan | | | |
| 2.3 Seminar coordinator | Lect. dr. Berinde Stefan | | | |
| 2.4. Year of study 2 2.5 4 | 2.6. Type of evaluation VP 2.7 Type of Op. | | | |
| Semester | discipline | | | |

3. Total estimated time (hours/semester of didactic activities)

| 3.1 Hours per week | 4 | Of which: 3.2 course | 2 | 3.3 seminar/laboratory | 2 |
|---|---------|---------------------------|----------|------------------------|-------|
| 3.4 Total hours in the curriculum | 56 | Of which: 3.5 course | 28 | 3.6 seminar/laboratory | 28 |
| Time allotment: | · | | | | hours |
| Learning using manual, course suppo | rt, bib | liography, course notes | , | | 36 |
| Additional documentation (in libraries, on electronic platforms, field documentation) | | | | | 13 |
| Preparation for seminars/labs, homew | ork, p | papers, portfolios and es | ssays | | 30 |
| Tutorship | | | | | 10 |
| Evaluations | | | | | 30 |
| Other activities: | | | | | |
| 3.7 Total individual study hours | 119 | | | | |
| 3.8 Total hours per semester | 175 | | | | |
| 3.9 Number of ECTS credits | 7 | | | | |

4. Prerequisites (if necessary)

| 4.1. curriculum | Mathematical Analysis I |
|-------------------|---|
| 4.2. competencies | Understanding calculus on the real axis |

5. Conditions (if necessary)

| 5.1. for the course | Class room with blackboard |
|---------------------------|----------------------------|
| 5.2. for the seminar /lab | Class room with blackboard |
| activities | |

6. Specific competencies acquired

| ofessional mpetencies |
|--------------------------|
| Pro |
| 2 2 |

- C1.5 Elaborarea unor proiecte si lucrari de prezentare a unor rezultate si metode matematice.
 - C5.4 Evaluarea comparativa si utilizarea eficienta a diferitelor metode de demonstratie

Transversal competencies

CT2. Desfasurarea eficienta si eficace a activitatilor organizate in echipa

7. Objectives of the discipline (outcome of the acquired competencies)

| 7.1 General objective of the discipline | Complementary results from the field of classical analysis on the real axis |
|--|--|
| 7.2 Specific objective of the discipline | a short history of mathematical analysis reccurent sequences and their connection with continued fractions and generating functions computation techniques based on operations with power series study of some remarcable series and their connection with Riemann zeta function study of some remarcable improper integrals: Euler's Gamma and Beta functions A short introduction to calculus of variations |

8. Content

| 8.1 Cc | ourse | Teaching methods | Remarks |
|--------|---|------------------------------------|---------|
| 1. | A short history of mathematical analysis | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 2. | Decimal and continued fractions | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 3. | Recurrent sequences | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 4. | Remarcable numbers as limits of sequences | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 5. | Arithmetic-geometric mean. Gauss formula | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 6. | Toeplitz theorem and applications | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 7. | Stirling formula | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 8. | Infinite products | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 9. | Operations with power series | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 10 | . Euler sum and Bernoulli numbers | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 11 | . Riemann zeta function | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 12 | . Euler's Gamma and Beta functions | interactive exposure, explanation, | |
| | | didactical demonstration | |
| 13 | . Proper integrals with parameter | interactive exposure, explanation, | |

| | didactical demonstration | |
|--|------------------------------------|--|
| 14. Introduction to calculus of variations | interactive exposure, explanation, | |
| | didactical demonstration | |

Bibliography

- 1. Cobzas S.: Analiza matematica (Calcul diferential), Presa Universitara Clujeana, 1997
- 2. Gelbaum B.R., Olmsted J.M.H.: Contraexample in analiza, Ed. Stiintifica, Bucuresti, 1973
- 3. Kaczor W.J., Nowak M.T.: Problems in Mathematical Analysis, vol. I and II, AMS, 2001
- 4. Megan M.: Bazele Analizei matematice, vol. 1,2,3, Editura Eurobit, 1997, 1997, 1998
- 5. Siretchi, Gh.: Calcul diferential si integral, vol. I si II, Editura Stiintifica si Enciclopedica, Bucuresti, 1985
- 6. Wilf H.S.: generatingfunctionology, A.K. Peters Ltd., Massachusetts, 2006
- 7. Zorich V.A.: Mathematical Analysis I, Springer, Berlin, 2004

| 8.2 Seminar / laboratory | Teaching methods | Remarks |
|--|----------------------------------|---------|
| Classic inequalities | project exposure by student team | |
| 2. Decimal and continued fractions | project exposure by student team | |
| 3. Recurrent sequences | project exposure by student team | |
| 4. Remarcable numbers as limits of sequences | project exposure by student team | |
| 5. Arithmetic-geometric mean. Gauss formula | project exposure by student team | |
| 6. Toeplitz theorem and applications | project exposure by student team | |
| 7. Stirling formula | project exposure by student team | |
| 8. Infinite products | project exposure by student team | |
| 9. Operations with power series | project exposure by student team | |
| 10. Euler sum and Bernoulli numbers | project exposure by student team | |
| 11. Riemann zeta function | project exposure by student team | |
| 12. Euler's Gamma and Beta functions | project exposure by student team | |
| 13. Proper integrals with parameter | project exposure by student team | |
| 14. Introduction to calculus of variations | project exposure by student team | |

Bibliography

- 1. Cobzas S.: Analiza matematica (Calcul diferential), Presa Universitara Clujeana, 1997
- 2. Duren P.: Invitation to Classical Analysis, AMS, 2012
- 3. Kaczor W.J., Nowak M.T.: Problems in Mathematical Analysis, vol. I si II, AMS, 2001
- 4. Siretchi, Gh.: Calcul diferential si integral, vol. I si II, Editura Stiintifica si Enciclopedica, Bucuresti, 1985
- 5. ***: Pagina cursului Complemente de analiza matematica (notite de curs ale titularului),

http://math.ubbcluj.ro/~sberinde/comp/

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

• This lecture is useful for teacher and research candidates in mathematics, enriching their knowledge in classical mathematical aanalysis. More specifically, we address new methods and results which might be useful later for a master degree preparation in mathematics or a related field.

10. Evaluation

| Type of activity | 10.1 Evaluation criteria | 10.2 Evaluation methods | 10.3 Share in the |
|------------------|--------------------------|-------------------------|-------------------|
| | | | grade (%) |
| 10.4 Course | Knowledge of basic | Written exam | 50 |
| | concepts and results, | | |

| | problem solving | | | |
|------------------------------------|-------------------------------|------------------------|----|--|
| 10.5 Seminar/lab activities | Individual project evaluation | Continous observation, | 50 | |
| | | dialogue | | |
| 10.6 Minimum performance standards | | | | |
| Grade 5 | | | | |

| Date | Signature of course coordinato | r Signature of seminar coordinator |
|------------------|-------------------------------------|------------------------------------|
| 8 april 2018 | lect.dr. Berinde Stefan | lect.dr. Berinde Stefan |
| Date of approval | Signature of the head of department | |
| | prof.dr. Octavian Agratini | |