## SYLLABUS

## 1. Information regarding the programme

| 1.1 Higher education <br> institution | Babes-Bolyai University |
| :--- | :--- |
| 1.2 Faculty | Mathematics and Computer Science |
| 1.3 Department | Department of Mathematics |
| 1.4 Field of study | Mathematics |
| 1.5 Study cycle | Master of Science |
| 1.6 Study programme / <br> Qualification |  |

## 2. Information regarding the discipline

| 2.1 Name of the discipline (en) <br> (ro) | Topics in Geometry III |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 2.2 Course coordinator | Prof. PhD. Dorin Andrica |  |  |

3. Total estimated time (hours/semester of didactic activities)

| 3.1 Hours per week | $\mathbf{3}$ | Of which: 3.2 course | $\mathbf{2}$ | 3.3 <br> seminar/laboratory | $\mathbf{1}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 3.4 Total hours in the curriculum | $\mathbf{3 6}$ | Of which: 3.5 course | $\mathbf{2 4}$ | 3.6 <br> seminar/laboratory | $\mathbf{1 2}$ |
| Time allotment: |  | hours |  |  |  |
| Learning using manual, course support, bibliography, course notes | $\mathbf{5 0}$ |  |  |  |  |
| Additional documentation (in libraries, on electronic platforms, field documentation) | $\mathbf{3 0}$ |  |  |  |  |
| Preparation for seminars/labs, homework, papers, portfolios and essays | $\mathbf{3 4}$ |  |  |  |  |
| Tutorship | $\mathbf{4 0}$ |  |  |  |  |
| Evaluations | $\mathbf{1 0}$ |  |  |  |  |
| Other activities: ............... |  |  |  |  |  |
| 3.7 Total individual study hours | $\mathbf{1 6 4}$ |  |  |  |  |
| 3.8 Total hours per semester | $\mathbf{2 0 0}$ |  |  |  |  |
| 3.9 Number of ECTS credits | $\mathbf{7}$ |  |  |  |  |

4. Prerequisites (if necessary)

| 4.1. curriculum | Minimal knowledges of vector calculus, complex numbers and <br> analytic geometry |
| :--- | :--- |
| 4.2. competencies | $\bullet$ |

## 5. Conditions (if necessary)

| 5.1. for the course | $\bullet$ |
| :--- | :--- |
| 5.2. for the seminar /lab <br> activities | $\bullet$ |

## 6. Specific competencies acquired

| • The capacity to understand methodical and scientific mathematical works, to propose new |
| :--- | :--- | :--- |
| Problems and to open new research. |

7. Objectives of the discipline (outcome of the acquired competencies)

| 7.1 General objective of the |
| :--- | :--- |
| discipline |\(\left|\begin{array}{l}1. To obtain new notions and results in geometry which are useful to understand <br>

and to improve new directions in modern mathematics. <br>
2. To get the abilities to apply the new theoretical results in the study of some <br>
concrete problems in a modern setting. <br>

3. To realize connections with other mathematical disciplines.\end{array}\right|\)| 7.2 Specific objective of the |
| :--- |
| discipline | | At the end of the course the students will be able |
| :--- |
| 1) to identify correctly various geometric configurations and the existing |
| connections; |
| 2) to combine the results and the methods in order to solve geometry problem |
| of various level of difficulties. |

## 8. Content

| 8.1 Course | Teaching methods | Remarks |
| :---: | :--- | :--- |
| 1. Week 1: Elements of vector algebra in plane and <br> space. | presentation, <br> explanation, dialog, <br> problem-solving |  |
| 2. Week 2: The dot product and Lagrange Theorem. | presentation, <br> explanation, dialog, <br> problem-solving |  |


| 3. Week 3: The cross product and the triple scalar product. | presentation, explanation, dialog, problem-solving |  |
| :---: | :---: | :---: |
| 4. Week 4: The group of isometries | presentation, explanation, dialog, problem-solving |  |
| 5. Week 5: Nonisometric transformations : homothety | presentation, explanation, dialog, problem-solving |  |
| 6. Week 6: Nonisometric transformations : inversion | presentation, explanation, dialog, problem-solving |  |
| 7. Week 7: The real product of two complex numbers | presentation, explanation, dialog, problem-solving |  |
| 8. Week 8: The complex product of two complex numbers | presentation, explanation, dialog, problem-solving |  |
| 9. Week 9: The n-th roots of unity | presentation, explanation, dialog, problem-solving |  |
| 10. Week 10: Classical theorems proved by complex numbers | presentation, explanation, dialog, problem-solving |  |
| 11. Week 11: The group of plane isometries described by complex numbers | presentation, explanation, dialog, problem-solving |  |
| 12. Week 12: Nonisometric transformations of complex plane | presentation, explanation, dialog, problem-solving |  |
|  |  |  |
| Bibliography <br> 1.Andreescu,T.,Andrica,T.,Complex Numbers from A to...Z, Second Edition, Birkhauser,2014. <br> 2.Andrica,D, GEOMETRIE. Teme pentru perfectionarea profesorilor de matematica 4, Casa Cartii de Stiinta, 2017. <br> 3.Andrica,D.,s.a.,Teme si probleme alese de geometrie,Editura Plus,Bucuresti,2002. <br> 4.Andrica,D.,s.a.,Matematica de baza,Editura Studium,Editia a 4-a,Cluj-Napoca,2004. <br> 5.Berger,M.,Geometrie, CEDUC NathanParis, 1977-1978. <br> 6.Coxeter,H.S.M.,Greitzer,S.L.,Geometry Revisited,Random House,New York, 1967. <br> 7.Engel,A.,Problem-Solving Strategies,Springer Verlag, 1998. <br> 8.Fenn,R.,Geometry,Springer Verlag,2001. <br> 9.Hahn,L.,Complex Numbers \& Geometry,The Mathematical Association of America, 1994. <br> 10.Mihalescu,C.,Geometria elementelor remarcabile, Societatea de Stiinte Matematice din Romania,2007. |  |  |
| 8.2 Seminar / laboratory | Teaching methods | Remarks |
| 1. Collinearity problems solved by vector algebra | conversation, dialog, problem-solving strategies |  |


| 2. Metric problems solved by the dot product | conversation, dialog, <br> problem-solving <br> strategies |  |
| :---: | :--- | :--- |
| 3. Problems involving areas | conversation, dialog, <br> problem-solving <br> strategies |  |
| 4. Problems solved by translation | conversation, dialog, <br> problem-solving <br> strategies |  |
| 5. Problems solved by symmetry | conversation, dialog, <br> problem-solving <br> strategies |  |
| 6. Problems solved by homothety | conversation, dialog, <br> problem-solving <br> strategies |  |
| 7. Problems solved by inversion | conversation, dialog, <br> problem-solving <br> strategies |  |
| 8. Metric problems solved by the real product | conversation, dialog, <br> problem-solving <br> strategies |  |
| 9. Written paper | conversation, dialog, <br> problem-solving <br> strategies |  |
| 10. Problems involving areas solved by the |  |  |
| complex product |  |  |$\quad$| conversation, dialog, |
| :--- |
| problem-solving |
| strategies |, | conversation, dialog, |
| :--- |
| problem-solving |
| strategies |,

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program
1) The contents is directed towards applications of the methods of Geometry to mathematical didactics and problem solving.
2) Most of the topics in the course are included in the national curriculum and are necessary for various exams for teachers in general schools and high schools.

## 10. Evaluation

| Type of activity | 10.1 Evaluation criteria | 10.2 Evaluation methods | 10.3 Share in the <br> grade (\%) |
| :--- | :--- | :--- | :--- |
| 10.4 Course | To understand the notions <br> and the results by typical <br> examples or <br> counterexamples. To be <br> able to present the main <br> ideas in the proof of the <br> theoretical results. | Written exam | $60 \%$ |
|  | To develop a specific <br> subject by reading the <br> bibliography. | Report | $10 \%$ |
| 10.5 Seminar/lab activities | Solving problems skills | Quiz <br> Continous observations | $10 \%$ |

Date
18.04.2018

Prof. Dr. Dorin Andrica
Signature of seminar coordinator
Prof. Dr. Dorin Andrica

Date of approval
21.04.2018

Signature of the head of department
Prof. Dr. Octavian Agratini

