#### **SYLLABUS**

# ${\bf 1.}\ {\bf Information}\ {\bf regarding}\ {\bf the}\ {\bf programme}$

| 1.1 Higher education institution    | Babeş-Bolyai University Cluj-Napoca         |  |
|-------------------------------------|---|--|
| 1.2 Faculty                         | Faculty of Mathematics and Computer Science |  |
| 1.3 Department                      | Department of Mathematics                   |  |
| 1.4 Field of study                  | Computer Science                            |  |
| 1.5 Study cycle                     | Bachelor of Science                         |  |
| 1.6 Study programme / Qualification | Computer Science                            |  |

## 2. Information regarding the discipline

| 2.1 Name of the discipline        | Mathematical Analysis   |  |  |
|-----------------------------------|---|--|--|
| 2.2 Course coordinator            | Prof. Nicolae Popovici, Ph.D. habil.                          |  |  |
| 2.3 Seminar coordinator           | Prof. Nicolae Popovici, Ph.D. habil.                          |  |  |
| 2.4. Year of study 1 2.5 Semester | 1 2.6. Type of evaluation E 2.7 Type of discipline Compulsory |  |  |

## 3. Total estimated time (hours/semester of didactic activities)

| 3.1 Hours per week   | 4       | Of which: 3.2 course    | 2       | 3.3 seminar/laboratory | 2     |
|--|---------|-------------------------|---------|------------------------|-------|
| 3.4 Total hours in the curriculum                                      | 56      | Of which: 3.5 course    | 28      | 3.6 seminar/laboratory | 28    |
| Time allotment:  |         |                         |         |                        | hours |
| Learning using manual, course supp                                     | ort, bi | bliography, course not  | es      |                        | 30    |
| Additional documentation (in librari                                   | es, on  | electronic platforms, f | field c | locumentation)         | 10    |
| Preparation for seminars/labs, homework, papers, portfolios and essays |         |                         |         | 20                     |       |
| Tutorship  |         |                         |         | 14                     |       |
| Evaluations  |         |                         |         |                        | 20    |
| Other activities   |         |                         | -       |                        |       |
| 3.7 Total individual study hours 94                                    |         |                         |         |                        |       |
| 3.8 Total hours per semester 150                                       |         |                         |         |                        |       |
| 3.9 Number of ECTS credits 6   |         |                         |         |                        |       |

# **4. Prerequisites** (if necessary)

| 4.1. curriculum   | High-school calculus                              |
|-------------------|---|
| 4.2. competencies | Computing limits, derivatives and antiderivatives |
|                   | Analytic thinking                                 |

## **5. Conditions** (if necessary)

| 5.1. for the course                  | Lecture hall equipped with blackboard and beamer |
|--------------------------------------|--|
| 5.2. for the seminar /lab activities | Classroom equipped with blackboard               |

# 6. Specific competencies acquired

| Professional competencies | <ul> <li>To understand, in-depth, some concepts and results of mathematical analysis.</li> <li>Ability to use mathematical methods for solving practical problems</li> </ul>   |
|---------------------------|--|
| Transversal competencies  | To apply rigorous and efficient work rules, by adopting a responsible attitude towards the scientific and didactic activities. To develop the own creative potential in specific areas, following the professional ethical norms and principles. |

# **7. Objectives of the discipline** (outcome of the acquired competencies)

| 7.1 General objective of  | To acquire elementary knowledge about differential and integral calculus for |  |
|---------------------------|--|--|
| the discipline            | real-valued functions of one or several real variables                       |  |
|                           |  |  |
| 7.2 Specific objective of | Students should acquire knowledge about:                                     |  |
| the discipline            | <ul> <li>Sequences and series of real numbers,</li> </ul>                    |  |
|                           | Power series;  |  |
|                           | Limits of functions;   |  |
|                           | Partial derivatives and the differential;                                    |  |
|                           | Extremum points  |  |
|                           | Riemann integrals, improper integrals, multiple integrals                    |  |

## 8. Content

| 8.1 Course  | Teaching methods  | Remarks |
|---|---|---------|
| 1. The real numbers: some basic concepts  | Direct instruction, mathematical proof, exemplification |         |
| 2. Sequences of real numbers  | Direct instruction, mathematical proof, exemplification |         |
| 3. Series of real numbers; Series with nonnegative terms (I)                                | Direct instruction, mathematical proof, exemplification |         |
| 4. Series with nonnegative terms (II); Alternating series                                   | Direct instruction, mathematical proof, exemplification |         |
| 5. Limits, continuity and differentiation of real-valued functions of one real variable     | Direct instruction, mathematical proof, exemplification |         |
| 6. Higher order derivatives; Taylor series and power series                                 | Direct instruction, mathematical proof, exemplification |         |
| 7. The Riemann integral; Improper integrals   | Direct instruction, mathematical proof, exemplification |         |
| 8. The Euclidean (topological) space R <sup>n</sup> ; Sequences of points in R <sup>n</sup> | Direct instruction, mathematical proof, exemplification |         |
| 9. Limits and continuity of real-valued functions of several variables                      | Direct instruction, mathematical proof, exemplification |         |
| 10. Partial derivatives and the differential  | Direct instruction, mathematical proof, exemplification |         |

| 11. Local extremum points for real-valued | Direct instruction, mathematical |
|---|----------------------------------|
| functions of several variables            | proof, exemplification           |
| 12. Double integrals                      | Direct instruction, mathematical |
|   | proof, exemplification           |
| 13. Triple and multiple integrals         | Direct instruction, mathematical |
|   | proof, exemplification           |
| 14. Change of variables                   | Direct instruction, mathematical |
|   | proof, exemplification           |

#### Bibliography

- 1. R.G. Bartle, D.R. Sherbert, Introduction to Real Analysis, 4<sup>th</sup> ed., John Wiley & Sons Inc., New York, 2011.
- 2. W.W. Breckner, Analiză matematică. Topologia spațiului  $\mathbb{R}^n$ , Universitatea din Cluj-Napoca, Cluj-Napoca, 1985.
- 3. Ş. Cobzaş, Analiză matematică Calculul diferențial, Presa Universitară Clujeană, Cluj-Napoca, 1997.
- 4. M. Mureşan, A Concret Approach to Classical Analysis, Springer, New York, 2008.
- 5. M. Oberguggenberger, A. Ostermann, Analysis for Computer Scientists, Foundations, Methods, and Algorithms, Springer, London, 2011.
- 6. W. Rudin, Principles of Mathematical Analysis, 3<sup>rd</sup> ed., McGraw-Hill Inc., New York, 1976.

|   |                             | Remarks |
|---|-----------------------------|---------|
| 8.2 Seminar / laboratory                          | Teaching methods            |         |
| 1. Classical inequalities and other properties of | Problem-based instruction,  |         |
| real numbers                                      | debate, mathematical proofs |         |
| 2. Sequences of real numbers                      | Problem-based instruction,  |         |
|   | debate, mathematical proofs |         |
| 3. Computing the sum of some series of real       | Problem-based instruction,  |         |
| numbers   | debate, mathematical proofs |         |
| 4. Convergence/divergence of some series of       | Problem-based instruction,  |         |
| real numbers                                      | debate, mathematical proofs |         |
| 5. Limits, continuity and differentiation of      | Problem-based instruction,  |         |
| real-valued functions of one real variable        | debate, mathematical proofs |         |
| 6. Higher order derivatives; Taylor series and    | Problem-based instruction,  |         |
| power series                                      | debate, mathematical proofs |         |
| 7. Riemann integrals                              | Problem-based instruction,  |         |
|   | debate, mathematical proofs |         |
| 8. Improper integrals                             | Problem-based instruction,  |         |
|   | debate, mathematical proofs |         |
| 9. The topology of the space R <sup>n</sup>       | Problem-based instruction,  |         |
|   | debate, mathematical proofs |         |
| 10. Limits and continuity of real-valued          | Problem-based instruction,  |         |
| functions of several variables                    | debate, mathematical proofs |         |
| 11. Partial derivatives and the differential      | Problem-based instruction,  |         |
|   | debate, mathematical proofs |         |
| 12. Local and global extremum points of real-     | Problem-based instruction,  |         |
| valued functions                                  | debate, mathematical proofs |         |
| 13. Multiple integrals                            | Problem-based instruction,  |         |
|   | debate, mathematical proofs |         |
| 14. Change of variables                           | Problem-based instruction,  |         |
|   | debate, mathematical proofs |         |

#### Bibliography

- 1. D.I. Duca, E. Duca, Exerciții și probleme de analiză matematică, vol. I, II, Casa Cărții de Știință, Cluj-Napoca, 2007, 2009.
- 2. W.J. Kaczor, M.T. Nowak, Problems in Mathematical Analysis, vol. I, II, III, American Mathematical Society, 2000, 2001, 2003.
- 3. T. Trif, Probleme de calcul diferențial și integral în R<sup>n</sup>, Casa Cărții de Știință, Cluj-Napoca, 2003.

# 9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

The course ensures a solid theoretical background, according to national and international standards

#### 10. Evaluation

| Type of activity                                      | 10.1 Evaluation criteria  | 10.2 Evaluation methods | 10.3 Share in the |
|---|---|-------------------------|-------------------|
|   |   |                         | grade (%)         |
| 10.4 Course   | <ul> <li>Knowledge of theoretical concepts and theoretical results;</li> <li>Ability to solve practical exercises and theoretical problems</li> </ul> | Final written exam      | 75%               |
| 10.5 Seminar/lab activities                           | Problem solving   | Midterm test            | 25%               |
| 10.6 Minimum performance standards                    |   |                         |                   |
| The final grade should be greater than or equal to 5. |   |                         |                   |

| Date             | Signature of course coordinator      | Signature of seminar coordinator     |
|------------------|--------------------------------------|--------------------------------------|
| 22.04.2018       | Prof. Nicolae Popovici, Ph.D. habil. | Prof. Nicolae Popovici, Ph.D. habil. |
|                  |                                      |                                      |
|                  |                                      |                                      |
| Date of approval |                                      | Signature of the head of department  |
|                  |                                      | Prof. Octavian Agratini, Ph.D.       |